

# Numbers and Algebra

Lesson One : Repeated multiplication.

**Lesson Two**: Non-negative integer powers.

**Lesson Three:** Negative integer powers.

**Lesson Four**: Scientific notation of the rational number.

Lesson Five : Order of mathematical operations.

Lesson Six : The square root of a perfect square rational number.

**Lesson Seven:** Solving equations of the first degree in

one unknown in Q.

**Lesson Eight:** Solving inequalities in Q.

# Ghiyath Al-Din Ibn Masoud Al-Kashi:

He was an Arab scientist who had many investigations in mathematics:

- He had invented the decimal fraction.
- He put a theory concerning the sum of the natural numbers that are raised to the fourth power.
- · He reached a very accurate rate for the approximate ratio  $(\pi)$  that nearly equates the accuracy of the calculators.



Ghiyath Al-Din Ibn Masoud Al-Kashi ( 1380 A.D. - 1436 A.D.)

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Lesson One



# Repeated multiplication

We had known before in the set of integers that :  $3^4 = 3 \times 3 \times 3 \times 3$  where we found that the number 3 has repeated 4 times in the multiplication operation and we read it as «3 to the power 4»

Also, in the set of rational Q, we find that:

• 
$$\left(\frac{2}{3}\right)^3 = \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} = \frac{2 \times 2 \times 2}{3 \times 3 \times 3} = \left|\frac{2^3}{3^3}\right| = \frac{8}{27}$$

$$\bullet \left[ \left( \frac{2}{3} \right)^4 \right] = \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} = \frac{2 \times 2 \times 2 \times 2}{3 \times 3 \times 3 \times 3} = \boxed{\frac{2^4}{3^4}} = \frac{16}{81}$$

## From the previous, we deduce that:

If  $\frac{a}{b}$  is a rational number and n is a positive integer, then:  $\left(\frac{a}{b}\right)^n = \frac{a}{b} \times \frac{a}{b} \times \frac{a}{b}$  ... to n times

It is read as  $\frac{a}{b}$  to the power n » or «the n<sup>th</sup> power of the number  $\frac{a}{b}$  »

*i.e.* 
$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

For example: • 
$$(\frac{2}{5})^3 = \frac{2^3}{5^3} = \frac{8}{125}$$

• 
$$(0.7)^2 = \left(\frac{7}{10}\right)^2 = \frac{7^2}{10^2} = \frac{49}{100}$$

#### Remark

If:  $\frac{a}{b}$  is a rational number, then:  $\left(\frac{a}{b}\right)^0 = 1$  where  $a \neq 0$ 

For example: 
$$\bullet \left(\frac{1}{5}\right)^0 = 1$$

$$\bullet \left(-\frac{3}{7}\right)^0 = 1$$

#### Remark

If  $\frac{a}{b}$  is a rational number , and m is a positive integer , then :

$$\left(-\frac{a}{b}\right)^m = \left(\frac{a}{b}\right)^m$$
 when m is an even number.

For example: 
$$\left(-\frac{1}{2}\right)^4 = \left(\frac{1}{2}\right)^4 = \frac{1}{16}$$

$$\left(-\frac{a}{b}\right)^m = -\left(\frac{a}{b}\right)^m$$
 when m is an odd number.

For example: 
$$\left(-\frac{1}{2}\right)^3 = -\left(\frac{1}{2}\right)^3 = -\frac{1}{8}$$

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#### Try by yourself

Find each of the following in its simplest form:

$$\left(\frac{1}{5}\right)^2 = \cdots = \cdots$$

$$(-\frac{4}{5})^4 = \dots = \dots$$

#### Example Find each of the following in the simplest form:

$$2(-\frac{5}{4})^2 \times (\frac{2}{5})^4$$

$$3 \left(3\frac{1}{2}\right)^2 \div \left(-10\frac{1}{2}\right)$$

$$3 \left(3\frac{1}{2}\right)^2 \div \left(-10\frac{1}{2}\right) \qquad 4 \left(-\frac{2}{5}\right)^2 \times \left(-\frac{5}{2}\right)^3 \times \left(\frac{1}{5}\right)^0$$

#### Solution

$$3 \left(3\frac{1}{2}\right)^2 \div \left(-10\frac{1}{2}\right) = \left(\frac{7}{2}\right)^2 \div \left(-\frac{21}{2}\right) = \frac{7^2}{2^2} \times \left(-\frac{2}{21}\right) = \frac{49}{4} \times \left(-\frac{2}{21}\right) = -\frac{7}{6}$$

$$4 \left(-\frac{2}{5}\right)^2 \times \left(-\frac{5}{2}\right)^3 \times \left(\frac{1}{5}\right)^0 = \frac{2^2}{5^2} \times \left(-\frac{5^3}{2^3}\right) \times 1 = \frac{4}{25} \times \left(-\frac{125}{8}\right) = -\frac{5}{2}$$

## Try by yourself

Find in the simplest form :  $\left(-\frac{3}{9}\right)^2 \times \left(\frac{9}{4}\right)^2 \times \left(\frac{81}{16}\right)^0$ 

**Example** 2 If  $x = -\frac{1}{2}$ ,  $y = \frac{1}{4}$  and z = 4, find the value of:  $(x + y)^3 \times z^3$ 

Solution 
$$(x + y)^3 \times z^3 = \left(-\frac{1}{2} + \frac{1}{4}\right)^3 \times 4^3 = \left(-\frac{2}{4} + \frac{1}{4}\right)^3 \times 4^3 = \left(-\frac{1}{4} + \frac{1}{4}\right)^3 \times 4^3 = -\frac{1}{4^3} \times 4^3 = -1$$

## Try by yourself

If  $x = -\frac{2}{3}$ ,  $y = \frac{1}{2}$  and  $z = -\frac{4}{3}$ , find the value of:  $x^2 - y^2 z$ 

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Lesson Two



# Non-negative integer powers

#### The first law

From the definition of repeated multiplication , we know that :

$$\left(\frac{2}{3}\right)^{3} \times \left(\frac{2}{3}\right)^{4}$$

$$\downarrow$$

$$\frac{2}{3} \times \frac{2}{3} \times \frac{2}{3}$$

$$\frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} = \left(\frac{2}{3}\right)^{7}$$

Notice that : 3 + 4 = 7i.e. When multiplying the like bases, we add their powers (indices).

i.e. If 
$$\frac{a}{b}$$
 is a rational number , n and m are non-negative integers , then  $\left(\frac{a}{b}\right)^n \times \left(\frac{a}{b}\right)^m = \left(\frac{a}{b}\right)^{n+m}$ 

#### For example:

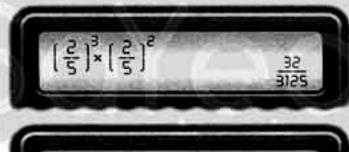
$$\bullet \left(\frac{2}{5}\right)^3 \times \left(\frac{2}{5}\right)^2 = \left(\frac{2}{5}\right)^{3+2} = \left(\frac{2}{5}\right)^5$$

• 
$$\left(-\frac{1}{2}\right)^4 \times \left(-\frac{1}{2}\right)^3 = \left(-\frac{1}{2}\right)^{4+3} = \left(-\frac{1}{2}\right)^7$$

You can check the truth of the previous law by using the calculator as follows : • .....

$$\bullet \left(\frac{2}{5}\right)^3 \times \left(\frac{2}{5}\right)^2 = \frac{32}{3125}$$

$$\bullet \left(\frac{2}{5}\right)^5 = \frac{32}{3125}$$





## Example 1

Calculate each of the following , then put the result in its simplest form :

$$(-\frac{1}{3})^3 \times (\frac{1}{3})^2$$

$$\frac{3}{4} \times \left(-\frac{3}{4}\right)^2$$

## Solution

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$$2 \left(-\frac{1}{3}\right)^3 \times \left(\frac{1}{3}\right)^2 = -\left(\frac{1}{3}\right)^3 \times \left(\frac{1}{3}\right)^2$$
$$= -\left(\frac{1}{3}\right)^5 = -\frac{1^5}{3^5} = -\frac{1}{243}$$

$$3 \frac{3}{4} \times \left(-\frac{3}{4}\right)^2 = \frac{3}{4} \times \left(\frac{3}{4}\right)^2$$
$$= \left(\frac{3}{4}\right)^3 = \frac{3^3}{4^3} = \frac{27}{64}$$

Notice that :  $\left(-\frac{1}{3}\right)^3 = -\left(\frac{1}{3}\right)^3$ 

because the index is an odd number.

Notice that :  $\left(-\frac{3}{4}\right)^2 = \left(\frac{3}{4}\right)^2$ because the index is an even number.

#### The Second law

From the definition of repeated multiplication , we know that :

$$\left(\frac{1}{3}\right)^{7} \div \left(\frac{1}{3}\right)^{4} = \frac{\frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3}}{\frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3}}$$
$$= \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} = \left(\frac{1}{3}\right)^{3}$$

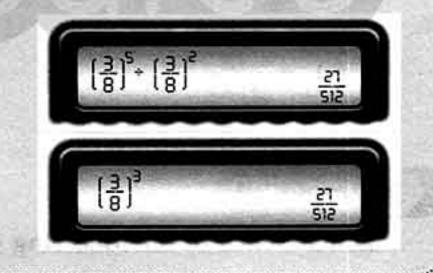
Notice that: 7 - 4 = 3i.e. When dividing like bases , we subtract their powers (indices)

If  $\frac{a}{b}$  is a rational number, where  $\frac{a}{b} \neq 0$ , n and m are non-negative numbers  $n \ge m$ , then  $\left(\frac{a}{b}\right)^n \div \left(\frac{a}{b}\right)^m = \left(\frac{a}{b}\right)^{n-m}$ 

You can check the truth of the previous law by using the calculator as follows:

$$\bullet \left(\frac{3}{8}\right)^5 \div \left(\frac{3}{8}\right)^2 = \frac{27}{512}$$

$$\bullet \left(\frac{3}{8}\right)^3 = \frac{27}{512}$$



# Example 2

Calculate each of the following, then put the result in the simplest form:

$$2^{\frac{2^5 \times 2^4}{2^6}}$$

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Lesson Two

#### Solution

$$2 \frac{2^5 \times 2^4}{2^6} = \frac{2^{5+4}}{2^6} = \frac{2^9}{2^6} = 2^{9-6} = 2^3 = 8$$

#### Try by yourself

Find each of the following in the simplest form:

$$\square \left(\frac{1}{5}\right)^2 \times \left(\frac{1}{5}\right)^2 = \dots$$

$$(\frac{3}{7})^8 \div (\frac{3}{7})^6 = \dots$$

$$3 \left(-\frac{2}{3}\right)^5 \times \left(-\frac{2}{3}\right)^2 \div \left(-\frac{2}{3}\right)^6 = \dots$$

$$4 \left(-\frac{1}{4}\right)^7 \div \left(\frac{1}{4}\right)^6 \times \frac{1}{4} = \dots$$

#### Remarks

• From the repeated multiplication, notice that:

$$(\frac{3}{4} \times \frac{5}{7})^3 = (\frac{3}{4} \times \frac{5}{7}) \times (\frac{3}{4} \times \frac{5}{7}) \times (\frac{3}{4} \times \frac{5}{7})$$

$$= (\frac{3}{4} \times \frac{3}{4} \times \frac{3}{4}) \times (\frac{5}{7} \times \frac{5}{7} \times \frac{5}{7}) = (\frac{3}{4})^3 \times (\frac{5}{7})^3$$

i.e. If  $\frac{a}{b}$  and  $\frac{c}{d}$  are two rational numbers , n is a non-negative integer , then :

$$\left(\frac{a}{b} \times \frac{c}{d}\right)^n = \left(\frac{a}{b}\right)^n \times \left(\frac{c}{d}\right)^n$$

From the repeated multiplication, notice that :

$$\left(\frac{2}{3} \div \frac{5}{11}\right)^4 = \left(\frac{\frac{2}{3}}{\frac{5}{11}}\right)^4 = \frac{\frac{2}{3}}{\frac{5}{11}} \times \frac{\frac{2}{3}}{\frac{5}{11}} \times \frac{\frac{2}{3}}{\frac{5}{11}} \times \frac{\frac{2}{3}}{\frac{5}{11}} \times \frac{\frac{2}{3}}{\frac{5}{11}}$$
$$= \frac{\frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3}}{\frac{5}{11} \times \frac{5}{11} \times \frac{5}{11} \times \frac{5}{11}} = \left(\frac{2}{3}\right)^4 \div \left(\frac{5}{11}\right)^4$$

i.e. If  $\frac{a}{b}$  and  $\frac{c}{d}$  are two rational numbers,  $\frac{c}{d} \neq 0$ , n is a non-negative integer, then:

$$\left(\frac{a}{b} \div \frac{c}{d}\right)^n = \left(\frac{a}{b}\right)^n \div \left(\frac{c}{d}\right)^n \quad \text{(where } \frac{c}{d} \neq 0\text{)}$$

## Example 3

Find the result of each of the following in its simplest form:

$$\left(\frac{xy}{z}\right)^2$$

$$2\left(\frac{2x}{3y}\right)^4$$

#### Solution

$$2 \left(\frac{2 x}{3 y}\right)^4 = \frac{2^4 x^4}{3^4 y^4} = \frac{16 x^4}{81 y^4}$$

#### The Third law

From the definition of repeated multiplication , we know that :

$$\left[ \left( \frac{1}{3} \right)^3 \right]^2 = \left( \frac{1}{3} \right)^3 \times \left( \frac{1}{3} \right)^3 = \left( \frac{1}{3} \right)^{3+3} = \left( \frac{1}{3} \right)^6$$

i.e. If 
$$\frac{a}{b}$$
 is a rational number, n and m are non-negative integers, then 
$$\left[\left(\frac{a}{b}\right)^n\right]^m = \left(\frac{a}{b}\right)^{n \times m}$$

#### For example:

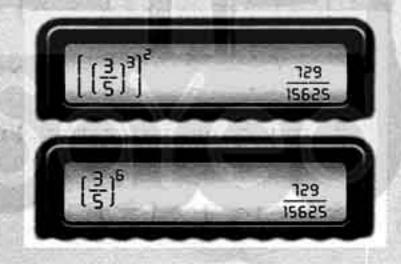
$$\bullet \left[ \left( \frac{3}{5} \right)^3 \right]^2 = \left( \frac{3}{5} \right)^{3 \times 2} = \left( \frac{3}{5} \right)^6$$

$$\bullet \left[ \left( \frac{3}{5} \right)^3 \right]^2 = \left( \frac{3}{5} \right)^{3 \times 2} = \left( \frac{3}{5} \right)^6 \qquad \bullet \left[ \left( -\frac{1}{2} \right)^4 \right]^2 = \left( -\frac{1}{2} \right)^{4 \times 2} = \left( -\frac{1}{2} \right)^8$$

You can check the truth of the previous law by using the calculator as follows : •

$$\bullet \left[ \left( \frac{3}{5} \right)^3 \right]^2 = \frac{729}{15625}$$

$$\bullet \left(\frac{3}{5}\right)^6 = \frac{729}{15625}$$



## Example 4

Calculate each of the following , then put the result in the simplest form :

$$\left[ \left( -2\frac{1}{2} \right)^2 \right]^2$$

$$2\left(\frac{x^2}{y^3}\right)^3$$

## Solution

$$2\left(\frac{x^2}{y^3}\right)^3 = \frac{(x^2)^3}{(y^3)^3} = \frac{x^{2\times 3}}{y^{3\times 3}} = \frac{x^6}{y^9}$$

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Lesson Two

$$3 \frac{(-4 \times^3 y^4)^2}{(-2 \times y^2)^4} = \frac{(-4)^2 \times x^3 \times 2 \times y^4 \times 2}{(-2)^4 \times x^4 \times y^2 \times 4} = \frac{16 \times^6 y^8}{16 \times^4 y^8} = x^{6-4} = x^2$$

## Example 5

If  $x = \frac{1}{2}$ ,  $y = -\frac{3}{4}$  and  $z = \frac{3}{2}$ , find the numerical value of each of the following

in the simplest form :  $\left(\frac{\chi^2}{2}\right)^3$ 

 $2\left(\frac{x^2z}{v}\right)^2$ 

#### Solution

$$\mathbf{1} \left(\frac{x^2}{z}\right)^3 = \left[\left(\frac{1}{2}\right)^2 \div \frac{3}{2}\right]^3 = \left(\frac{1^2}{2^2} \times \frac{2}{3}\right)^3 \\
= \left(\frac{1}{4} \times \frac{2}{3}\right)^3 = \left(\frac{1}{6}\right)^3 = \frac{1^3}{6^3} = \frac{1}{216}$$
Notice that:
$$\frac{x^2}{z} = x^2 \div z$$

$$2\left(\frac{x^2z}{y}\right)^2 = \frac{x^{2\times2}z^2}{y^2} = \frac{x^4z^2}{y^2} = \frac{\left(\frac{1}{2}\right)^4\times\left(\frac{3}{2}\right)^2}{\left(-\frac{3}{4}\right)^2} = \frac{1^4}{2^4}\times\frac{3^2}{2^2}\times\frac{4^2}{3^2} = \frac{1}{16}\times\frac{16}{4} = \frac{1}{4}$$

#### Try by yourself

Calculate each of the following, then put the result in the simplest form:

$\left[\left(\frac{1}{2}\right)^2\right]^3$	$2\left(\frac{a^2b^2}{a^2}\right)^2$	$(\frac{5^2 \times 5^4}{5^2})^2$
	$c^3 d^4$	55 /



# Negative integer powers

Notic the table , then try to discover the pattern to complete it :

The power form	25	24	23	2 <sup>2</sup>	21	20	2-1	2-2
The value	32	16	8	4	2	1,	A	

From the previous pattern, we can deduce that:

$$2^{-1} = 1 \div 2 = \frac{1}{2}$$
,  $2^{-2} = \frac{1}{2} \div 2 = \frac{1}{4} = \frac{1}{2^2}$ 



#### Definition:

If a is a rational number,  $a \neq 0$  and n is a positive integer, then  $a^{-n} = \frac{1}{a^n}$ and  $a^n = \frac{1}{a^{-n}}$ 

For example: • 
$$3^{-3} = \frac{1}{3^3} = \frac{1}{27}$$

$$\bullet \frac{2}{5^{-2}} = 2 \times 5^2 = 2 \times 25 = 50$$

$$\bullet 0.1 = \frac{1}{10} = 10^{-1}$$

• 
$$0.1 = \frac{1}{10} = 10^{-1}$$
 ,  $0.01 = \frac{1}{100} = \frac{1}{10^2} = 10^{-2}$  , ... and so on.

## Remark

If a is a rational number,  $a \neq 0$  and n is a positive integer, then:

 $a^n \times a^{-n} = a^n \times \frac{1}{a^n} = 1$  (the multiplicative neutral)

i.e. each of an and an is the multiplicative inverse of the other.

2 If  $\frac{a}{b}$  is a rational number not equal to zero and n is a positive integer, then:

$$\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^{n}$$

For example: 
$$(\frac{2}{3})^{-2} = (\frac{3}{2})^2 = \frac{9}{4}$$

Find the value of each of the following in the simplest form:

$$1 3 \times 5^{-1}$$

$$2\frac{3}{7^{-1}}$$

$$(\frac{7^2}{7^{-2}})^0$$

## Solution

$$2 \frac{3}{7^{-1}} = 3 \div 7^{-1} = 3 \div \frac{1}{7} = 3 \times 7 = 21$$

$$3 \left( \frac{7^2}{7^{-2}} \right)^0 = 1$$

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Lesson Three

## Find each of the following in the simplest form :

$$1 2^4 \times 2^{-2}$$

$$2\frac{5^{-2}}{5^{-3}}$$

$$(3^2)^{-2}$$

$$\frac{6^{-3} \times 6^5}{6^2}$$

$$(7^3)^2 \times (7^{-2})^2$$

$$7 \left(\frac{3}{5}\right)^{-3} \div \left(\frac{4}{5}\right)^{-3}$$

#### Solution

$$112^4 \times 2^{-2} = 2^4 \times \frac{1}{2^2} = \frac{2^4}{2^2} = 2^{4-2} = 2^2 = 4$$

$$2\frac{5^{-2}}{5^{-3}} = \frac{5^3}{5^2} = 5^{3-2} = 5$$

$$(3^2)^{-2} = \frac{1}{(3^2)^2} = \frac{1}{3^4} = \frac{1}{81}$$

$$4 \frac{6^{-3} \times 6^{5}}{6^{2}} = \frac{6^{5}}{6^{3} \times 6^{2}} = \frac{6^{5}}{6^{5}} = 1$$

$$(7^3)^2 \times (7^{-2})^2 = (7^3)^2 \times \left(\frac{1}{7^2}\right)^2 = 7^6 \times \frac{1}{7^4} = 7^{6-4} = 7^2 = 49$$

$$\mathbf{7} \left(\frac{3}{5}\right)^{-3} \div \left(\frac{4}{5}\right)^{-3} = \left(\frac{5}{3}\right)^3 \div \left(\frac{5}{4}\right)^3 = \left(\frac{5}{3} \div \frac{5}{4}\right)^3 = \left(\frac{5}{3} \times \frac{4}{5}\right)^3 = \left(\frac{4}{3}\right)^3 = \frac{4^3}{3^3} = \frac{64}{27}$$

#### Remark

All laws of powers that we have studied in the previous lesson are correct in the case of the negative powers. So, the previous example can be solved by using laws of powers as follows:

$$1 2^4 \times 2^{-2} = 2^{4 + (-2)} = 2^2 = 4$$

$$2 \frac{5^{-2}}{5^{-3}} = 5^{-2 - (-3)} = 5^{-2 + 3} = 5$$

$$3(3^2)^{-2} = 3^{2 \times (-2)} = 3^{-4} = \frac{1}{3^4} = \frac{1}{81}$$

$$4\frac{6^{-3} \times 6^5}{6^2} = 6^{-3 + 5 - 2} = 6^0 = 1$$

$$\boxed{4} \frac{6^{-3} \times 6^5}{6^2} = 6^{-3+5-2} = 6^0 = 1$$

$$\mathbf{5} \left(\frac{5^3 \times 5^{-2}}{5^{-1} \times 5^4}\right)^{-2} = \left(5^{3 + (-2) - (-1) - 4}\right)^{-2} = \left(5^{3 - 2 + 1 - 4}\right)^{-2}$$
$$= \left(5^{-2}\right)^{-2} = 5^{(-2) \times (-2)} = 5^4 = 625$$

$$7 \left(\frac{3}{5}\right)^{-3} \div \left(\frac{4}{5}\right)^{-3} = \left(\frac{3}{5} \div \frac{4}{5}\right)^{-3} = \left(\frac{3}{5} \times \frac{5}{4}\right)^{-3} = \left(\frac{3}{4}\right)^{-3} = \left(\frac{4}{3}\right)^{3} = \frac{4^{3}}{3^{3}} = \frac{64}{27}$$

### Try by yourself

Find the value of each of the following in the simplest form:

$$11 5^{-3} = \cdots$$

$$(\frac{3}{7})^{-2} = \dots$$

$$(2^{-3})^2 = \cdots$$

$$\left( \frac{2^{-2} \times 2^6}{2^3} \right)^{-3} = \dots$$

**Example** 3 Simplify each of the following to the simplest form where  $x \neq 0$ :

1 
$$x^5 \times x^{-2} \times x^{-3}$$

$$(x^2)^{-3} \div (x^{-1})^2$$

$$3 \left( \frac{x^4 \times x^{-3}}{x^{-4} \times x} \right)^{-2}$$

Solution

2 
$$(x^2)^{-3} \div (x^{-1})^2 = x^{-6} \div x^{-2} = x^{-6-(-2)} = x^{-6+2} = x^{-4} = \frac{1}{x^4}$$

$$\left( \frac{x^4 \times x^{-3}}{x^{-4} \times x} \right)^{-2} = (x^{4+(-3)-(-4)-1})^{-2} = (x^{4-3+4-1})^{-2}$$

$$= (x^4)^{-2} = x^{-8} = \frac{1}{x^8}$$

#### Try by yourself

Simplify each of the following to the simplest form putting the result in positive integer power where the denominator doesn't equal zero:

$$11 (x^{-2})^{-5} = \dots$$

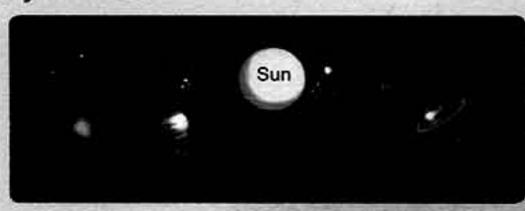
3 
$$(y^5 \times y^{-2})^3 = \dots$$

Lesson Four

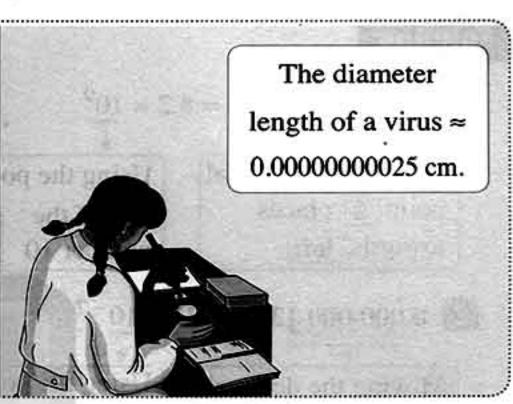


## Scientific notation of the rational number

Do you know?



Neptune planet is far from the sun by 2 800 000 000 miles. (the mile = 1.6 km. approximately).



- The scientific notation of the number is one easy method to deal with the very great numbers or the very small numbers like the numbers mentioned in the previous figures , given that most calculators can show these numbers in the scientific notation.
- Before explaining how to write the numbers in their scientific notation, we should notice the following:
  - 1  $10 = 10^1$ ,  $100 = 10 \times 10 = 10^2$ ,  $1000 = 10 \times 10 \times 10 = 10^3$  and so on Hence we find that:  $2000 = 2 \times 1000 = 2 \times 10^3$ ,  $50\,000 = 5 \times 10\,000 = 5 \times 10^4$
  - 2  $0.1 = \frac{1}{10} = 10^{-1}$ ,  $0.01 = \frac{1}{100} = \frac{1}{10 \times 10} = 10^{-2}$ ,  $0.001 = \frac{1}{1.000} = \frac{1}{10 \times 10 \times 10} = 10^{-3}$  and so on Hence we find that:

$$0.03 = \frac{3}{100} = \frac{3}{10 \times 10} = 3 \times 10^{-2},$$
  
$$0.0007 = \frac{7}{10000} = \frac{7}{10 \times 10 \times 10 \times 10} = 7 \times 10^{-4}$$

## The standard scientific notation of a number:

The number is written in the standard form as:

$$a \times 10^n$$
 where  $1 \le |a| < 10$  and  $n \in \mathbb{Z}$ 

#### For example:

Each of the following two numbers is written in its standard form:

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# **Example** 1 Put each of the following two numbers in the standard form:

8 200 000 000

0.000000135

#### Solution

$$1 \quad 8 \quad 200 \quad 000 \quad 00$$

Moving the decimal point 9 places towards left

Using the power 9 of the number 10

$$2 0.000.000 135 = 1.35 \times 10^{-7}$$

Moving the decimal point 7 places towards right

Using the power -7 of the number 10

## Try by yourself

Write each of the following two numbers in the standard form:

- 650 000 000 = .....
- 2 0.00000102 = .....

## Remarks

• Notice that the number  $32.4 \times 10^5$  is not in the standard form because  $32.4 > 10^5$ and to write it in the standard form, we move the decimal point one place towards left and multiply by 10

*i.e.* 
$$32.4 \times 10^5 = 3.24 \times 10^5 \times 10 = 3.24 \times 10^6$$
 (the standard form)

• Notice that the number  $0.032 \times 10^{-4}$  is not in the standard form because 0.032 < 1and to write it in the standard form, we move the decimal point two places towards right and multiply by  $10^{-2}$ 

*i.e.* 
$$0.032 \times 10^{-4} = 3.2 \times 10^{-4} \times 10^{-2} = 3.2 \times 10^{-6}$$
 (the standard form)

Notice that the standard form of the number 1 is  $1 \times 10^0$ , also the number 2 is  $2 \times 10^{0}$ , and so on ...

# Write each of the following numbers in the standard form:

 $1.45 \times 10^8$ 

 $2706.4 \times 10^5$ 

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Lesson Four

$$30.248 \times 10^{-7}$$

$$4 - 0.0015 \times 10^{-9}$$

#### Solution

$$11.45 \times 10^8 = 4.5 \times 10 \times 10^8 = 4.5 \times 10^9$$

2 
$$706.4 \times 10^5 = 7.064 \times 10^2 \times 10^5 = 7.064 \times 10^7$$

$$30.248 \times 10^{-7} = 2.48 \times 10^{-1} \times 10^{-7} = 2.48 \times 10^{-8}$$

$$4 - 0.001_45 \times 10^{-9} = -1.5 \times 10^{-3} \times 10^{-9} = -1.5 \times 10^{-12}$$

## Try by yourself

In the following, determine the numbers that are not in the standard form, then write them in the standard form:

$$1.5 \times 10^{-4}$$

$$217 \times 10^{8}$$

$$30.5 \times 10^{-7}$$

4 530.5 
$$\times$$
 10 9

$$5 - 0.999 \times 10^{-5}$$

......

$$6 6 \times 10^{6}$$

Example (3) (connecting with georaphy)

The following table shows the areas of the world Oceans. Arrange these areas descendingly.



The Ocean	Indian	Arctic	Pacific	Antarctic	Atlantic
The area (in k.m².)	$7.35 \times 10^{7}$	$1.4 \times 10^7$	$1.66 \times 10^{8}$	$7.6 \times 10^{6}$	$8.65 \times 10^{7}$

#### Solution

Pacific:  $1.66 \times 10^8$ 

Indian:  $7.35 \times 10^7$ 

Arctic:  $1.4 \times 10^7$ Atlantic:  $8.65 \times 10^7$ 

Antarctic:  $7.6 \times 10^6$ 

·· 8.65 > 7.35 > 1.4

$$\therefore 8.65 \times 10^7 > 7.35 \times 10^7 > 1.4 \times 10^7$$

.. Atlantic > Indian > Arctic

.. The descendingly arrangement : pacific > Atlantic > Indian > Arctic > Antarctic

# Example 4

Write the result of each of the following in the standard form:

$$1 (1.2 \times 10^5) \times (4 \times 10^3)$$

$$2 (6.5 \times 10^4) \times (8 \times 10^2)$$

$$3 (2.4 \times 10^{11}) \div (1.2 \times 10^{-4})$$

$$4 (6.6 \times 10^7) \times (3 \times 10)^4$$

$$(2.3 \times 10^6) + (3.7 \times 10^5)$$

## Solution

$$11 (1.2 \times 10^{5}) \times (4 \times 10^{3}) = (1.2 \times 4) \times (10^{5} \times 10^{3}) = 4.8 \times 10^{8}$$

$$(6.5 \times 10^{4}) \times (8 \times 10^{2}) = (6.5 \times 8) \times (10^{4} \times 10^{2})$$

$$= 52 \times 10^{6}$$

Notice that:

 $=5.2 \times 10^7$ 

 $52 \times 10^6$  is not in the standard form, then we should put it in the standard form.

3 
$$(2.4 \times 10^{11}) \div (1.2 \times 10^{-4}) = \frac{2.4}{1.2} \times \frac{10^{11}}{10^{-4}} = 2 \times 10^{15}$$

$$(6.6 \times 10^{7}) \times (3 \times 10)^{4} = (6.6 \times 10^{7}) \times (3^{4} \times 10^{4}) = (6.6 \times 3^{4}) \times (10^{7} \times 10^{4})$$

$$= 534.6 \times 10^{11} = 5.346 \times 10^{13}$$

$$(2.3 \times 10^6) + (3.7 \times 10^5) = 10^5 (2.3 \times 10 + 3.7) = 10^5 (23 + 3.7)$$

$$= 10^{5} \times 26.7 = 2.67 \times 10^{6}$$

# Example

Write the result of each of the following in the standard form:

$$2140000 \times 0.005$$

$$30.000015 \div 30$$

$$4 (50\ 000)^3$$

$$5(0.0003)^5$$

$$(-0.001)^6$$

## Solution

$$11 30 000 \times 400 000 = (3 \times 10^{4}) \times (4 \times 10^{5}) = (3 \times 4) \times (10^{4} \times 10^{5})$$

$$= 12 \times 10^9 = 1.2 \times 10^{10}$$

2 
$$140\ 000 \times 0.005 = (1.4 \times 10^{5}) \times (5 \times 10^{-3}) = (1.4 \times 5) \times (10^{5} \times 10^{-3}) = 7 \times 10^{2}$$

3 
$$0.000015 \div 30 = (1.5 \times 10^{-5}) \div 3 \times 10 = \frac{1.5}{3} \times \frac{10^{-5}}{10} = 0.5 \times 10^{-6} = 5 \times 10^{-7}$$

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Lesson Four

$$(50\ 000)^3 = (5 \times 10^4)^3 = 5^3 \times 10^{12} = 125 \times 10^{12} = 1.25 \times 10^{14}$$

$$(0.0003)^5 = (3 \times 10^{-4})^5 = 3^5 \times 10^{-20} = 243 \times 10^{-20} = 2.43 \times 10^{-18}$$

$$6 (-0.001)^6 = (0.001)^6 = (1 \times 10^{-3})^6 = 1^6 \times 10^{-18} = 10^{-18}$$

#### Try by yourself

Write the result of each of the following in the standard form:

- $1 (5.3 \times 10^{7}) \times (3 \times 10^{5})$
- $20.0006 \div 20$

- $(400\ 000)^2$
- $4(3.2 \times 10^9) (0.2 \times 10^8)$

..........

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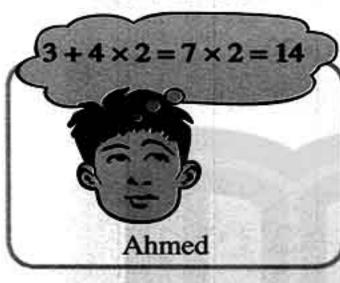


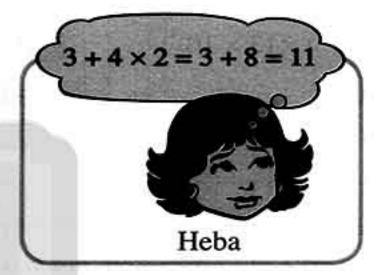
# Order of mathematical operations

The following problem was given to each of Ahmed and Heba.

Calculate:  $3 + 4 \times 2$ 

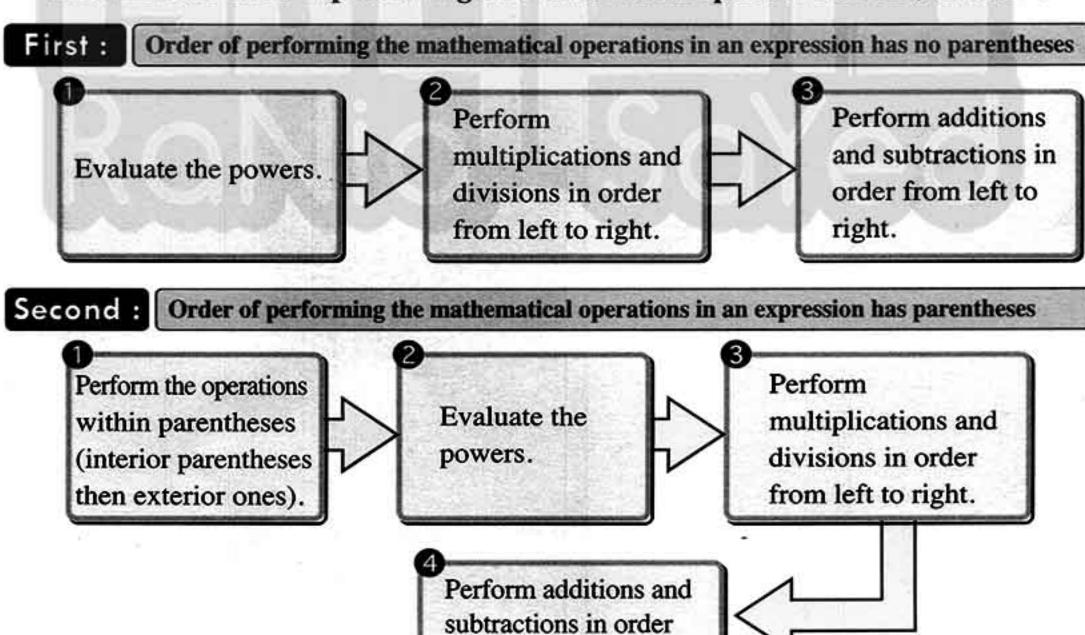
Their answers were as follows:





It is clear that each of them followed a different way to solve this problem and that led to the difference in the two answers:

- Ahmed performed the addition operation first, then he performed the multiplication operation.
- Heba multiplied first, then she added the two numbers. In order to avoid this difference in these problems , it is agreed about some rules that determine the order of performing the mathematical operations for us , that are :



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from left to right.

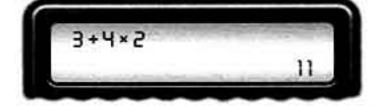
Lesson Five

 According to these rules, we can determine that Heba held the correct answer because she performed the multiplication operation first, then the addition operation.

#### Remark

The scientific calculators and computers follow the same rules of ordering the operations.

For example, we can use the calculator in the previous problem by clicking the following buttons successively from the left and note the result.



$$3+4\times 2=$$

## Example (1)

Calculate the value of each of the following:

$$13+6\times(5+4)\div3-7$$

$$29-5 \div (8-3) \times 2+6$$

#### Solution

$$=3+54 \div 3-7$$

$$=3+18-7$$

$$=21-7$$

$$= 14$$

(parentheses)

(multiplication)

(division)

(addition)

(subtraction)

$$29-5 \div (8-3) \times 2 + 6 = 9-5 \div 5 \times 2 + 6$$

$$=9-1\times2+6$$

$$=9-2+6$$

$$= 7 + 6$$

=7

$$= 7 + 6$$

= 13

(multiplication)

(subtraction)

(addition)

## Example 2

Calculate the value of each of the following:

$$1 \cdot 4 - 3 \cdot [4 - 2 \cdot (6 - 3)] \div 2$$

$$216 \div [8-3(4-2)] + 1$$

(addition)

## Solution

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2 
$$16 \div \begin{bmatrix} 8-3 (4-2) \end{bmatrix} + 1 = 16 \div \begin{bmatrix} 8-3 \times 2 \end{bmatrix} + 1$$
 (the interior parentheses)  

$$= 16 \div \begin{bmatrix} 8-6 \end{bmatrix} + 1$$
 (multiplication inside parentheses)  

$$= 16 \div 2 + 1$$
 (subtraction inside the parentheses)  

$$= 8+1$$
 (division)  

$$= 9$$
 (addition)

# Example (3

Calculate the value of each of the following:

$$18 \times 2^2 - 7 \times (4+1)$$

$$22 + 3[5 + (4-1)^2]$$

$$[3] 3[(3^2+1)-(2^3-2)]$$

#### Solution

1 
$$8 \times 2^2 - 7 \times (4 + 1) = 8 \times 2^2 - 7 \times 5$$
 (addition inside parentheses)  
=  $8 \times 4 - 7 \times 5$  (powers)  
=  $32 - 35$  (multiplication)  
=  $-3$  (subtraction)

$$2 + 3 [5 + (4 - 1)^{2}] = 2 + 3 [5 + 3^{2}]$$
 (subtraction inside interior parentheses)  

$$= 2 + 3 [5 + 9]$$
 (powers inside parentheses)  

$$= 2 + 3 \times 14$$
 (addition inside parentheses)  

$$= 2 + 42$$
 (multiplication)  

$$= 44$$
 (addition)

$$3 [(3^{2}+1)-(2^{3}-2)] = 3 [(9+1)-(8-2)]$$
 (powers)
$$= 3 [10-6]$$
 (the interior parentheses)
$$= 3 \times 4$$
 (subtraction inside parentheses)
$$= 12$$
 (multiplication)

#### Remark

In the problems containing fractions, we should perform the operations in the numerator and denominator before division.

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Lesson Five

# Example 4

Calculate the value of each of the following:

$$1 \frac{36-6}{3+12}$$

$$2 \frac{11 - (5 - 4)}{5^2 - 10 \times 2}$$

$$37 + 8 \div \frac{4 + 12 - 2}{3^2 - 2} - (2^3 + 2)$$

#### Solution

$$2 \frac{11 - (5 - 4)}{5^2 - 10 \times 2} = \frac{11 - 1}{25 - 20} = \frac{10}{5} = 2$$

3 
$$7 + 8 \div \frac{4 + 12 - 2}{3^2 - 2} - (2^3 + 2) = 7 + 8 \div \frac{14}{7} - (2^3 + 2)$$
  
=  $7 + 8 \div 2 - 10 = 7 + 4 - 10 = 1$ 

#### Try by yourself

22+2-9

Calculate the value of each of the following:

$$1 20 \div (12-2) \times 3^2 - 2$$

$$2 \frac{6 \times 3 + 10 \div 5}{2 - (10 - 2^2)}$$

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## Lesson (6) The square root of a perfect square rational number

• We know that :  $3^2 = 3 \times 3 = 9$  and it is read as the square of the number 3 is 9 And the square root is the inverse operation of finding the square of the number.

For example: To find the square root of the number 36, we search for a number whose square is 36

- We find that this number is : 6 (because :  $6^2 = 36$ ) or -6 [because :  $(-6)^2 = 36$ ] *i.e.* The number 36 has two square roots which are  $\pm 6$ 
  - 6 is the positive square root of 36 and it is written as :  $\sqrt{36} = 6$
  - - 6 is the negative square root of 36 and it is written as:  $-\sqrt{36} = -6$

From the previous , we can deduce the following definition :



#### Definition:

The square root of the perfect square rational number "a" is the number whose square equals "a".

#### Generally:

\* The positive square root of the number a is symbolized by √a

Notice that:

VZero = Zero

- For example: The positive square root of 25 is  $\sqrt{25} = 5$
- \* The negative square root of the number a is symbolized by -√a

For example: The negative square root of 16 is  $-\sqrt{16} = -4$ 

\* The two square roots of the number a is symbolized by  $\pm \sqrt{a}$ , and each of them is the additive inverse of the other.

For example: The two square roots of 49 are  $\pm \sqrt{49} = \pm 7$ 

#### Remarks

I It is meaningless to find √a if a is a negative rational number because there is no rational number if it is multiplied by itself, the result will be negative.

$$2\sqrt{\left(\frac{a}{b}\right)^2} = \left|\frac{a}{b}\right|$$

For example:  $\sqrt{(-3)^2} = |-3| = 3$   $\sqrt{(-\frac{4}{5})^2} = |-\frac{4}{5}| = \frac{4}{5}$ 

- 3  $\sqrt{a^2 b^2} = \sqrt{(ab)^2} = |ab|$  For example:  $\sqrt{a^4 b^6} = \sqrt{(a^2 b^3)^2} = |a^2 b^3|$
- If:  $x^2 = a$  "where a is a perfect square rational number", then:  $x = \pm \sqrt{a}$

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Lesson Six

# Example 1

Find each of the following in the simplest form:

$$2 - \sqrt{\frac{16}{25}}$$

$$3 \pm \sqrt{2\frac{1}{4}}$$

$$4\sqrt{(-\frac{2}{7})^2}$$

$$5 - \sqrt{0.25}$$

$$6 \pm \sqrt{\frac{3.6}{10}}$$

$$7\sqrt{16+9}$$

$$8\sqrt{100-36}$$

$$9 \sqrt{\frac{36 \text{ a}^8}{49 \text{ d}^4}}$$

## Solution

$$\boxed{1} \sqrt{36} = 6$$

because 
$$6^2 = 36$$

$$2 - \sqrt{\frac{16}{25}} = -\frac{4}{5}$$

because 
$$\left(\frac{4}{5}\right)^2 = \frac{16}{25}$$

$$3 \pm \sqrt{2\frac{1}{4}} = \pm \sqrt{\frac{9}{4}} = \pm \frac{3}{2}$$

$$4 \sqrt{\left(-\frac{2}{7}\right)^2} = \left|-\frac{2}{7}\right| = \frac{2}{7}$$

$$5 - \sqrt{0.25} = -\sqrt{\frac{25}{100}} = -\frac{5}{10} = -\frac{1}{2}$$

6 
$$\pm \sqrt{\frac{3.6}{10}} = \pm \sqrt{\frac{36}{100}} = \pm \frac{6}{10} = \pm \frac{3}{5}$$

$$7\sqrt{16+9} = \sqrt{25} = 5$$

## Notice that : |

 $8\sqrt{100-36} = \sqrt{64} = 8$ 

When there is an addition or a subtraction operation under the square root, it must be performed first before finding the square root.

 $\sqrt{\frac{36 a^8}{49 d^4}} = \frac{6 a^4}{7 d^2}$ 

#### Try by yourself

1 
$$\sqrt{64} = \cdots$$

$$2 - \sqrt{900} = \cdots$$

$$3 - \sqrt{\frac{36}{25}} = \cdots$$

$$4 \pm \sqrt{6\frac{1}{4}} = \cdots$$

$$\sqrt{100-64} = \cdots$$

#### Remarks

If the operation of finding the square root of a number directly is difficult, then we factorize this number into its prime factors, then we take one factor from each two equal factors, then the product of these taken factors is the square root of this number.

Example (2)

Find : √441

Solution

$$\therefore 441 = 3 \times 3 \times 7 \times 7$$

$$\therefore \sqrt{441} = 3 \times 7$$

$$= 21$$

$$\mathfrak{J}(3) \begin{vmatrix} 441 \\ 3 \\ 147 \end{vmatrix}$$
 $\mathfrak{D}(7) \begin{vmatrix} 49 \\ 7 \\ 1 \end{vmatrix}$ 

# Example (3

Simplify each of the following to the simplest form:

$$\square - \frac{2}{7} \times \sqrt{\frac{49}{4}} \times \left(\frac{2}{7}\right)^2$$

$$1 - \frac{2}{7} \times \sqrt{\frac{49}{4}} \times \left(\frac{2}{7}\right)^2 \qquad 2 \left(-\frac{3}{2}\right)^2 \times \sqrt{\frac{64}{9}} \times \left(\frac{5}{2}\right)^0 \qquad 3 \left(2\frac{7}{9}\right)^2 \div \sqrt{\frac{25}{9}}$$

$$(2\frac{7}{9})^2 \div \sqrt{\frac{25}{9}}$$

Solution

$$2 \left(-\frac{3}{2}\right)^2 \times \sqrt{\frac{64}{9}} \times \left(\frac{5}{2}\right)^0 = \frac{9}{4} \times \frac{8}{3} \times 1 = 6$$

$$3 \left(2\frac{7}{9}\right)^2 \div \sqrt{\frac{25}{9}} = \left(\frac{25}{9}\right)^2 \div \frac{5}{3} = \left(\left(\frac{5}{3}\right)^2\right)^2 \div \frac{5}{3} = \left(\frac{5}{3}\right)^4 \div \frac{5}{3} = \left(\frac{5}{3}\right)^{4-1} = \left(\frac{5}{3}\right)^3 = \frac{125}{27}$$

## Try by yourself

Simplify each of the following to the simplest form:

$$2 \frac{5}{7} \times \sqrt{\frac{49}{36}} \div \left(-\frac{5}{3}\right)^2 = \dots$$

## Example 4

A square whose area equals the area of the triangle whose base length is 16 cm. and its corresponding height is 8 cm.

Find the side length of the square.

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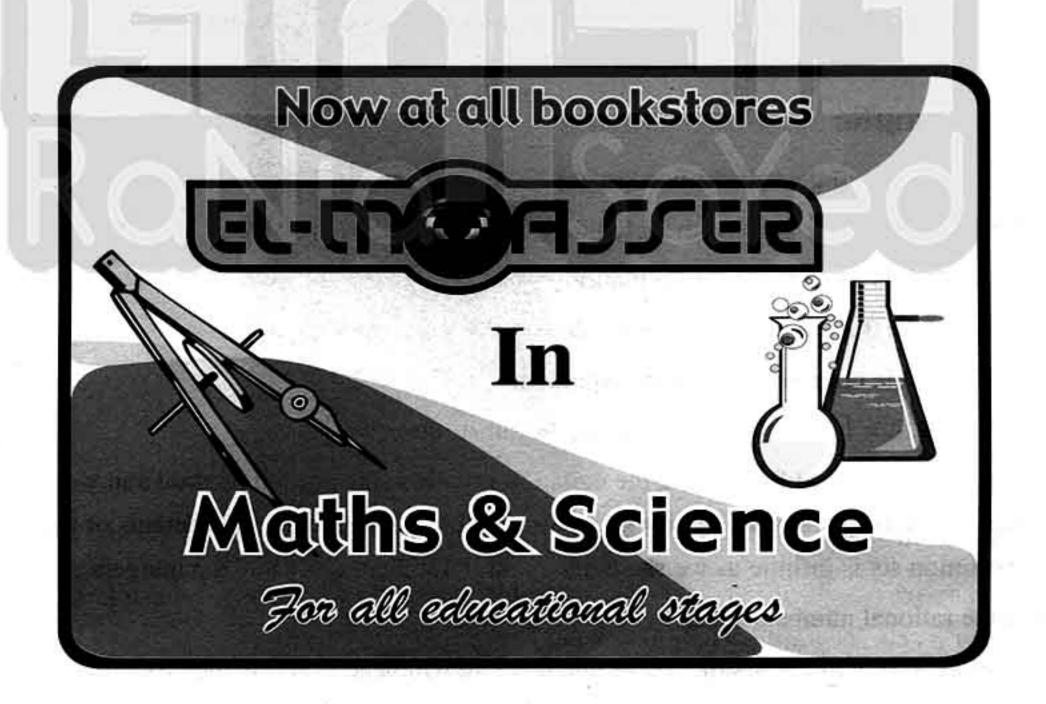
Lesson Six

#### Solution

- : The area of the triangle =  $\frac{1}{2}$  of the base length × its corresponding height.
- $\therefore$  The area of the triangle =  $\frac{1}{2} \times 16 \times 8 = 64$  cm<sup>2</sup>.
- $\therefore$  The area of the square = 64 cm<sup>2</sup>.
- $\therefore$  The side length of the square =  $\sqrt{64}$  = 8 cm.

#### Try by yourself

The area of a square is 1.44 cm<sup>2</sup>. Find its perimeter.



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Unit :



# Solving equations of the first degree in one unknown in **Q**

#### Prelude

The equation is a mathematical statement which contains one variable as X (or more as X and y) and contains equality relation x = x

as: 
$$2 \times 2 = 6 \times 1 + 3 = 5 \times 2 \times 1 + 3 = 3 \text{ and } x^2 = 25$$

The degree of the equation is determined by the heighest degree of the terms forming the equation.

#### For example:

- 5 X + 2 = 7 is an equation of the first degree in one unknown X
- $x^2 + x 3 = 0$  is an equation of the second degree in one unknown x
- 2 X + 3 y = 5 is an equation of the first degree in two unknowns X and y

The substituting set: is the set that contains the probable values of the unknown.

The solution set (the S.S.): is the set whose elements satisfy the equality of the equation and it is a subset of the substitution set.

#### For example:

- If x + 3 = 5 and the substitution set is  $\{2, 3\}$
- Putting x = 2, we get that the left side = 2 + 3 = 5 = the right side.
  - *i.e.* x = 2 is a solution to the equation.
- Putting x = 3, we get that the left side =  $3 + 3 = 6 \neq$  the right side.
  - *i.e.* x = 3 is not a solution to the equation.
  - $\therefore$  The S.S. =  $\{2\}$  and it is a subset of the substitution set  $\{2,3\}$

The previous method for solving the equation is called substitution method and we notice that it is a long way and it may be impossible if the number of elements of the substitution set is infinite as we see in the natural numbers set  $\mathbb{N}$  and the integers set  $\mathbb{Z}$  and the rational numbers set  $\mathbb{Q}$ 

Therefore, we will use another easier method that will need studying the properties of the equality relation to enable us to make the unknown X in one side of the equation alone.

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Lesson Seven

## The properties of the equality relation :

• We can add any rational number to both sides of the equation.

For example: If x-1=5, then x-1+1=5+1

*i.e.* x = 6

• We can subtract any rational number from both sides of the equation.

For example: If x + 3 = 2, then x + 3 - 3 = 2 - 3

i.e. x = -1

We can multiply both sides of the equation by the same rational number.

For example: If  $\frac{1}{5}x = 2$ , then  $\frac{1}{5}x \times 5 = 2 \times 5$ 

*i.e.* x = 10

We can divide both sides of the equation by the same rational number not equal to zero.

For example: If 7x = 14, then  $\frac{7x}{7} = \frac{14}{7}$ 

*i.e.* x = 2

Then by applying any of the previous properties in any equation, then we will get an equivalent equation to the origin equation that has the same solution.

#### Generally:

If a , b and c are three rational numbers , then these numbers have the following properties :

If 
$$a = b$$
, then  $a + c = b + c$ 

2 If 
$$a+c=b+c$$
, then  $a=b$ 

3 If 
$$a = b$$
, then  $a \times c = b \times c$ 

If 
$$a \times c = b \times c$$
,  $c \neq 0$ , then  $a = b$ 

The following examples show how to use the equality properties to solve an equation of the first degree in one unknown.

# Example 1

Find the solution set of the equation x + 5 = 4 if the substitution set is :

 $\mathbf{1}$   $\mathbf{z}$ 

2 N

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#### Solution

If the substitution set is  $\mathbb{Z}$ 

$$\therefore x + 5 = 4$$

Adding – 5 to both sides

(-5 is the additive inverse of 5)

$$\therefore X + 5 + (-5) = 4 + (-5)$$

*i.e.* 
$$x + 0 = -1$$
 *i.e.*  $x = -1$ 

*i.e.* 
$$x = -1$$

#### Another method:

You can imagine that 5 is moved from the left side to the right side and became - 5

$$x+5=4 \Rightarrow x=4-5$$

You can check the truth of your solution by substituting by X = -1 in the origin equation, you will get the left side = -1 + 5 = 4 = the right side.

$$\therefore \text{ The S.S.} = \{-1\}$$

2 If the substitution set is N

$$\therefore x + 5 = 4$$

Subtracting 5 from both sides

Another method :

and it became divisor

You can imagine that 2 is moved

from the left side to the right side

 $2x = 18 \Rightarrow x = \frac{18}{2}$ 

$$x+5-5=4-5$$

$$\therefore x = 4 - 5$$

: The subtraction (4-5) is impossible in  $\mathbb{N}$ 

## Example

Find the solution set of each of the following equations in Q:

$$12x-5=13$$

$$2 \ 2 \ \frac{1}{2} - \frac{3}{2} \ x = 5$$

## Solution

Adding 5 to both sides (it is the additive inverse of (-5))

$$\therefore 2 \times -5 + 5 = 13 + 5$$

*i.e.* 
$$2 x = 18$$

Dividing both sides by 2

$$\therefore x = 9$$

 $\therefore \frac{2 X}{2} = \frac{18}{2}$ 

:. The S.S. = 
$$\{9\}$$

"Check the truth of the solution"

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Lesson Seven

 $2 : 2\frac{1}{2} - \frac{3}{2} x = 5$ 

$$\therefore 2\frac{1}{2} - \frac{3}{2} x - 2\frac{1}{2} = 5 - 2\frac{1}{2}$$

$$\therefore -\frac{3}{2} x = \frac{5}{2}$$

Multiplying both sides by  $\left(-\frac{2}{3}\right)$ 

$$\therefore -\frac{3}{2} \times \times \left(-\frac{2}{3}\right) = \frac{5}{2} \times \left(-\frac{2}{3}\right)$$

$$\therefore \text{ The S.S.} = \left\{-\frac{5}{3}\right\}$$

Subtracting  $2\frac{1}{2}$  from both sides

$$\therefore -\frac{3}{2} x = 2\frac{1}{2}$$

(it is the multiplicative inverse of  $-\frac{3}{2}$ )

$$\therefore x = -\frac{5}{3}$$

"Check the truth of the solution"

## Example 3

Find the S.S. of each of the following equations:

1 
$$2(x+3) = 4$$
, where  $x \in \mathbb{Z}$ 

$$25(x+2)-1=19$$
, where  $x \in \mathbb{Q}$ 

#### Solution

$$11 : 2(x+3) = 4$$

$$\therefore \frac{2(x+3)}{2} = \frac{4}{2}$$

Adding (-3) to both sides

$$\therefore x = -1$$

$$2 : 5(x+2)-1=19$$

Using the distribution property

$$\therefore 5 X + 10 - 1 = 19$$

$$\therefore 5 X + 9 = 19$$

Adding (-9) to both sides

$$\therefore$$
 5  $x = 10$ 

$$\therefore \frac{5 \, x}{5} = \frac{10}{5}$$

$$\therefore$$
 The S.S. =  $\{2\}$ 

Dividing both sides by 2

$$\therefore x + 3 = 2$$

$$x + 3 - 3 = 2 - 3$$

∴ The S.S. = 
$$\{-1\}$$

#### Notice that :

$$5(X+2)-1=19$$
,  $5X+9=19$  and  $5X=10$  are equivalent equations.

$$\therefore 5 \times 49 - 9 = 19 - 9$$

Dividing both sides by 5

$$\therefore x = 2$$

# Example 4

Find in Q the solution set of each of the following equations:

$$1 3 x + 4 = 2 (x + 1)$$

$$2(x+3)-(x-2)=4(x-1)+3$$

#### Solution

Notice that the variable (x) exists in the two sides, then we try to collect it in one side (say the left side)

$$11 : 3 x + 4 = 2 (x + 1)$$

Using the distribution property

$$\therefore 3 X + 4 = 2 X + 2$$

Subtracting 2 X from both sides

$$\therefore 3 \times -2 \times +4 = 2 \times -2 \times +2$$

$$\therefore x + 4 = 2$$

Subtracting 4 from both sides

$$x+4-4=2-4$$

$$\therefore \text{ The S.S.} = \{-2\}$$

2 : 
$$2(x+3)-(x-2)=4(x-1)+3$$

Using the distribution property

$$\therefore 2 \times +6 - \times +2 = 4 \times -4 +3$$

$$x + 8 = 4x - 1$$

Subtracting X from both sides

$$\therefore X - X + 8 = 4X - X - 1$$

Adding 1 to both sides

$$\therefore 8 + 1 = 3 \times -1 + 1$$

$$\therefore 9 = 3 X$$

Dividing both sides by 3

$$\therefore \frac{9}{3} = \frac{3 X}{3}$$

$$\therefore 3 = x$$

$$\therefore \text{ The S.S.} = \{3\}$$

#### Another method:

$$3 x + 4 = 2 x + 2$$

$$(-2 x)$$

$$\therefore 3 X - 2 X = 2 - 4$$

*i.e.* 
$$x = -2$$

$$\therefore x = -2$$

$$\therefore 8 = 3 \times -1$$

#### Another method:

$$x + 8 = 4x - 1$$

$$\therefore 8 + 1 = 4 X - X$$

*i.e.* 
$$9 = 3 \times$$

Lesson Seven

#### Try by yourself

Find the solution set of each of the following equations:

- 1 X-5=2, where  $X \in \mathbb{N}$
- 2 2x + 11 = 3, where  $x \in \mathbb{Z}$
- 3 2x-3=5x+6, where  $x \in \mathbb{Q}$

The solution of the equations can help us in solving some of our life problems and we will show some of these in the following examples:

## Example 5

Two natural numbers , one of them is thrice of the other If the sum of them is 16, find the two numbers.

## Solution

- We give one of the two number the symbol X
- Using the information given, we form a first degree equation in one unknown.
  - : The other number is thrice of the number x
  - $\therefore$  The other number = 3  $\times$
  - .. The sum of the two numbers = 16
  - $\therefore$  The equation is x + 3x = 16
- · We solve the equation we get to find the value of the unknown.
- $\therefore x + 3x = 16$  $\therefore 4 \times 16$ 
  - Dividing by 4  $\therefore x = 4$
- *i.e.* one of the two numbers = 4 the other number =  $3 \times 4 = 12$
- We make sure that the solution is right by using the problem itself, not by using the equation
  - : 12 is the thrice of 4, 12 + 4 = 16
  - .. The solution is right.

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Unit 1

#### Remarks for solving life problems:

- If a number = X, then its twice = 2 X and its three times = 3 X, .........
- If a number = x and another number exceeds it by 5
  - , then the other number = x + 5
- If a number = x and another number decreases than it by 5, then the other number = x-5
- If the age of a man now = x years, then:
  - \* His age after 3 years = (x + 3) years.
  - \* His age 3 years ago = (x 3) years.
- Three consecutive integers are: x, x + 1 and x + 2
- Three consecutive natural (even or odd) numbers are x, x + 2 and x + 4
- The perimeter of a rectangle = 2 (length + width)
- The perimeter of a square = side length  $\times 4$
- The perimeter of the triangle = the sum of its sides lengths
- The area of the triangle =  $\frac{1}{2}$  the base length × the height.
- The sum of measures of the interior angles of the triangle = 180°

Example 6

Three natural consecutive odd numbers whose sum is 27, find these numbers.

#### Solution

Let the smallest odd number = x

- : Each odd number exceeds the odd number just before it by 2
- $\therefore$  The next odd number = x + 2 and the third odd number = x + 4
- $\therefore$  The sum of the numbers = 27
- X + (X + 2) + (X + 4) = 27

 $\therefore 3 \times + 6 = 27$ 

 $\therefore 3 \times = 27 - 6$ 

 $\therefore 3 x = 21$ 

 $\therefore x = \frac{21}{3}$ 

 $\therefore x = 7$ 

i.e. The numbers are 7,9 and 11

To check the solution: the numbers 7, 9 and 11 are natural consecutive odd numbers

$$7+9+11=27$$

.. The solution is true.

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Lesson Seven

# Example 7

A rectangle with length equals twice its width and its perimeter = 18 cm.

Find the dimensions of the rectangle.

#### Solution

Let the width of the rectangle = x cm.

 $\therefore$  Its length = 2  $\times$  cm.

: The perimeter of the rectangle = 2 (length + width)

$$\therefore 18 = 2(2 X + X)$$

$$\therefore 18 = 2 \times 3 X$$

$$\therefore 18 = 6 X$$

$$\therefore x = 3$$

*i.e.* The width of the rectangle = 3 cm. and its length = 6 cm.

To check the solution:

- : The length of the rectangle = 6 cm. equals twice its width 3 cm.
  - The perimeter of the rectangle =  $2(6 + 3) = 2 \times 9 = 18$  cm.
- .. The solution is true.

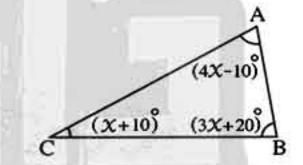
# Example 8

#### In the opposite figure:

ABC is a triangle in which m  $(\angle A) = (4 \times -10)^{\circ}$ 

$$m (\angle B) = (3 X + 20)^{\circ}, m (\angle C) = (X + 10)^{\circ}$$

Find the measures of the angles of the triangle.



## Solution

: The sum of measures of the interior angles of the triangle = 180°

$$\therefore (4 X - 10) + (3 X + 20) + (X + 10) = 180$$

$$\therefore 8 X + 20 = 180$$

Subtracting 20 from both sides

$$\therefore 8 \ x = 180 - 20$$

$$\therefore 8 \ x = 160$$

$$\therefore x = \frac{160}{8}$$

$$\therefore x = 20$$

$$\therefore$$
 m ( $\angle$  A) = (4 × 20) – 10 = 80 – 10 = 70°

$$m (\angle B) = (3 \times 20) + 20 = 60 + 20 = 80^{\circ}$$

$$m (\angle C) = 20 + 10 = 30^{\circ}$$

To check the solution: :  $m (\angle A) + m (\angle B) + m (\angle C) = 70^{\circ} + 80^{\circ} + 30^{\circ} = 180^{\circ}$ 

.. The solution is true.

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The difference between two integers is 4 and their sum is 14 Find the two numbers.

#### Solution

Let the small number = x

: The difference between the two numbers = 4 : The great number =  $x + \dots$ 

......

......

: Their sum is 14 ∴ ······· + ····· = 14

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Lesson Eight



# Solving inequalities in Q

#### Prelude

- We had studied before some concepts as the substitution set and the solution set in equations which they are also the same concepts for inequalities.
- The solution set of the inequality is the set whose elements satisfy the inequality and it is a subset of the substitution set.

#### Illustrated example

Find the solution set of the inequality x + 3 < 5 if the substitution set is  $\{-2, -1, 0, 1, 2, 3\}$ , then represent the S.S. on the number line.

#### Solution

Substitute for the value of X by each element of the substitution set.

• At 
$$x = -2$$

• At 
$$x = -1$$

• At 
$$x = 0$$

• At 
$$x = 1$$

• At 
$$x = 2$$

• At 
$$x = 3$$

$$\therefore$$
 The left side =  $-2 + 3 = 1$ 

$$\therefore$$
 The left side =  $-1 + 3 = 2$ 

$$\therefore$$
 - 1 is a solution to the inequality.

$$\therefore$$
 The left side =  $0 + 3 = 3$ 

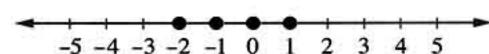
$$\therefore$$
 The left side = 1 + 3 = 4

$$\therefore$$
 The left side = 2 + 3 = 5

$$\therefore$$
 The left side = 3 + 3 = 6

#### From the previous:

$$\therefore \text{ The solution set} = \{-2, -1, 0, 1\}$$



#### Remark

The substitution method which is followed in the previous example is a long method and difficult and it may be impossible if the substitution set is infinite. Therefore we use another easier method for the solution and that requires studying the properties of inequalities.

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#### Properties of inequalities:

We know that 6 > -9 is a true inequality.

But do the following operations lead to true inequalities?

Add 2 to the two sides of the inequality

$$\therefore 6+2>-9+2 \longrightarrow 8>-7$$
 (true inequality)

i.e. We can add a constant number to both sides of the inequality without change in the inequality relation.

2 Subtract 7 from the two sides of the inequality

$$\therefore 6-7>-9-7 \longrightarrow -1>-16$$
 (true inequality)

i.e. We can subtract a constant number from the two sides of the inequality without change in the inequality relation.

Multiply the two sides of the inequality by 5 (positive number)

$$\therefore 6 \times 5 > -9 \times 5 \longrightarrow 30 > -45$$
 (true inequality)

i.e. Multiplying the two sides of the inequality by a positive number does not change the inequality relation.

4 Divide the two sides of the inequality by 3 (positive number)

$$\therefore \frac{6}{3} > -\frac{9}{3} \longrightarrow 2 > -3 \text{ (true inequality)}$$

i.e. Dividing the two sides of the inequality by a positive number does not change the inequality relation.

Multiply the two sides of the inequality by – 1 (negative number)

$$\therefore$$
 6 × (-1) > -9 × (-1)  $\longrightarrow$  -6 > 9 (false inequality) because -6 < 9

i.e. If we multiply the two sides of the inequality by a negative number, then we change the sign of the inequality to the opposite sign.

6 Divide the two sides of the inequality by – 3 (negative number)

$$\therefore \frac{6}{-3} > \frac{-9}{-3} \longrightarrow -2 > 3 \text{ (false inequality) because } -2 < 3$$

i.e. If we divide the two sides of the inequality by a negative number, then we change the inequality sign to the opposite sign.

We can summarize the properties of inequality that noticed before as follows:

Lesson Eight

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Assuming that a , b , c are three rational numbers , then :

- If a < b, then a + c < b + c
- 2 If a < b, then a c < b c
- 3 If a < b , c is a positive number, then ac < bc
- If a < b , c is a positive number, then  $\frac{a}{c} < \frac{b}{c}$
- If a < b , c is a negative number, then ac > bc
- 6 If a < b, c is a negative number, then  $\frac{a}{c} > \frac{b}{c}$

#### Remark

If a and b are two rational numbers not equal to zero and a > b, then :  $\frac{1}{a} < \frac{1}{b}$ 

# Example (1

Find the solution set of the inequality:

$$x+2<5$$
, where :  $II x \in \mathbb{Z}$ 

$$2x \in \mathbb{N}$$

then represent the solution set on the number line in each case.

## Solution

$$x + 2 < 5$$

Subtracting 2 from the two sides

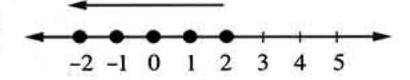
$$x+2-2<5-2$$

i.e. 
$$x < 3$$

1 When 
$$x \in \mathbb{Z}$$

The solution set is all the integers which are less than 3

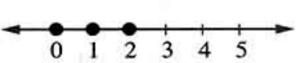
*i.e.* The S.S. = 
$$\{2, 1, 0, -1, ...\}$$



## 2 When $x \in \mathbb{N}$

The solution set is all the natural numbers which are less than 3

*i.e.* The S.S. = 
$$\{2, 1, 0\}$$



#### We notice from the previous example that:

The solution set of the inequality depends on the substitution set, we find that:

The solution set in  $\mathbb{N}$  differs from the solution set in  $\mathbb{Z}$ 

#### Example 2

Find the solution set of the inequality 2x-5>5, where :

$$\mathbf{1} x \in \mathbb{Q}$$

$$2x \in \mathbb{Z}$$

#### Solution

$$\therefore 2X-5>5$$

Adding 5 to both sides

$$\therefore 2x-5+5>5+5$$

$$\therefore 2 \times 10$$

Multiplying both sides by  $\frac{1}{2}$ 

i.e. 
$$x > 5$$

$$\blacksquare$$
 When  $x \in \mathbb{Q}$ 

The S.S. is all the rational numbers which are greater than 5, then we write it by characterized property method because it is difficult to list all its members.

*i.e.* The S.S. = 
$$\{x : x \in \mathbb{Q}, x > 5\}$$

2 When 
$$x \in \mathbb{Z}$$

The solution set is all the integers which are greater than 5

*i.e.* The S.S. = 
$$\{6, 7, 8, \dots\}$$

#### Example 3

Find in Q the solution set of each of the two following inequalities:

$$\prod 4 - 2 X \le 2$$

$$27(x-1) > 9x-6$$

#### Solution

$$\therefore -4 + 4 - 2 \times \leq -4 + 2$$

$$\therefore -2 \times \leq -2$$

Dividing both sides by (-2)

$$\therefore \frac{-2x}{-2} \ge \frac{-2}{-2}$$

*i.e.* The S.S. = 
$$\{x: x \in \mathbb{Q}, x \ge 1\}$$

Lesson Eight

2:7(x-1)>9x-6

$$\therefore 7x-7>9x-6$$

Subtracting (9 X) from both sides

$$\therefore 7x-9x-7>9x-9x-6$$

$$\therefore -2x-7>-6$$

Adding 7 to both sides

$$\therefore -2 \times -7 + 7 > -6 + 7$$

$$\therefore -2 \times > 1$$

Dividing both sides by (-2)

$$\therefore \frac{-2X}{-2} < \frac{1}{-2}$$

$$\therefore x < -\frac{1}{2}$$

Notice that: The change of inequality sign.

*i.e.* The S.S. = 
$$\{x : x \in \mathbb{Q}, x < -\frac{1}{2}\}$$

#### Example 4

Find in  $\mathbb{Z}$  the solution set of the inequality  $-11 \le 3 \times -5 < 4$ , then represent it on the number line.

#### Solution

$$: -11 \le 3 \times -5 < 4$$

$$\therefore -11 + 5 \le 3 \times -5 + 5 < 4 + 5$$

Dividing all sides by 3

$$\therefore \frac{-6}{3} \le \frac{3 \times 3}{3} < \frac{9}{3}$$

*i.e.* The S.S. = 
$$\{-2, -1, 0, 1, 2\}$$

Adding 5 to the three sides

$$\therefore -6 \le 3 \times < 9$$

$$\therefore -2 \leq x < 3$$



#### Try by yourself

Find the solution set of each of the following inequalities:

1  $2x-3 \ge 5$ , where  $x \in \mathbb{Q}$ 

2 5 X-10 < 2 X-1, where  $X \in \mathbb{N}$ 

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# Unit

# Statistics and Probability

Lesson One : Samples :

- Systematic sample.
- Random sample.

Lesson Two: Probability:

- Experimental probability.
- Theoretical probability.

#### Pierre Simon Marquis de Laplace (1749 - 1827)

He was a French mathematician and astronomer. His first work was published in 1771 starting with differential equations however he had already started to think about the mathematical and philosophical concepts of probability and statistics.



Pierre Simon Marquis de Laplace (1749 - 1827)

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Lesson One



#### Samples 5 4 1

Samples are greatly important for scientific and social studies and researches as when we study researches or different phenomena, these studies are not carried out on all the society but it is enough to study the results on samples representing the society under study.

#### For example:

#### In medical field :

When we make blood analysis to a person, we take a sample of his blood to make the analysis for it, this sample is enough to make a true decision for the all of his blood.



#### In industrial field:

When we check the production of a factory to know if its products are manufactured according to the certain specifications, we don't carry out this check to all the production of the factory but it is enough to check a sample of it on condition that this sample must represent the production of this factory completely, then we can generalize the results for all the production.



#### In the media field:

When we do a survey to know which TV program is the most effective on the public opinion, we don't do the survey on all inhabitants but we choose a sample representing all inhabitants with different classes, then we generalize the results for all society.



#### Why are samples used?

#### Samples are used for many reasons as:

- I Samples save time because if we try to check all the production of a factory, it will take a very long time.
- 2 Samples save money because the chosen produced units which are under check may be damaged and that leads to a great economic loss besides checking all the production needs a large number of researchers and a large number of laboratories.
- 3 Samples save efforts because checking all the production of a factory needs great efforts of a large number of researchers.

In this lesson, we will know the concept of the sample and its types and how it is chosen.

The concept of the sample : \_\_\_\_\_

A sample is a small part of a society. "society" means a collection, a set or a group of objects being studied and is selected randomly.

- From the previous , the selected sample should wholly represent the society (the object of study) and it shouldn't be based on a certain group and neglect the other , so that the results of the study can be near reality and we can make decisions according to these results, so we can generalise these results on the society as a whole.
- And the sample representing the society should be random.
  - This sample can be classified according to the method of selecting its elements into :

#### Systematic sample:

Systematic sample is the sample whose elements are selected from the elements of a society distributed randomly by following a certain system or method in selection.

#### For example :

To select a systematic sample representing 10% of the marks of students in a preparatory school in the mid-year exam in maths, to study the standards of students, we will do as follows:



- Ill Students must be distributed randomly in a numbered list , i.e. selection shouldn't be from certain classes as excellent students' classes or selecting certain classes and neglecting others.
- 2 We select in a regular way the tenth student in each 10 student from the students list i.e. we select the mark of the tenth, twentieth, thirtieth, ... students is the list.

#### Remark

If the society (the object of study) is allready divided into classes or groups as the school is divided into classes for boys and others for girls, then we select a part of each group to represent the sample so that it can represent the society as a whole.

#### Random sample:

Random sample is the sample whose elements are selected from the elements of a society distributed randomly by following a random and irregular method or system of selecting.

In this sample, each individual must get the same chance of selecting.

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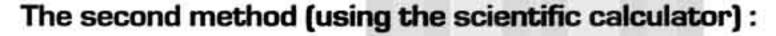
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Lesson One

So , we can select its elements by two methods :

The first method (manual method): It is done as follows:

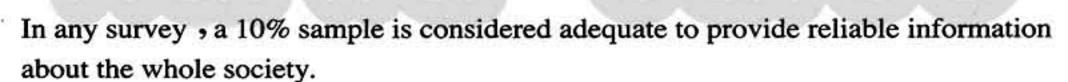
- 1 Every member of the society is given a number, then this number is written on a piece of paper such that all pieces of paper are of the same colour and size.
- 2 Each piece of paper is folded perfectly such that the written number does not appear and is put in a bag or a box and mixed together very well.
- 3 The selection is carried out by drawing a piece after piece without looking inside the paper till the operation of drawing is finished when the required number of selected members is done.



This method depends on using the random number function on the scientific calculator shown in the opposite figure by pressing the following keys successively from the left:



Then a random number in the range 0.000 to 0.999 will appear every time. Take the apparent numbers without the decimal point. The numbers which are greater than the whole number of the society under study should be ignored and , also if a number is repeated it must be ignored and taken once only.



#### Example

A factory has 300 workers. The people in charge of the monthly magazine of this factory want to develop this magazine by doing a survey of a sample representing 10% of the total number of the workers in this factory. Show how the selection of this sample can be carried out using the calculator.





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**\_** Unit **2** 

#### Solution

- The number of workers in the factory = 300 workers.
- $\therefore$  The number of the random sample =  $\frac{10}{100} \times 300 = 30$  workers.

Then we want to select 30 workers to do this survey. The selection operation can be carried out as follows:

- 1 Each worker in the factory is given a number from 1 to 300
- 2 Use the calculator to select 30 numbers randomly by the method mentioned before such that these numbers are included between 0 and 301 and the number that is more than 300 should be ignored.

#### For example :

successively. By pressing the keys

- If we get the decimal 0.56, then the number of the selected person is 56
- If we get the decimal 0.049, then the number of the selected person is 49
- If we get the decimal 0.132, then the number of the selected person is 132
- If we get the decimal 0.453, it must be ignored because 453 is more than 300 and so on till we get 30 numbers.

Assuming that the calculator gave us the shown numbers in the opposite table, then the workers who carry these numbers are the selected sample to carry out this survey.

56	49	132	141	249	272
254	256	4	213	74	198
131	2	156	47	172	13
8	3	3 85 82		9	38
41	14 34		279	118	103

#### Remark

The random numbers can be generated by using «Excel» program that will be explained in details at the end of this book.

Lesson Two



#### Probability

#### **Prelude**

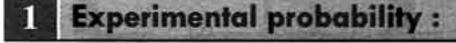
In our daily life, many times we ask ourselves about some affairs that may happen in the future and that we cannot give a certain result for them.

#### For example:

- If the Egyptian football team get to the finals of African nations championship, what is its chance for winning the cup?
- If an Egyptian citizen puts himself up for parliamentary elections in one of elections zones , what is his chance for winning in the elections?

All these questions' answers are expectations to what may happen (occur) in the future referring to previous experience , studies or observations.

When we answer these questions, we use some words as «may be, chance or probable». In mathematics, we call this probability. In this lesson, we will study: experimental probability, theoretical probability.



 If one of the Olympic swimmers wants to achieve a new record in the next Olympic Games, what is the probability that this swimmer achieves this record?



The answer to this question cannot be got by expecting, hoping or by doing a survey of the opinions of the trainers or by asking the swimmer himself, but by trying.

- i.e. The swimmer covers the needed distance in the race several times, then we record the number of times in which he could achieve the requested number and divide it by the total number of times, so the quotient is the probability of achieving the new record in the next Olympics.
- i.e. The experimental probability depends on performing an experiment, then we record the results and use them to calculate the value of probability of an event occurrence using the rule:

Number of trials in which the outcome occurs Experimental probability = Total number of trials





Unit 2

It is noticed that the more we carry out the experiment, the more we obtain an accurate value for the probability.

#### Example 1

If we tossed a piece of coin with double face 200 times and the results of appearance of a head or a tail in each toss were recorded in a table as shown:





			He	ads		Mrs.		T	ails			Total
Statistics	<del>+++</del>	<i>\\\\</i>			<del>##</del>	100	<del>}</del>			<i>+++</i>	<del>    </del>	
Tallies	<del>+++</del>	+++			<del>\</del> ##		+++	***			+++	
Frequency			1	06				9	94			200

#### Calculate:

- The probability of appearance of a head.
- 2 The probability of appearance of a tail.

#### Solution

- The probability of appearance of a head =  $\frac{\text{Number of getting heads}}{\text{Total number of tosses}} = \frac{106}{200} = 0.53$
- The probability of appearance of a tail =  $\frac{\text{Number of getting tails}}{\text{Total number of tosses}} = \frac{94}{200} = 0.47$

#### Try by yourself

A fair die is rolled 25 times. The results of appearance of a number on the upper face were recorded in the following table:

020 - 1500 1	1	2	3	4	5	6	Total
Statistics tallies							
Frequency							25

#### Calculate:

- The probability of appearance of the number 4
- 2 The probability of appearance of the number 3

.....

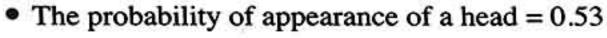
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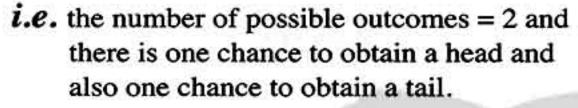
Lesson Two

#### Theoretical probability:

In the previous, we carried out the experiment of tossing a piece of coin and we found that:



 The probability of appearance of a tail = 0.47 But when we study this experiment theoretically, we find that: If we tossed the coin piece once, then we obtain either a head or a tail.



- (i.e. all outcomes of the experiment have the same chance to happen).
- *i.e.* the probability of appearance of a head =  $\frac{1}{2}$  = 0.50 and the probability of appearance of a tail =  $\frac{1}{2}$  = 0.50

#### Notice that :

We can express the probability by percentage.

i.e. we write the probability of appearance of a head = 50%

#### Remark

Notice the difference between the experimental probability of appearance of a head (0.53) and the theoretical probability of appearance of a head (0.50)

We can interpret this as:

The more the number of times of carrying out the experiment increases, the more the value of experimental probability approaches the value of theoretical probability.

Random experiment : \_\_\_

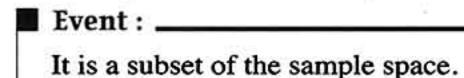
It is an experiment in which we can specify all its possible outcomes before carrying it out but we cannot determine certainly which of them will occur.

Sample space :

It is the set of all possible outcomes of a random experiment and it is denoted by S

#### For example:

- When we toss a piece of coin once, then the sample space is  $S = \{H, T\}$
- When we roll a fair die once observing the apparent number on the upper face, then the sample space is  $S = \{1, 2, 3, 4, 5, 6\}$







#### For example:

If A is the event of appearance of an odd number when rolling a fair die once and observing the apparent number on the upper face, then  $A = \{1, 3, 5\}$ ,  $A \subset S$ 



#### Generally

The probability of any event occurrence  $A \subset S$  is denoted by P(A) and it is given by using the relation:

$$P(A) = \frac{\text{The number of elements of the event } (A)}{\text{The number of elements of sample space } (S)} = \frac{n(A)}{n(S)}$$

#### Example 2

If a fair die is rolled once and we observe the apparent number on the upper face, find the probability of each of the following events:

1 A is the event of appearance of a number more than 4 (Approximating the result to the nearest hundredth)



- 2 B is the event of appearance of an even number.
- 3 C is the event of appearance of a number equal to 5 (Approximating the result to the nearest tenth)
- 4 D is the event of appearance of a number equal to 7
- 5 E is the event of appearance of a number less than 7

#### Solution

$$S = \{1, 2, 3, 4, 5, 6\}, n(S) = 6$$

- $\mathbf{1} \mathbf{A} = \{5, 6\}, \mathbf{n}(\mathbf{A}) = 2$ 
  - ∴ P(A) =  $\frac{2}{6} = \frac{1}{3} \approx 0.33$  (to the nearest hundredth)
- **2** B =  $\{2, 4, 6\}$ , n (B) = 3 : P(B) =  $\frac{3}{6}$  = 0.5
- $3 C = \{5\}, n(C) = 1$ 
  - $\therefore P(C) = \frac{1}{6} \approx 0.2$  (to the nearest tenth)
- - $\therefore$  P(D) =  $\frac{0}{6}$  = Zero (the impossible event)
- $\mathbf{5} \mathbf{E} = \{1, 2, 3, 4, 5, 6\}, \mathbf{n}(\mathbf{E}) = 6$ 
  - :.  $P(E) = \frac{6}{6} = 1$ (the certain event)

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Lesson Two

#### Remarks

- The impossible event: is the event that has no chance for occurring.
  - i.e. the probability of the impossible event = Zero
- 2 The certain event: is the event that has all the possible outcomes.
  - *i.e.* the probability of the certain event = 1
- 3 The value of probability of any event is not less than zero and not more than one
  - i.e.  $0 \le$  The probability of an event occurrence ≤ 1

#### Example 3

From the set of digits  $\{3,4,5\}$ , form a two-digit number, then find the probability of each of the following events:

- 1 A « the event that the unit digit is odd »
- 2 B « the event that the tens digit is even »
- 3 C « the event that the two digits are odd »
- 4 D « the event that the sum of the two digits = 8 »
- 5 E « the event that the product of the two digits = 20 »

#### Solution

$$S = \{33, 43, 53, 34, 44, 54, 35, 45, 55\}, n(S) = 9$$

$$\mathbf{II} A = \{33, 43, 53, 35, 45, 55\}, n(A) = 6$$

:. 
$$P(A) = \frac{6}{9} = \frac{2}{3}$$

$$B = \{43, 44, 45\}, n(B) = 3$$

:. 
$$P(B) = \frac{3}{9} = \frac{1}{3}$$

$$3C = {33,53,35,55}, n(C) = 4$$

$$\therefore P(C) = \frac{4}{9}$$

$$\mathbf{4} D = \{53,44,35\}, n(D) = 3$$

:. 
$$P(D) = \frac{3}{9} = \frac{1}{3}$$

$$\mathbf{5} \mathbf{E} = \{54, 45\}, \mathbf{n} (\mathbf{E}) = 2$$

$$\therefore P(E) = \frac{2}{9}$$

#### Example 4

A bag has an amount of marbles of the same size and touch. If 2 marbles are red > 3 are blue and 5 are white and a marble is drawn randomly , calculate :

- The probability of that (the drawn marble is red)
- 2 The probability of that (the drawn marble is blue)
- 3 The probability of that (the drawn marble is white)
- 4 The probability of that (the drawn marble is not blue)



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#### Solution

The probability of occurrence of a certain outcome

The number of possible chances to get this outcome

The total number of chances

The total number of marbles = 2 + 3 + 5 = 10

The probability of that (the drawn marble is red)

$$= \frac{\text{The number of red marbles}}{\text{The total number of marbles}} = \frac{2}{10} = \frac{1}{5}$$

2 The probability of that (the drawn marble is blue)

$$= \frac{\text{The number of blue marbles}}{\text{The total number of marbles}} = \frac{3}{10}$$

3 The probability of that (the drawn marble is white)

$$= \frac{\text{The number of white marbles}}{\text{The total number of marbles}} = \frac{5}{10} = \frac{1}{2}$$

4 The probability of that (the drawn marble is not blue)

$$= \frac{\text{The number of marbles which aren't blue}}{\text{The total number of marbles}} = \frac{10-3}{10} = \frac{7}{10}$$

#### Remark

In the previous example, notice that:

P (red marble) =  $\frac{2}{10}$ , P (blue marble) =  $\frac{3}{10}$ ,

P (white marble) = 
$$\frac{5}{10}$$
,  $\therefore \frac{2}{10} + \frac{3}{10} + \frac{5}{10} = 1$ 

... the sum of probabilities of all outcomes of a random experiment = 1

So, if the probability of occurrence of an event is a, then the probability that it doesn't occur = 1 - a

So, we can find the probability that the drawn marble is not blue as follows:

The probability that the drawn marble is not blue

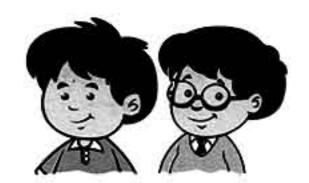
= 1 - the probability that it is blue =  $1 - \frac{3}{10} = \frac{7}{10}$ 

Lesson Two

## Example (5

A Class has some students who wear glasses and other students who don't wear glasses.

If a student is chosen randomly from this class and the probability that this student wears glasses is 0.1



- I Find the probability that this student does not wear glasses.
- 2 If the number of students in this class is 30 students, find the expected number of students who wear glasses.

#### Solution

- If The probability that this student does not wear glasses = 1 the probability that theNotice that : student wears glasses = 1 - 0.1 = 0.9
- 2 The expected number of students who wear glasses =  $0.1 \times 30 = 3$  students.

The expected number of outcomes of an event

= The probability of occurrence of this event × the total number of all possible outcomes.

#### Example 6

A spinner game was divided into some equal sectors. 2 of them are green , 4 are blue and the rest are red. If the probability that the pointer stops pointing at a green sector is  $\frac{1}{6}$ , then find the number of red sectors.

#### Solution

- : The probability that the pointer stops pointing at a green sector
- The number of green sectors

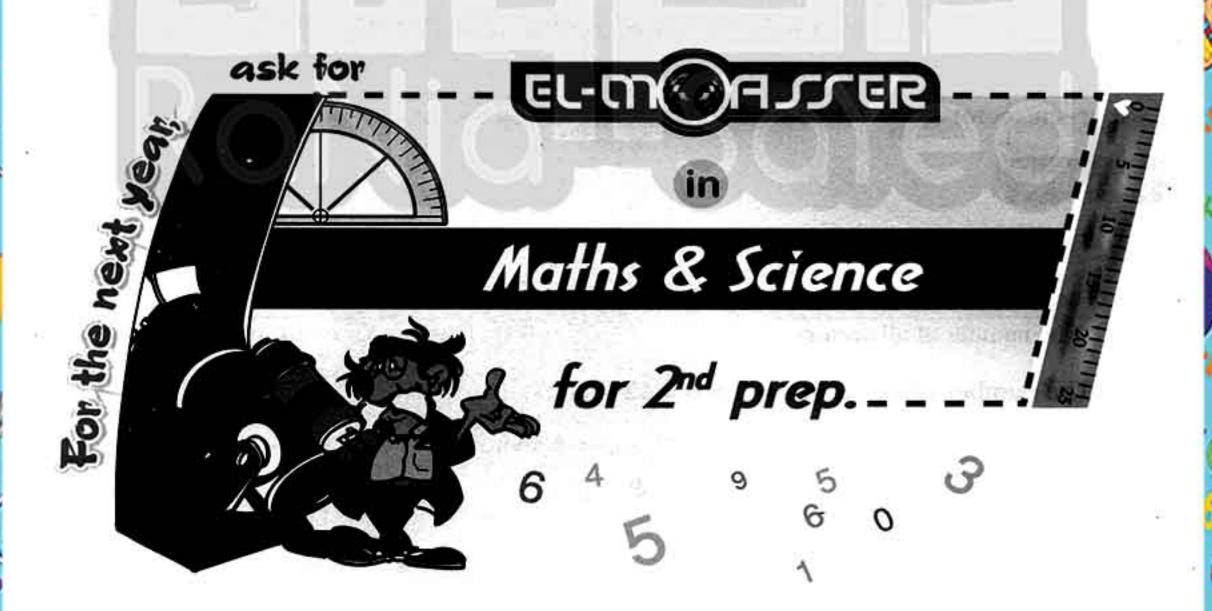
$$\therefore \frac{1}{6} = \frac{2}{\text{The number of all sectors}}$$

- $\therefore$  The number of all sectors =  $2 \times 6 = 12$  sectors.
- $\therefore$  The number of red sectors = 12 (2 + 4) = 6 sectors.

**L** Unit **2** 

#### Try by yourself

0	A box contains cards numbered from 1 to 15. If a card is drawn randomly, what is the probability that the written number on the card is divisible by 5?  Answer:
2	An experiment has 3 outcomes. If the probability of occurrence of the first outcome is 0.3 and the probability of the second is 0.45, calculate the probability of the third outcome.  Answer:
3	A farm has 2000 cows. If the probability of cow madness infection in this farm is 0.17, what is the expected number of infected cows?  Answer:



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# Numbers and Algebra

Lesson One: Repeated multiplication.

**Lesson Two**: Non-negative integer powers.

Lesson Three: Negative integer powers.

Lesson Four: Scientific notation of the rational number.

Lesson Five : Order of mathematical operations.

Lesson Six: The square root of a perfect square rational

number.

Lesson Seven: Solving equations of the first degree in one

unknown in Q.

**Lesson Eight**: Solving inequalities in Q.

General exercises from the school book at the end of the unit.

From the school book

#### Exercise

#### On repeated multiplication

#### Choose the correct answer from those given:

- (1) The multiplicative inverse of the number  $\left(\frac{2}{5}\right)^0 = \cdots$ 
  - (a)  $\frac{5}{2}$

- (b)  $-\frac{2}{5}$

- (d)0
- 2 The additive inverse of the number (-3)0 is .......
  - (a) 1

(b) - 3

(c) 3

- $(d) (3)^0$
- (3) The multiplicative inverse of the number (-1)<sup>3</sup> is .......
  - $(a) (-1)^3$
- (b)  $(-1)^2$
- (c)  $1^3$
- (d)  $1^2$

- (4) The additive inverse of the number  $\left(-\frac{2}{5}\right)^2$  is ......
  - (a)  $\frac{4}{25}$

- (b)  $-\frac{4}{25}$
- (c)  $\frac{25}{4}$
- (d)  $-\frac{25}{4}$

- **(5)**  $\left(\frac{1}{4}\right)^0 + \frac{1}{4} = \cdots$ 
  - (a)  $\frac{1}{4}$

(b)  $\frac{3}{4}$ 

- (c)  $\frac{5}{4}$
- (d)  $\frac{2}{4}$

- (6)  $\left(\frac{5}{3}\right)^2 \times \left(\frac{3}{5}\right)^0 = \dots$ 
  - (a)  $\frac{5}{3}$

(b)  $\frac{25}{9}$ 

(c) 0

(d) 1

- (7) If x = y, then  $(\frac{3}{5})^{x-y} = \cdots$ 
  - (a)  $\frac{3}{5}$

(c) 1

(d) 0

- (8)  $\left(\frac{a}{b}\right)^2 \times \frac{b^2}{a^2} = \dots$  (where  $ab \neq 0$ )
  - (a) ab

- (b)  $\left(\frac{a}{b}\right)^4$
- (c)  $(ab)^0$
- $(d) \frac{a}{b}$

- (9) If  $x = -\frac{1}{2}$  and y = 3, then  $x^y = \dots$ 
  - (a)  $\frac{1}{8}$

- (b)  $-\frac{1}{8}$
- (c)  $\frac{1}{6}$
- $(d) \frac{1}{6}$

- (10) If:  $y^{26} + y^{27} = 0$ , then  $y = \dots$ 
  - (a) 1

(b) - 1

(c) 2

(d) - 2

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Lesson One

2 Calculate each of the following, then put the result in the simplest form:

$$(1)(\frac{1}{2})^3$$

(2) 
$$\square \left(\frac{1}{3}\right)^4$$

$$(3)\left(\frac{3}{5}\right)^2$$

(4) 
$$\square \left(-\frac{1}{7}\right)^3$$

(5) 
$$\square$$
  $\left(-\frac{3}{4}\right)^4$ 

(6) 
$$\left(\frac{5}{9}\right)^0$$

$$(7) \left(1\frac{1}{5}\right)^2$$

(8) 
$$\left(-2\frac{1}{2}\right)^3$$

$$(9)(0.04)^2$$

$$(10)(1.5)^3$$

$$(11)(-3.2)^2$$

(12) 
$$\left(1-1\frac{2}{3}\right)^2$$

Calculate each of the following, then put the result in the simplest form:

(1) 
$$8 \times (\frac{1}{2})^3$$

(3) 
$$\square (-\frac{3}{5})^3 \times (-\frac{25}{27})$$

$$(5)\left(\frac{4}{3}\right)^2\times\left(\frac{3}{2}\right)^3$$

$$(7) \left(2\frac{1}{2}\right)^2 \times \frac{4}{25}$$

(2) 
$$\square \left(-\frac{3}{4}\right)^2 \times \frac{8}{27}$$

$$(4) \left(\frac{3}{5}\right)^2 \div \left(-\frac{9}{125}\right)$$

(6) 
$$\square \left(-\frac{5}{6}\right)^2 \div 3\frac{3}{4}$$

(8) 
$$\square 2\frac{7}{9} \div \left(-1\frac{2}{3}\right)^2$$

Calculate each of the following, then put the result in the simplest form:

$$(1) \left(\frac{4}{5}\right)^2 \times \frac{5}{16} \times \left(\frac{2}{3}\right)^0$$

(3) 
$$\left(-\frac{5}{3}\right)^4 \times \left(-\frac{3}{5}\right)^3 \times (-1)^7$$

(5) 
$$\left[ \left( \frac{5}{2} \right)^3 \div \left( \frac{3}{2} \right)^4 \right] \times \left( \frac{3}{5} \right)^3$$

$$(2)\frac{3}{4} \times (-\frac{2}{3})^3 \times (\frac{3}{2})^2$$

(4) 
$$\square \left(-\frac{2}{3}\right)^3 \times \left(\frac{1}{3}\right)^3 \div \left(-\frac{2}{9}\right)^2$$

(6) 
$$\square \left(-\frac{1}{2}\right)^3 \div \left[8 \times \left(-\frac{1}{2}\right) \times \frac{3}{4}\right]$$

If  $x = -\frac{2}{3}$  and  $y = -\frac{1}{3}$ , find the value of :  $x^2 + y^3$ 

 $< \frac{11}{27} >$ 

If  $a = \frac{2}{3}$  and  $b = -\frac{4}{3}$ , find the value of :  $|a^3 \div b^3|$ 

 $\ll \frac{1}{8} \gg$ 

7 If x = 0.5,  $y = -\frac{2}{3}$  and z = -3, find the value of :  $9 \times y^2 - z^3$ 

« 29 »

If  $a = -\frac{1}{2}$ , b = 2 and  $c = \frac{3}{4}$ , find the numerical value of:  $a^3b^2 + b^2c - 8$  abc

 $\times 8\frac{1}{2} \times$ 

If  $x = -\frac{3}{2}$ ,  $y = \frac{1}{2}$  and  $z = -\frac{4}{3}$ , find the numerical value of each of the following in its simplest form:

$$(1) X^2 y^2 z^2$$

(2) 
$$\chi^2 \div z^2$$

(3) 
$$\chi^2 - y z^2$$

"1" (2) 
$$x^2 \div z^2$$
"49" (4)  $\frac{x^2 y^2 z^2}{x + y}$ 

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 $2 \frac{9}{16} = (\frac{3}{4})^{\dots}$ 

(12)  $2^2 + 2^2 = 2^{\dots}$ 

(4)  $2\frac{1}{4} = \frac{3}{1} = \frac{3}{2}$ 

(6) 64 % =  $\frac{4}{5}$ 

(B) If c = -3 and d = -5, then  $\left(\frac{c}{d}\right)^2 = \cdots$ 

(10) If  $x = \frac{1}{2}$  and  $y = \frac{2}{3}$ , then  $x^2 y^2 = \dots$ 

#### 10 Complete the following:

(1) 
$$\frac{8}{27} = (\frac{2}{3})^{\dots}$$

(3) 
$$-\frac{64}{125} = \left(-\frac{4}{5}\right)^{\dots}$$

**(5)** 
$$0.027 = \frac{....}{...} = \left(\frac{3}{10}\right)^{...}$$

(7) If 
$$\frac{x}{y} = -\frac{2}{5}$$
, then  $\left(\frac{x}{y}\right)^3 = \dots$ 

(9) If: 
$$\frac{a}{b} = 0.2$$
, then:  $\left(\frac{a}{b}\right)^3 = \cdots$ 

(1) 
$$\square$$
  $\left(-\frac{1}{2}\right)^3 - \left(-\frac{1}{2}\right)^2 = \dots$ 

(13)  $\frac{3}{4}$ ,  $\frac{9}{16}$ ,  $\frac{27}{64}$ , ...... (in the same pattern)

(13) 
$$\frac{3}{4}$$
,  $\frac{9}{16}$ ,  $\frac{27}{64}$ , ...... (in the same part)

(14) The greater number of the two numbers  $\left(\frac{1}{4}\right)^2$  and  $\left(-\frac{8}{3}\right)^3$  is .......

#### Geometric Application

11 If the volume of the cube is found from the relation  $V = \ell^3$  where V is the cube volume and  $\ell$  is its edge length, then calculate the volume of the cube whose edge length is  $1\frac{1}{2}$  cm.

 $\frac{27}{8}$  cm<sup>3</sup>. »



#### For excellent pupils

- 12 Choose the correct answer from those given:
  - (1) If  $x \in \{0, 1, 2, 3\}$ , then the greatest value of the number  $(\frac{1}{2})^x$  is when  $x = \dots$

- (2) If  $x \in \{0, 1, 3, 4\}$ , then the smallest value of the number  $\left(-\frac{2}{5}\right)^x$ is when  $x = \cdots$ 
  - (a) 0

(b) 1

(c) 3

- (d)4
- 13 Arrange the following numbers ascendingly without expanding:

$$\left(\frac{2}{3}\right)^2, \left(-\frac{2}{3}\right)^3, \left(-\frac{1}{3}\right)^2, \left(-\frac{1}{3}\right)^3$$

Lesson Two

From the school book

## Exercise

#### On non-negative integer powers

1 Calculate each of the following, then put the result in the simplest form:

$$(1)^2 \times (\frac{1}{4})^2$$

(4) 
$$\frac{1}{5} \times \left(-\frac{1}{5}\right)^4$$

$$\bigcirc \square (-\frac{3}{5})^7 \div (\frac{3}{5})^5$$

$$(0)(\frac{4}{5})^8 \div (\frac{4}{5})^6 \times \frac{4}{5}$$

(2) 
$$\square (\frac{2}{3})^3 \times (\frac{2}{3})^2$$

(5) 
$$\left(\frac{1}{6}\right)^9 \div \left(\frac{1}{6}\right)^8$$

(B) 
$$\left(-\frac{5}{2}\right)^2 \div 2\frac{1}{2}$$

(2) 
$$\square \left(\frac{2}{3}\right)^3 \times \left(\frac{2}{3}\right)^2$$
 (3)  $\square \left(-\frac{2}{3}\right)^3 \times \left(\frac{2}{3}\right)^2$ 

**6** 
$$\square$$
  $\left(\frac{2}{7}\right)^5 \div \left(\frac{2}{7}\right)^3$ 

2 Calculate each of the following, then put the result in the simplest form:

(1) 
$$\frac{3^7 \times 3^3}{3^6}$$

$$(4) \frac{(-2)^5 \times 2^4}{(-2)^3 \times 2^2}$$

$$x^4 \times y^3 \times x^5$$
$$x^6 \times y^2$$

(2) 
$$\frac{2^6 \times 2}{2^3 \times 2^4}$$

$$\frac{x^2 \times x^3 \times x^4}{x^7 \times x}$$

(B) 
$$\frac{xy^2 \times x^2y}{x^2y^2}$$

(3) 
$$\frac{(-5)^4 \times 5^2}{5^3}$$

(6) 
$$\frac{(-3)^5 \times (-2)^7}{(-3)^3 \times (-2)^5}$$

$$\frac{\left(-1\frac{1}{2}\right)^5 \times \left(-1\frac{1}{4}\right)^8}{\left(-\frac{3}{2}\right)^4 \times \left(-\frac{5}{4}\right)^6}$$

Calculate each of the following, then put the result in the simplest form:

(4) 
$$\square \left(\frac{x^2}{v^3}\right)^2$$

$$\bigcirc \square \left(-\frac{x^3}{y^2}\right)^2$$

$$\left(\frac{5 \times 3}{3 \text{ y}}\right)^2$$

$$\left(\frac{a^3b^2}{c^5}\right)^3$$

(B) 
$$\frac{(4 \times^3 y^2)^7}{(2 \times^2 y)^7}$$

$$(3)\left(-\frac{2ab}{3c}\right)^4$$

(9) 
$$\frac{(2 \text{ a})^3 \times (2 \text{ a})^4}{(-2 \text{ a})^6 \times \text{a}}$$

Calculate each of the following, then put the result in the simplest form:

$$\left(1 + \left(\frac{1}{2}\right)^2\right)^2$$

$$(4) \left( \left( -1 \frac{1}{3} \right)^2 \right)^3$$

$$(2\frac{1}{2})^2 \times (-\frac{2}{5})^2$$

**(5)** 
$$\left(\frac{3}{5}\right)^{10} \times \left(\frac{5}{3}\right)^{10}$$

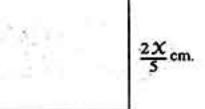
$$\left(\frac{x^3}{v^2}\right)^{16} \div \left(\frac{x^2}{v^2}\right)^{16}$$

$$\bigcirc \left( \left( \frac{2}{7} \right)^2 \right)^3 \times \left( \frac{7}{2} \right)^6$$

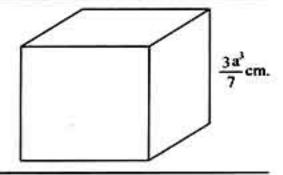
المحاصلا ریاضیات لفات (فیارین) / ۱ باعدادی / تیری ۱۲:۲۱

Unit 1

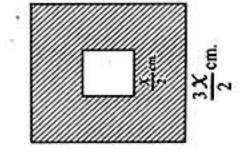
Find the area of the square whose side length is  $\frac{2 x}{5}$  cm.



Find the volume of the cube whose edge length is  $\frac{3 a^3}{7}$  cm.



7 In the opposite figure:
A square is drawn inside another square.
Find the area of the shaded part.



Match each expression in column (A) with an equivalent expression in column (B):

Column (A)	Column (B)
$(1) (x^2)^n$	(a) $x^{n^2}$
(2) (X <sup>n</sup> ) <sup>n</sup>	$(\mathbf{b}) \frac{3  \mathbf{m}^{\mathbf{c}}}{2  \mathbf{n}^{\mathbf{c}}}$
(3) $(x y^a)^b$	(c) $27 \times 3a$
$(4)\left(\frac{x}{y^a}\right)^b$	$(\mathbf{d})  \frac{3^{\mathbf{c}}  \mathbf{m}^{\mathbf{c}}}{2^{\mathbf{c}}  \mathbf{n}^{\mathbf{c}}}$
$(5) (-3 X^a)^3$	(e) $x^{2n}$
(6) $(3 \times a)^3$	$(f) - 27 x^{3a}$
$(7) \ \frac{3}{2} \left(\frac{m}{n}\right)^{c}$	$(\mathbf{g})  \frac{\mathbf{n}^{\mathbf{b}}}{\mathbf{y}^{\mathbf{a}\mathbf{b}}}$
$(8) \left(\frac{3 \text{ m}}{2 \text{ n}}\right)^{c}$	
	(h) $x^{b} y^{ab}$ (i) $\frac{x^{b}}{y^{ab}}$ (j) $x y^{ab}$
¥ = '.	(j) X y <sup>ab</sup>

Lesson Two

#### Choose the correct answer from those given:

(1) 
$$3^2 \times 3^5 = \cdots$$

(a) 
$$3^7$$

(b) 
$$3^3$$

(c) 
$$3^{10}$$

(d) 
$$3^{25}$$

(a) 
$$5^2 + 5^2 = \cdots$$

(a) 
$$10^2$$

(b) 
$$10^4$$

(c) 
$$5^4$$

(3) 
$$3^5 \times 2^5 = \cdots$$

(a) 
$$5^{10}$$

(b) 
$$6^{10}$$

(c) 
$$6^5$$

(d) 
$$6^{25}$$

(4) 
$$(5a)^0 = \cdots , a \neq 0$$

(a) 
$$3^6$$

(b) 
$$3^5$$

(c) 
$$3^8$$

(d) 
$$3^{23}$$

**(6)** 
$$(5^2)^3 = \cdots$$

(a) 
$$5^6$$

2+2-8

(b) 
$$5^5$$

(c) 
$$5^{23}$$

$$(7) 3^{10} + 3^{10} + 3^{10} = \dots$$

(a) 
$$3^{10}$$

(b) 
$$3^{30}$$

(c) 
$$9^{10}$$

(d) 
$$3^{11}$$

$$(8) 4^{x} + 4^{x} + 4^{x} + 4^{x} = \dots$$

(a) 
$$4^{x+4}$$
 (b)  $4^{4x}$ 

(b) 
$$4^{4}$$
 x

(c) 
$$4^{x+1}$$

(d) 
$$4 x^4$$

(9) 
$$\frac{(3^2)^5}{(3^5)^2} = \cdots$$

(a) 
$$3^{10}$$

(c) 
$$3^{25}$$

$$(10)$$
  $\frac{(x^2)^3}{x^3} = \dots, x \neq 0$ 

(a) 
$$x^6$$

(b) 
$$x^2$$

(c) 
$$x^3$$

**(1)** 
$$(2 y)^3 = \cdots$$

(a) 
$$2 y^3$$

(c) 
$$8y^3$$

$$(b^3)^4 = \cdots$$

(a) 
$$b^{34}$$

(b) 
$$b^{7}$$

(c) 
$$b^3 \times b^3 \times b^3$$

(d) 
$$b^4 \times b^4 \times b^4$$

(13) 
$$\square$$
 The quarter of the number  $4^{20} = \cdots$ 

(a) 
$$4^5$$

(b) 
$$4^{10}$$

(c) 
$$4^{19}$$

(d) 
$$2^{10}$$

Unit 1

10 Simplify to the simplest form:

$$\frac{(2 \text{ y})^4 \times (3 \text{ y})^2}{12 \text{ y}^5}$$
, then find the value of the result at  $y = -\frac{1}{6}$ 

« – 2 »

If  $a = \frac{1}{2}$ ,  $b = \frac{3}{4}$  and  $c = -\frac{2}{3}$ , find the numerical value of each of:

(1) 
$$(c^2 b)^3$$

$$(2) (4 a^3 c)^2$$

(3) 
$$(a^2 b c^2)^2$$

$$\frac{1}{27}, \frac{1}{9}, \frac{1}{144}$$
»

If  $a = \frac{5}{3}$ ,  $b = -\frac{3}{2}$  and  $c = \frac{2}{5}$ , find the numerical value of each of:

(1) 
$$\frac{(a^2 c^2)^2}{b}$$

$$(2) \left( \frac{2ab}{5c} \right)^3$$

$$\frac{32}{243}, -\frac{125}{8}$$

13 If  $x = -\frac{1}{2}$ ,  $y = \frac{3}{4}$  and  $z = -\frac{3}{2}$ ,

find the numerical value of each of the following in the simplest form:

(1) 
$$x^3 y^2$$

(2) 
$$y^3 x^2$$

$$3 \frac{x^3}{y^2 z^2}$$

$$\frac{9}{128}, \frac{27}{256}, -\frac{8}{87}$$

14 Complete the following:

(1) 
$$\left( \left( \frac{7}{9} \right)^3 \right)^4 = \frac{7^{12}}{3 \cdots}$$

(2) If: 
$$(\frac{3}{4})^5 \times x = (\frac{3}{4})^7$$
, then  $x = \dots$ 

(3) The greater number in the two numbers  $((-3)^5)^3$  and  $((-3)^2)^4$  is .......

(4) 
$$((-1)^5)^2 - ((-1)^3)^2 = \cdots$$

(5) 
$$\frac{4^4}{4^3} + \frac{4^3}{4^2} + \frac{4^2}{4} + 4 = 2$$
 .....

(6) 
$$2^{2X} \times 4^X = 4^{\dots}$$



15 From computer technology , we know that :

1 kilobyte =  $2^{10}$  bytes,

1 megabyte =  $2^{10}$  kilobytes,

1 gigabyte = 2 10 megabytes >

1 terabyte =  $2^{10}$  gigabyte,

How many bytes are there in one terabyte?



2

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Lesson Two



#### For excellent pupils

16 If four times a number is  $4^3$ , find  $\frac{3}{4}$  this number.

«12»

If  $X = \left( \left( \frac{2}{3} \right)^5 \right)^2$  and  $y = 3 \left( \frac{3}{2} \right)^9 - \left( \frac{3}{2} \right)^{10}$ 

, prove that the number X is the multiplicative inverse of the number y

If  $x = \frac{1}{5}$  and y = 5, find the value of :  $x^{15}$  y<sup>14</sup>

19 Prove that: (1)  $5^{X+2} - 5^{X+1} = 20 \times 5^X$ 

(2)  $3^{15} + 3^{14}$  is divisible by 4



## <del>essesses</del>

- Worksheets.
- Models of the mid-term examination.

- Final examinations.

free part



III From the school book

## Exercise

#### On negative integer powers

1 Evaluate each of the following:

(2) 
$$\coprod 5^{-2}$$

(3) 
$$\left(\frac{1}{2}\right)^{-1}$$

$$(4)\left(-\frac{2}{3}\right)^{-2}$$

$$(5)(0.2)^{-2}$$

(6) 
$$(1.2)^{-1}$$

2 Evaluate each of the following:

(1) 
$$\square$$
  $3^7 \times 3^{-3}$ 

(2) 
$$2^{-2} \times 2^{-3}$$

(3) 
$$\square \frac{3}{3^{-2}}$$
 (4)  $\square \frac{6^{-2}}{6^{-3}}$ 

(4) 
$$\square \frac{6^{-2}}{6^{-3}}$$

3 Evaluate each of the following:

(1) 
$$\square$$
 (5<sup>-1</sup>)<sup>-3</sup>

$$(2) (3^{-2})^2$$

$$(3) (0.25)^{-2}$$

$$(4) (2^{-1} \times 2^{-2})^3$$

(5) 
$$\square \left(\frac{3^{-1}}{3}\right)^2$$

4 Evaluate each of the following:

(1) 
$$\square$$
  $\frac{8 \times 8^{-2}}{8^{-3}}$ 

(2) (1) 
$$\frac{7^{-2} \times 7^5}{7^3}$$

(3) 
$$\frac{2^5 \times 2^{-2}}{2^{-4} \times 2^3}$$

$$(4) \frac{2^3 \times 2^{-3}}{(2^2)^2}$$

$$(5) \ \frac{(3^{-2})^3}{3^{-2} \times 3^{-6}}$$

(6) 
$$\square \left(\frac{9^3 \times 9}{9^5}\right)^{-3}$$

$$(7) \left( \frac{4^{-2} \times 3}{4^{-3}} \right)^{-3}$$

(B) 
$$\left(\frac{2^5 \times 3^2}{3^4 \times 2^3}\right)^{-1}$$

(9) 
$$\square$$
  $(3^0 \times 2^{-2})^{-2}$ 

(10) 
$$(3^0 - 2^{-2})^{-2}$$

(11) 
$$\frac{(10)^2 \times (0.01)^3}{(10)^{-3}}$$

5 Simplify each of the following and write the result in terms of positive exponents, where the denominator does not equal zero:

(1) 
$$\square$$
 7  $x^{-1}$ 

(2) 
$$\square x^{-1} y^2$$

(3) 
$$\square$$
  $a^{-2}b^{-3}$ 

(4) 
$$\coprod X^3 \times X^{-5}$$

(5) 
$$X^3 \times X^{-2} \times X^{-1}$$

(7) 
$$X' \div X^{-3}$$

(10) 
$$\square$$
  $(a^2 \times a^{-5})^2$ 

(11) 
$$(X^2)^{-3} \times (X^{-3})^{-2}$$

(5) 
$$X^3 \times X^{-2} \times X^{-1}$$
 (6)  $\square \frac{C^{-5}}{C^2}$  (7)  $X^7 \div X^{-5}$  (8)  $\square (a^{-2})^3$  (9)  $\square (b^{-1})^{-3}$  (10)  $\square (a^2 \times a^{-5})^2$  (11)  $(X^2)^{-3} \times (X^{-3})^{-2}$  (12)  $\square \left(\frac{y^5}{y^{-2}}\right)^{-3}$ 

$$(13) \frac{x^2 \times x^{-3}}{x^{-4} \times x}$$

(17)  $(X + X^{-1})^2$ 

(14) 
$$\frac{(x^2)^{-3} \times (x^{-1})^2}{x^{-3} \times x^{-4}}$$

$$(15) \left( \frac{x^{-2} \times y^{-1}}{y^{-3} \times x} \right)^{-1}$$

(13) 
$$\frac{x^2 \times x^{-3}}{x^{-4} \times x}$$
 (14)  $\frac{(x^2)^{-3} \times (x^{-1})^2}{x^{-3} \times x^{-4}}$  (15)  $\left(\frac{x^{-2} \times y^{-1}}{y^{-3} \times x}\right)^{-1}$  (16)  $\square \frac{a^{-1}}{b^2} \left(\frac{a^{-1}}{2b^2}\right)^{-2}$ 

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(Lesson Three)

#### 6 Complete the following:

(1) 
$$2^{-3} \times C^0 = \cdots$$

(4) 
$$\square$$
  $(3 \ x^{-1})^2 = 9 \ x^{---} = \frac{9}{\dots}$   
(5)  $(3 \ y^{-2})^{-2} = \dots$   
(7)  $\square$   $(2 \ x^{-2} \ y^{-3} = \frac{2}{\dots}$   
(8)  $\frac{x^{-5}}{y^{-5}} = (\dots)^5$   
(9)  $(\frac{1}{2})^2 + 2^0 - (2)^{-2} = \dots$ 

(7) 
$$\square$$
 2  $\chi^{-2}$  y  $^{-3} = \frac{2}{\dots}$ 

(10) 
$$(x^2)^{...} = \frac{1}{x^4}$$

(a) 
$$\square$$
  $(b^{-1})^{-3} = b^{---}$ 

(5) 
$$(3 y^{-2})^{-2} = \cdots$$

(8) 
$$\frac{x^{-5}}{y^{-5}} = (\cdots)^5$$

$$(11) 2^{10} \times 2^{-10} = 3^{\cdots}$$

(a) 
$$\square$$
  $(b^{-1})^{-3} = b^{---}$  (3)  $\square$   $2 x^{-3} = \frac{2}{---}$ 

(6) 
$$\square$$
 (3 a<sup>2</sup>)<sup>-1</sup> =  $\frac{1}{2}$ 

(9) 
$$\left(\frac{1}{2}\right)^2 + 2^0 - (2)^{-2} = \dots$$

#### 7 Choose the correct answer from those given:

(13) If:  $X = \frac{1}{2}$ ,  $y = \frac{1}{4}$ , then  $(X - y)^{-1} = \dots$ 

(1) If 
$$a^{-1} = \frac{2}{3}$$
, then  $a = \dots$ 

(a) 
$$-\frac{2}{3}$$
 (b)  $\frac{3}{2}$ 

(b) 
$$\frac{3}{2}$$

(c) 
$$-\frac{3}{2}$$

(2) If 
$$a = 7^{x}$$
 and  $b = 7^{-x}$ , then  $a \times b = \dots$ 

(a) 
$$7^{2x}$$

(b) 
$$49^{2}$$
 x

(3) 
$$\frac{5^{x}}{5^{-y}} = \dots$$

(a) 
$$5^{x+y}$$
 (b)  $5^{x-y}$ 

(b) 
$$5^{x-y}$$

(c) 
$$5^{x+y}$$

$$(d) - \frac{x}{y}$$

(4) 
$$\square \frac{6 a^2 x^4}{2 a^3 x^3} = \cdots$$

(b) 
$$3 a^5 x^7$$

(c) 
$$\frac{3x}{a}$$

$$(d) \frac{3}{a x}$$

(5) 
$$\square \frac{(-2 s^2 t)^3}{(-4 s t^2)^2} = \cdots$$

$$(a) - \frac{s^3}{2t}$$

(b) 
$$-\frac{s^{4}}{2t}$$

(c) 
$$\frac{s^5}{2t^2}$$

$$(d) \frac{s^4}{t}$$

(6) 
$$\left( \frac{m^2}{n^{-3}} \right)^{-1} \left( \frac{3 m^{-2}}{n^{-2}} \right)^{-2} = \dots$$

(a) 
$$\frac{9 \text{ m}^2}{\text{n}^7}$$
 (b)  $\frac{\text{m}^2}{9 \text{ n}^7}$ 

(b) 
$$\frac{m^2}{9 n^7}$$

(c) 
$$\frac{\text{m}^2}{9 \text{ n}}$$

$$(d) \frac{9 \text{ m}^6}{n}$$

(7) 
$$\square \frac{(2 \text{ a b}^{-2})^0}{3^0 \text{ a}^{-2} \text{ b}} = \cdots$$

(a) 
$$\frac{a^3}{3b^3}$$
 (b)  $a^2$  (c) 1

(b) 
$$a^2$$

(d) 
$$\frac{a^2}{b}$$

(8) If 
$$a^{x} = 2$$
 and  $a^{-y} = 3$ , then  $a^{x-y} = \dots$ 

$$(b) - 1$$

(c) 
$$\frac{2}{3}$$

(9) If  $x y^{-1} = \frac{1}{2}$ , then  $\frac{y}{x} = \dots$ 

(a) 
$$\frac{1}{2}$$

(b) 
$$-\frac{1}{2}$$

(10)  $3^{-1} + 3^{-1} + 3^{-1} = \cdots$ 

(a) 
$$3^{-3}$$
 (b)  $3^3$ 

(b) 
$$3^3$$

(c) 
$$9^{-3}$$

(11) The multiplicative inverse of 5<sup>-1</sup> is ......

(a) 
$$\frac{1}{5}$$

$$(c) - 5$$

(d) 
$$-\frac{1}{5}$$

 $(2)(\frac{3}{5})^2 \times (\frac{5}{3})^{-2} = \cdots$ 

(a) 
$$\left(\frac{3}{5}\right)^4$$

(c) 
$$(\frac{3}{5})^{-4}$$

8 Complete each of the following by the suitable sign of (>), (<) or (=):

$$(4)(-7)^{-2}\cdots\cdots(-7)^{15}$$

(4) 
$$(-7)^{-2}$$
 .....  $(-7)^{19}$  (5)  $(-1)^{-6}$  .....  $(-1)^{-9}$ 

9 Why is not  $b^{-3}$  defined when b = 0?

Calculate the value of  $\left(-\frac{3}{5}\right)^x \times \left(\frac{3}{5}\right)^y$  in each of the following cases:

(1) 
$$X = -2$$
 and  $y = 2$ 

(2) 
$$X = -1$$
 and  $y = 2$ 

$$\left( -\frac{3}{5} \right)$$

If:  $x = -\frac{1}{3}$ ,  $y = \frac{2}{3}$ , then find in the simplest form the numerical value of the

expression: 
$$\left(\frac{y}{x^2}\right)^{-2}$$

 $\frac{1}{36}$ »



#### Life Applications

12 The flea can jump at a height of 200 times of its length. If a flea of length 2<sup>-4</sup> inches can jump at a height of 2<sup>3</sup> inches, what does this height represent according to the length of the flea?



13 The population of a city has been growing exponentially. It is estimated that in (t) years the population (p) will be :  $p = 2 (1.03)^t$  million.

(1) What will the population be in 2 years?

(2) What is the population now?

(3) What was the population last year?

16

ا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع العمل الاحدادي مواقع العمل الاحدادي مواقع العمل الاحدادي مواقع العمل الاحدادي العمل العمدادي العمل العمدادي العمل العمدادي العمل العمدادي العمدادي

Lesson Three



#### For excellent pupils

14 Simplify to the simplest form:  $\frac{2^{10} \times 3^4}{(12)^5}$ 

 $\ll \frac{1}{3} \gg$ 

15 Simplify to the simplest form:

$$\frac{6^{2 n+1} \times 4^{-n}}{2^{n} \times 3^{2 n+1}}$$
, then find the value of the result when  $n=3$ 

 $\ll \frac{1}{4} \gg$ 

16 If  $2^n = 3$ , find the value of:

$$(1) 2^{n+1}$$

and the second

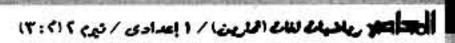
(4) 
$$2^{n-1}$$
 «6,9, $\frac{1}{9}$ , $\frac{3}{2}$ »

17 If 
$$a = 5$$
 and  $b = 5^{-1}$ , find the value of:  $a^{51}$   $b^{50}$ 

«5»

Without finding the result, arrange the following ascendingly by inspection:

$$(-2)^{-15}$$
,  $(-5)^{20}$ ,  $(-2)^{15}$ ,  $2^{-20}$ ,  $(-5)^{15}$ ,  $(-2)^{20}$ 



ه الأعدادي مرتع الكرال الكليبي

Lesson Four

11 Put the suitable sign (<) or (>):

(1) 
$$6.4 \times 10^3$$
  $4.6 \times 10^3$ 

(3) 
$$0.0041$$
  $3.2 \times 10^{-2}$ 

(5) 
$$2.10 \times 10^{-5}$$
  $1.82 \times 10^{-5}$ 

(7) 
$$6.920 \times 10^5$$
 96230

(2) 
$$6.2 \times 10^4$$
  $4.1 \times 10^5$ 

(4) 4370 
$$\boxed{\phantom{0}}$$
 3.41 × 10<sup>4</sup>

(6) 
$$9.1 \times 10^{-4}$$
  $1.2 \times 10^{-5}$ 

(8) 
$$3.69 \times 10^{-4}$$
  $\boxed{\phantom{0}}$  0.0000623

12 Arrange the following numbers in a descending order:

$$3.6 \times 10^{-3}$$
,  $5.2 \times 10^{-5}$ ,  $1 \times 10^{-2}$ ,  $8.35 \times 10^{-2}$ ,  $6.08 \times 10^{-8}$ 

13 Choose the correct answer from those given :

(1) 
$$3.04 \times 10^7 = \cdots$$

- (a) 340 000
- (b) 304 000
- (c) 3 400 000
- (d) 30 400 000

(2)  $\square$  2.37 × 10<sup>-4</sup> = ......

- (a) 0.00237
- (b) 0.000237
- (c) 23700
- (d) 0.0000237

(3) If 0.00079 = 7.9 a, then  $a = \dots$ 

- (a)  $10^{-1}$
- (b)  $10^{-3}$
- (c)  $10^{-4}$
- (d)  $10^4$

(4) If  $0.0000503 = m \times 10^{-5}$ , then  $m = \dots$ 

- (a) 503
- (b) 5.03
- (c) 50.3
- (d) 0.503

(5) III If the thickness of a sheet of paper is 0.012 cm., then a ream of 400 sheets is of height .....

- (a)  $48 \times 10^{-3}$  cm. (b)  $48 \times 10^{-2}$  cm.
  - (c)  $4.8 \times 10^{0}$  cm.
- (d) 48 cm.

(6) Which of the following equals  $\frac{1}{2}$  milliard?

- (a)  $50 \times 10^8$
- (b)  $5 \times 10^8$
- (c)  $0.5 \times 10^8$
- (d)  $500 \times 10^7$

(7) Which of the following is the greatest?

- (a)  $6.3 \times 10^5$
- (b)  $9.8 \times 10^4$
- (c)  $5.2 \times 10^5$
- (d)  $7.3 \times 10^4$

(8) Which of the following is the smallest?

- (a)  $0.6 \times 10^5$
- (b)  $0.25 \times 10^5$
- (c)  $7 \times 10^4$
- (d)  $17.5 \times 10^4$

(9) 6 000 × 50 = ·······

- (a)  $300 \times 10^2$
- (b)  $30 \times 10^5$
- (c)  $3 \times 10^5$
- (d)  $30 \times 10^4$

 $(10) 45 \times 900 = \dots$ 

- (a)  $4.05 \times 10^2$
- (b)  $4.05 \times 10^3$
- (c)  $4.05 \times 10^4$
- (d)  $45 \times 10^2$

 $(11) 0.7 \times 0.005 =$ 

- (a)  $3.5 \times 10^3$
- (b)  $3.5 \times 10^{-2}$
- (c)  $3.5 \times 10^2$
- (d)  $3.5 \times 10^{-3}$

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

#### 14 Write the result of each of the following in the standard form:

- (1)  $(6.4 \times 10^8) \times (1.5 \times 10^5)$
- (3)  $(5.02 \times 10^{-4}) \times (0.1 \times 10^{-3})$
- (5)  $\square$  (3.8 × 10<sup>8</sup>) ÷ (1.9 × 10<sup>6</sup>)
- (7)  $(8.8 \times 10^{25}) \div (8.8 \times 10^{22})$

#### 15 Write the result of each of the following in the standard form:

- (3)  $\square$  (5.3 × 10<sup>8</sup>) (0.8 × 10<sup>7</sup>)

- (2)  $(8.2 \times 10^7) \times (2.1 \times 10^{-4})$
- (4)  $(4.4 \times 10^3) \times (2 \times 10)^5$
- **(6)**  $(125.5 \times 10^{-3}) \div (5 \times 10^{4})$

(4)  $(2.65 \times 10^{-2}) - (6.34 \times 10^{-3})$ 

(8)  $(5 \times 10)^4 \div (2.5 \times 10^{-3})$ 

## $(2)(4.54 \times 10^4) + (3.76 \times 10^3)$

- (1)  $\square$  (3.8 × 10<sup>5</sup>) + (4.6 × 10<sup>4</sup>)
- [16] Write the result of each of the following in the standard form:

(2) 400  $\times$  0.00007

 $(5)(20000)^3$ 

- $(3)8000 \div 0.004$
- $(6)(0.002)^2$

#### 17 Find the value of n in each of the following:

(1)  $800\ 000 = 8 \times 10^{n}$ 

(1) 5000 × 3000

 $(7)(0.1)^{-8}$ 

 $(4) 0.000033 \div 500$ 

- (3)  $0.00052 = 5.2 \times 10^{n}$
- (5)  $\square$   $(0.004)^2 = 1.6 \times 10^n$

- (2)  $\square$  0.000000006 = 6 × 10<sup>n</sup>
- (4)  $\square$  0.000357 = 3.57 × 10<sup>n</sup>
- (6)  $76293 = n \times 10^4$

## Life Applications

#### 18 If the diameter of the Earth equals $1.27 \times 10^4$ km. long and the length of the diameter of Mars is $6.79 \times 10^3$ km. Which of the two planets is the greater and what is the difference between the two diameter lengths in the standard form?

- 19 If light travels at a speed of  $3 \times 10^8$  m/s.:
  - (a) Calculate the distance from the Sun to the Earth if you know that the light of the Sun takes 8 minutes to reach the Earth.
  - (b) If the distance between planet Venus and the Sun is 108 million kilometres, calculate the elapsed time (in minutes) that light takes to reach Venus from the Sun.

## For excellent pupils

# Find the result of the following in the standard form : $\frac{9.02 \times 10^3 + 4.98 \times 10^4}{2.5 \times 10^{-5}}$

#### 21 Without using the calculator, write each of the following numbers in the standard form:

- (1)  $10^{29} 10^{28}$
- (2)  $2^{19} \times 5^{15}$

If 
$$X = 5 + (3 \times 10) + (4 \times 10^2) + (6 \times 10^3) + (9 \times 10^4) + (4 \times 10^5) + (2 \times 10^6)$$
  
Write X in the standard form without using the calculator.

Lesson Five

III From the school book

#### Exercise 5 On order of mathematical operations

(2)  $18 \div (9-6) \times (1+2)$ 

(5)  $(7-4) \times 2 \div (5-3)$ 

(B)  $\square$  12 (2<sup>2</sup>) ÷ 24 + 3<sup>2</sup>

1 Calculate the value of each of the following:

$$(1)$$
 3 + 12 ÷ 6

$$(2) - 5 + 2 \times 3$$

(3) 
$$\square 2 \times 6 - 4 \div 2$$

(4) 
$$\square 4 \times 7 - 3^2$$

(5) 
$$\square 4 \times 2^3 - 20$$
 (6)  $\square 9 + 4 \times 3^2$  (7)  $\square 144 - 8 \div 2^3$ 

(6) 
$$\square$$
 9 + 4 × 3<sup>2</sup>

7) 
$$\square$$
 144 – 8 ÷ 2<sup>3</sup>

(1) 
$$\square$$
 196 ÷  $(7-5)^2$ 

(4) 
$$10 \times 4 - (2 \times 6 - 8)$$

(7) 
$$\square$$
 7 (6<sup>2</sup> ÷ 2 × 3)

(10) 
$$9 \times 10 + 20 \div 2 - 3$$

(11) 
$$6 + 9 \div 3 + 2 \times 3^2 + 11 - 8$$

(12) 
$$6-5+72 \div 9+24 \div 2^3+4 \times 1+10 \times 1+5$$

(3) 
$$20 \div 5 + 8 - (4 - 1)$$

(6) 
$$(30-6) \div 6 \times 30 \div 3$$

(9) 
$$\square$$
 9 (4)<sup>2</sup> ÷ 2<sup>2</sup> × 3

#### 3 Calculate the value of each of the following:

(1) 
$$\square 2 - [(7-3)-2]$$

(3) 
$$\square$$
 3 +  $[5 + 2(8 \div 4)]$ 

(5) 
$$[(2+23-7)\times 2] \div 4$$

$$(7)(26+1) \div [3(4-3)]$$

(9) 
$$2 + 3 [4 + (6 \times 3 - 8)] \times 2$$

(1) 
$$\square$$
 5  $\lceil (2^2-1)-(2^2-2) \rceil$ 

(2) 
$$\square$$
  $[4-(5-2)]-1$ 

(4) 
$$\square 2^3 + [4 + (2-1)]$$

(6) 
$$10 \times 3 \div [4 - (9 - 8)]$$

(8) 
$$(15 \times 2) \div [5 - (9 - 7)]$$

(10) 
$$\square$$
 2  $[(5^2+1)-(4^2-1)]$ 

$$(12) 6 \div 3 + [7 + 20 \div (6 - 2^2)]$$

#### 4 Calculate the value of each of the following:

(1) 
$$[-6 \div (-3)] \times [-30 \div (-3)]$$

(3) 
$$7 - [10 - (-8)] - 3$$

(5) 
$$2 \div (-1) - (-4)^2$$

$$(2)(-10+3) \div (-8+7)$$

(4) 
$$[(11 - (-10)] \times 2 \div (-6)$$

$$(6) - 6 - [-2 - 5]^2$$

#### 5 Calculate the value of each of the following:

(1) 
$$\square \frac{15+7}{15-4}$$

$$(4) \frac{1+15}{8-(2-2)}$$

$$(3)$$
  $\frac{5^2-5\times2}{(15+3)\div6}$ 

(2) 
$$\square \frac{8+20-4}{8-4}$$

(5) 
$$\frac{11-(5-4)}{1+4}$$

(3) 
$$\frac{5^2 - 5 \times 2}{(15 + 3) \div 6}$$
 (8) (1)  $\frac{5 + 2 \times 5}{2^2 + 1} + 5^2 - 5$ 

(3) 
$$\frac{-4 \times (-10)}{-9 + 7}$$

(6) 
$$(3-1)^3 + \frac{7 \times 3}{-1-6} - \frac{2 \times 15}{6}$$

(9) 
$$\frac{3^2 \times 6 \div 3}{2 \times 1 + (3+1)^2}$$

6 Calculate the value of each of the following:

(1) 
$$\left(\frac{3}{2} \times 3\frac{1}{2}\right) \div \left(\frac{6}{5} - 1\right)$$

(3) 
$$16 + 4 \div 2 - 3 \times 10^{-2}$$

(2) 
$$\square$$
 15 ÷  $\frac{1}{3} - \frac{3}{4} \times 10^3 + 27$ 

(4) 
$$9 \div \frac{1}{2} \times 2 - 3 \div \frac{1}{5}$$

If 
$$x = 3$$
, what is the numerical value of the expression:  $2\left(\frac{5x+3}{4x-3}\right)$  «4»

**8**  $\square$  Evaluate the expressions when t = 2 and s = 5:

$$(1) (t + s)^2$$

(2) 
$$(s-t)^3$$

$$(3)\left(\frac{s}{t}\right)^3$$

(4) 
$$\frac{6^2}{s-1}$$

$$(5) \frac{s-t}{s^3}$$

(6) 
$$\frac{12}{4 s^2}$$

9 Evaluate: 
$$16 t \div (4 s) + 3 st$$
, for  $t = 9$  and  $s = 6$ 

« 168 »

10 If 
$$x = 4(5 + 6) - 6$$
 and  $y = 9(36 \div 12) \div 3$ , find the value of the expression :  $2x + 4y$ 

« 112 »

If 
$$x = 3(5+7) - 4$$
 and  $y = 4(8+2) \div 5$ ,  
find the numerical value of the expression :  $x - 4y$ 

« zero »

If 
$$x = 18 - 4 \times 2 \div 2 + 1$$
 and  $y = 8 + 9 \times 3 - 4^2 + 11$ , find the numerical value of the expression :  $(\frac{y}{x})^{-3}$ 

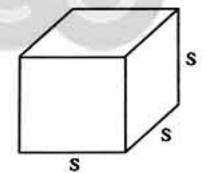
#### **Geometric Applications**

13 In the opposite figure :

The total area of a cube is  $T = 6 s^2$ , find T when:

(1) 
$$s = 3 m$$
.

(2) 
$$s = 0.8 \text{ cm}$$
.



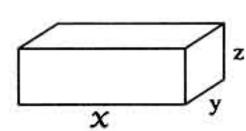
 $\times$  54 m.<sup>2</sup> , 3.84 cm.<sup>2</sup> »

14 In the opposite figure:

The total area of a cuboid is T = 2 (X y + y z + z X) find T when:

(1) 
$$X = 2$$
 cm.,  $y = 3$  cm. and  $z = 5$  cm.

(2) 
$$X = \frac{3}{5}$$
 m.,  $y = 0.4$  m. and  $z = \frac{1}{5}$  m.



« 62 cm<sup>2</sup> , 
$$\frac{22}{25}$$
 m<sup>2</sup> »

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى

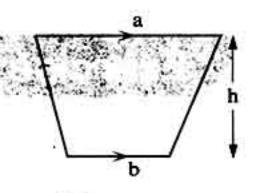
Lesson Five

#### 15 In the opposite figure :

The area of a trapezium

is 
$$A = \frac{1}{2}h(a+b)$$
, find A when:

- (1) h = 2 metres  $a = \frac{3}{4}$  metre and  $b = \frac{1}{4}$  metre.
- (2) h = 4 metres,  $a = \frac{1}{2}$  metre and  $b = \frac{1}{2}$  metre.



 $\ll 1 \text{ m.}^2 \cdot 2 \text{ m.}^2 \times$ 



#### For excellent pupils

16 Rewrite each of the following mathematical statements after putting the parentheses in the places which make them true:

(1) 
$$3 + 96 \div 12 \times 4 = 5$$

(a) 
$$3 + 96 \div 12 \times 4 = 35$$

(3) 
$$3 + 96 \div 12 \times 4 = 33$$



III From the school book

#### 6 On the square root of a perfect square rational number Exercise

#### Find each of the following:

(5) (1) 
$$\sqrt{\frac{9}{49}}$$

$$9\sqrt{6\frac{1}{4}}$$

(13) 
$$\square \sqrt{(\frac{81}{100})^2}$$

(17) 
$$\square$$
  $-\sqrt{\frac{49 \text{ a}^4}{25 \text{ b}^6}}$ 

**(6)** 
$$\square$$
  $-\sqrt{\frac{64}{25}}$ 

$$1\frac{11}{25}$$

$$(14)\sqrt{(-\frac{3}{4})^2}$$

**(18)** 
$$\Box = \sqrt{\frac{16 \, b^8}{121 \, h^2}}$$

(3) 
$$\pm \sqrt{2500}$$

(1) 
$$\square - \sqrt{4^2}$$

**(15)** 
$$\pm \sqrt{\frac{576}{1225}}$$

(19) (11) 
$$\sqrt{\frac{49 a^4 b^2}{9}}$$

(4) 
$$\Box$$
  $\pm \sqrt{40000}$ 

(12) 
$$\square = \pm \sqrt{8^2}$$

**(16)** 
$$-\sqrt{\frac{2.5}{40}}$$

**20** 
$$\square \sqrt{\frac{25 \times^2 y^2}{36}}$$

#### 2 Find the two square roots of each of the following numbers:

(3) 
$$\frac{9}{25}$$

(4) 
$$6\frac{1}{4}$$

#### 3 Find each of the following:

$$(1)\sqrt{9}+\sqrt{16}$$

(2) 
$$\sqrt{36+64}$$

$$(4) - \sqrt{225 - 81}$$

(5) 
$$\sqrt{3^2+4^2}$$

(6) 
$$-\sqrt{(10)^2-8^2}$$

$$\sqrt{\frac{9}{16}} + 1$$

**B** 
$$-\sqrt{\frac{1}{4}\left(1-\frac{3}{4}\right)}$$

(9) 
$$\sqrt{\frac{5^4 \times 5^3}{5^5}}$$

$$\sqrt{(\frac{1}{2})^2 \div (\frac{1}{5})^2}$$

$$\sqrt{(\frac{1}{2})^4 \times (\frac{1}{3})^4}$$

(2) 
$$\sqrt{(\frac{1}{4})^2 \times (\frac{1}{4})^3}$$

#### 4 Complete the following:

$$(1)\frac{3}{4} \times \sqrt{\frac{16}{9}} = \dots$$

(3) 
$$\sqrt{\frac{9}{4}} - \frac{3}{2} + \left(\frac{3}{2}\right)^{\text{zero}} = \dots$$

$$(5)\sqrt{(81)^2-81\times2+1}=\cdots$$

$$\sqrt{\frac{81}{49}} \times \frac{14}{27} = \cdots$$

**4** 
$$\sqrt{36} + \sqrt{16} = \sqrt{\dots}$$

Lesson Six

(6) The multiplicative inverse of  $\sqrt{\frac{4}{25}}$  in the simplest form equals ..........

7) The multiplicative inverse of  $\sqrt{0.49}$  in the simplest form equals .........

(8)  $\square$  The multiplicative inverse of the rational number  $\sqrt{\frac{10}{2.5}}$  equals .........

(9) The additive inverse of the number  $-\sqrt{\frac{9}{16}}$  in the simplest form equals .........

(10) The rational number  $6\frac{1}{4}$  in the form  $\left(\frac{a}{b}\right)^2$  is .......

(1) 
$$\sqrt{\frac{25}{64}} = \sqrt{\left(\frac{\dots}{1}\right)^2} = \dots$$

(12)  $\sqrt{(-3)^2} = \cdots$ 

(13)  $\sqrt{a^4b^8} = \cdots$ 

(14) If  $a = \sqrt{\frac{1}{4}}$  and b = 2, then  $ab = \dots$ 

(15) If  $a = -\frac{1}{2}$  and  $b = -\frac{9}{8}$ , then  $\sqrt{ab} = \dots$  (16) If  $2x = \sqrt{36}$ , then  $x = \dots$ 

(17) If a = 0.000625, then  $\sqrt{a} = 2.5 \times 10^{-10}$ 

 $(18)\sqrt{(2009)^2 + 2(2009) \times 213 + (213)^2} = \dots$ 

#### 5 Choose the correct answer from those given :

(1)  $\sqrt{1\frac{9}{16}} = \cdots$ 

(a)  $1\frac{3}{4}$  (b)  $-1\frac{3}{4}$ 

(c)  $1\frac{1}{4}$ 

(d)  $-1\frac{1}{4}$ 

(2)  $\square \sqrt{10^2 - 6^2} = \dots$ 

(a) 4

(b) 8

 $(c) \pm 4$ 

 $(d) \pm 8$ 

(3) √18×10×10×18 = ·········

(a) 18

(b) 180

(c) 10

(d) 100

(4)  $\sqrt{\sqrt{81}} = \dots$ 

(a) 81

(b) 27

(c) 9

(d)3

(5)  $\sqrt{2^2 + \sqrt{25}} = \dots$ 

(a) 3

(b) - 3

(c) 9

(d) - 9

(6) If:  $\frac{x}{2} = \frac{8}{x}$ , then  $x = \dots$ 

(a) 4

(b) - 4

 $(c) \pm 4$ 

(d) 16

الم العدادى / تيم ؟ (٢) : ١٤ إعدادى / تيم ؟ (٢) : ١٤

(7) If: 
$$x = \sqrt{\frac{1}{4}}$$
, then  $x^3 = \dots$ 

- (a)  $\frac{3}{8}$
- (b)  $\frac{1}{8}$
- (c)  $\frac{1}{16}$

(d)  $\frac{1}{64}$ 

(8) 
$$\sqrt{(a+b)^3(a+b)} = \cdots$$

- (a)  $(a + b)^2$  (b)  $a^4 + b^4$
- $(c) (a + b)^2$
- $(d) \pm (a + b)^2$

(9) 
$$\sqrt{1} + \sqrt{4} + \sqrt{9} + \sqrt{16} + \sqrt{25} + \sqrt{36} + \sqrt{49} + \sqrt{64} = \dots$$

- (a) 6
- (b)  $\sqrt{204}$
- (c)  $\sqrt{81}$

(d)  $6^2$ 

(10) The side length of the square whose area is 
$$16 \times 2^2 \text{ cm.}^2 = \dots$$
 cm.

- (a) 8 X
- (b) 4 X
- (c) 2 X

(d)  $8 X^2$ 

#### 6 Simplify each of the following to the simplest form:

(1)  $\left(-\frac{1}{2}\right)^3 \times \sqrt{\frac{64}{9}}$ 

- (2)  $\sqrt{\frac{49}{4}} \times (\frac{2}{7})^{\text{zero}} \times (-\frac{2}{7})^2$
- (3)  $\frac{2}{5} \times \sqrt{\frac{9}{16}} \div \left(-\frac{1}{2}\right)^3$

(4)  $\left(-\frac{1}{3}\right)^2 + \sqrt{\frac{64}{81}} - \left(\frac{3}{4}\right)^{\text{zero}}$ 

(5)  $\frac{3}{4} \times \left(-\frac{2}{3}\right)^3 \times \left(\frac{3}{\sqrt{4}}\right)^2$ 

(6)  $\sqrt{(\frac{25}{4})^2} \times (\frac{2}{5})^2$ 

#### Simplify each of the following to the simplest form:

(1)  $\sqrt{16} + \sqrt{25}$ 

- (2)  $\sqrt{16} + \sqrt{25}$
- (3)  $\sqrt{(\sqrt{16} + \sqrt{25})^2}$

8 Find two rational numbers lying between: 
$$\sqrt{\frac{4}{9}}$$
 and  $\frac{3}{4}$ 

- 9 Which is greater:  $\frac{3}{5}$  or  $\sqrt{\frac{4}{9}}$ ? Find the difference between them.
- 10 Which is smaller:  $\sqrt{2 \frac{1}{4}}$  or  $\left(-\frac{2}{3}\right)^2$ ? Find their difference.

#### 11 Find each of the following:

(1)  $\sqrt{5^2-2\times 5+1}$ 

(2)  $\sqrt{(\frac{1}{4})^2 - 2 \times \frac{1}{4} + 1}$ 

(3)  $\sqrt{20 \div 5 + 8 - (4 - 1)}$ 

- (4)  $\sqrt{8 \times (5+11) \div (2+6)}$
- (5)  $\sqrt{2 \times 8 + 10 3 + 12 + 11 \times 6 + 88 \div 2^3 + 99 \div 11}$
- (6)  $\sqrt{6+3\sqrt{100}} \sqrt{121}$

26

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمحسوس

Lesson Six

#### **Geometric Applications**

- Eind the length of  $\overline{XY}$  is a line segment where  $(XY)^2 = 25 \text{ cm}^2$ , E is the midpoint of  $\overline{XY}$ 
  - Find the length of: XE « 2.5 cm. »
  - (2)  $\square$  If:  $(AB)^2 = 144 \text{ cm.}^2$ ,  $(BC)^2 = 625 \text{ cm.}^2$  and  $B \in \overline{AC}$ Find the length of:  $\overline{AC}$  « 37 cm. »
  - (3) The area of a square is 0.49 cm. Find its perimeter. « 2.8 cm. »
  - (4) The area of a square is equal to the area of a triangle with base = 9 cm. long and its height = 8 cm. find the side length of the square. « 6 cm. »
  - (5) The area of a circle 154 cm. Calculate its radius length  $(\pi = \frac{22}{7})$  « 7 cm. »
  - (B) The area of a circle 78.5 cm. Calculate its diameter length ( $\pi = 3.14$ ) « 10 cm. »
  - (7) The area of a circle 616 cm. Calculate its circumference  $(\pi = \frac{22}{7})$  « 88 cm. »
  - Calculate the side length of the square.

    (a) (b) The length of a restangle is twice its width and its area is 24.5 cm<sup>2</sup>

(B)  $\square$  If three quarters of the area of a square is  $1\frac{11}{64}$  m<sup>2</sup>.

(9) The length of a rectangle is twice its width and its area is 24.5 cm<sup>2</sup>.

Calculate each of its width and length.

« 3.5 cm. » 7 cm. »

## For excellent pupils

If  $\frac{m}{n}$  is a rational number and  $\frac{m^2}{n^2} = 0.16$ , find the value of  $(\frac{m}{n})^3$  « ± 0.064 »

From the school book

#### On solving equations of the first degree in one unknown in ${\mathbb Q}$ Exercise

#### Find the solution set of each of the following equations:

(1) 
$$x-7=3$$
 where  $x \in \mathbb{N}$ 

(3) 
$$5 X = 20$$
 where  $X \in \mathbb{Q}$ 

(5) 
$$\square$$
 - 4 + y = 13 where y  $\in \mathbb{N}$ 

(7) 
$$X-7=0$$
 where  $X \in \mathbb{Z}$ 

(9) 
$$\square x - 6\frac{1}{4} = 12\frac{1}{2}$$
 where  $x \in \mathbb{Q}$ 

(2) 
$$\square X + 17 = 13$$
 where  $X \in \mathbb{N}$ 

(4) 
$$\frac{2}{5} x = \frac{1}{5}$$
 where  $x \in \mathbb{Q}$ 

(6) 
$$\square$$
 m - (-3) = 1 where m  $\in \mathbb{Z}$ 

**(8)** 
$$y - (-5) = -3$$
 where y ∈ ℚ

**10 □** 8.91 + 
$$x = 11.09$$
 where  $x ∈ \mathbb{Q}$ 

#### 2 Solve each of the following equations:

(1) 
$$2 \times -1 = 5$$
 where  $\times \in \mathbb{Q}$ 

(3) 
$$\square$$
 3  $X - 13 = 26$  where  $X \in \mathbb{N}$ 

(5) 
$$\square$$
 8 + 2  $x$  = 14 where  $x \in \mathbb{Z}$ 

(7) 
$$8-2 X=-2$$
 where  $X \in \mathbb{Z}$ 

(9) 
$$2 X + 3 X + 25 = 5$$
 where  $X \in \mathbb{Z}$ 

(2) 
$$\square$$
 8  $x$  + 4 = 12 where  $x \in \mathbb{Q}$ 

(4) 
$$2 \times + 14 = 14$$
 where  $\times \in \mathbb{N}$ 

(6) 
$$\square$$
  $\frac{5}{6}x-4=11$  where  $x \in \mathbb{Q}$ 

(8) 
$$2-5 X=0$$
 where  $X \in \mathbb{Q}$ 

(10) 
$$6x-2x+7=4$$
 where  $x \in \mathbb{Z}$ 

#### Solve each of the following equations in Q:

(1) 
$$2(x-3) = 4$$

(3) 
$$7(x-2)-3(x+1)=3$$

(5) 
$$\square$$
 4  $(X-1)-(X+3)=0$ 

(7) 
$$2(x-3) + 3(x-2) - 4x = -3$$

(2) 
$$3 \times 2 + 2 (5 \times 2 - 3) = 7$$

(4) 
$$\square$$
 3 (X + 2) + 7 (X - 1) = 12

(6) 
$$5(x-2) + 2(x+4) = -16$$

(B) (L) 
$$3y + 6(y + 3) - (8y - 16) = 60$$

#### 4 Find in Q the solution set of each of the following equations:

$$(1) 2 X + 5 = X + 9$$

(3) 
$$\square \square X + 3 = 18 - 3 X$$

(5) 
$$4(X+1) = 2(X-1)$$

(7) 
$$\square$$
 a + 5 a - 2 = 2 (3 - a)

(9) 
$$\frac{x+1}{3} = \frac{x-1}{4}$$

(2) 
$$\square$$
 5  $x-4=2x+11$ 

(4) 
$$3 X + 6 = 30 - 5 X$$

(6) 
$$3(x-2) = 5x-10$$

(B) 
$$\square 3(2X-8)-(2X+2)=X-3$$

(10) 
$$\frac{5}{4+4x} = \frac{3}{1-2x}$$

#### 5 Complete the following:

(1) If 
$$X + 5 = 7$$
, then  $X = \dots$ 

(2) 
$$\square$$
 If 3 t = 6, then the value of 6 t = ......

(3) If 
$$2 \times 2 = 5$$
, then the value of  $4 \times 2 = \dots$ 

(4) 
$$\coprod$$
 If  $X + 9 = 11$ , then the value of  $7X = \cdots$ 

Lesson Seven

(5)  $\square$  If 2 t + 3 = 15, then the value of  $\frac{1}{3}$  t = ........

(6)  $\square$  If  $Z - 1\frac{1}{4} = 5\frac{1}{2}$ , then the value of  $4Z - 18 = \dots$ 

(7)  $\square$  If  $\frac{P}{4} = \frac{2}{3}$ , then the value of  $\frac{P}{2} = \cdots$ 

(8) If the age of a man now is X years, then his age 5 years ago is .........

(9) If the age of a man now is y years, then his age after 4 years is .........

(10) If the age of a man after 5 years is X years, then his age now is .........

(11) If the age of Youssef after 4 years is X years, then his age 2 years ago is .........

(12) A rectangle with length equals triple its width. if the length = x cm. , then its width = ······ cm.

(13) The rectangle whose width = x cm. and its length is twice its width, then its perimeter = ······ cm.

(14) Two integers, their sum is 5, if one of them is x, then the other one is ........

(15) Two integers, the difference between them is 2, if the small one is X, then the great one is .....

#### 6 Choose the correct answer from those given :

(1) If  $2 \times 2 = 2$ , then  $3 \times -1 = \dots$ 

(a) 2

(b) 3

(c) 4

(d)5

(2) If  $2 \times 0$ , then  $\times = \dots$ 

(a) 2

(b) 3

(c) 5

(d) zero

(3) If 2 a b = 10, then  $3 a b = \dots$ 

(a) 5

(b) 6

(c) 15

(d) 30

(4) If 0.2 + a = 5, then  $\frac{a}{4} = \dots$ 

(a) 4.8

(b) 1.3

(c) 1.2

(d) 19.2

(a) 33

(b) 35

(c) 47

(d) 8 X

(6) The S.S. of the equation  $\frac{2a}{3} = 8 + 4a$  in  $\mathbb{Q}$  is ......

(a)  $\{-2.4\}$ 

(b)  $\{2.4\}$ 

(c)  $\{-3\frac{1}{3}\}$ 

(d)  $\{0\}$ 

(7) Which of the following equations is equivalent to the equation x + 3 = 12?

(a) X - 3 = -12

(b) X + (-3) = 12

(c) X - (-3) = 12

(d) X - (-3) = -12

(8) Which of the following equations is equivalent to the equation x - 12 = 15?

(a) X + 12 = -15

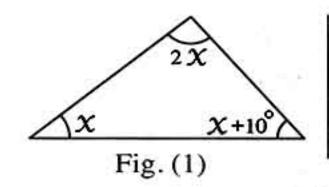
(b)  $\frac{1}{3}x - 4 = 5$ 

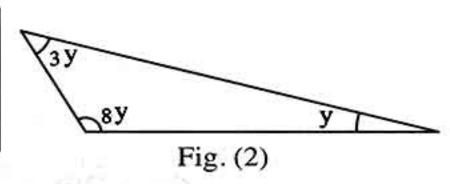
(c) X - 4 = -5

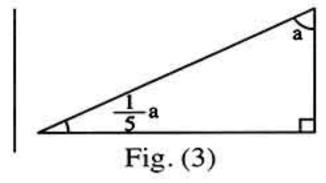
(d) X + 4 = 5

#### **Geometric Applications**

7 🕮 Find the measure of each angle in each of the following triangles :

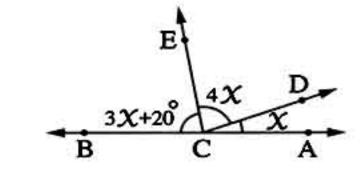






In the opposite figure:

If  $C \in \overrightarrow{AB}$ , find m ( $\angle$  DCE)



The length of a rectangle exceeds its width by 4 metres and its perimeter is 68 metres.

Find the dimensions of the rectangle.

« 19 m., 15 m.»

« 80° »

- The length of a rectangle decreases than the twice of its width by 4 cm., if its perimeter equals the perimeter of a square of side length 7 cm.

  Find the dimensions of the rectangle.

  « 6 cm., 8 cm.)
- 11 The length of a rectangle is twice its width. If the length decreases 5 cm. and the width increases 6 cm., then the rectangle becomes a square.

  Find the area of the rectangle.

  « 242 cm<sup>2</sup>, »

# Life Applications

- Two integers, the smaller number is 2 X and the greater number is 7 X, if the difference between them is 25, find the two integers.

  « 10,35 »
- Two natural numbers, one of them is twice the other and their sum is 108

  Find the two numbers.

  « 36,72 »
- The difference between two natural numbers is 5 and their sum is 21

  What are the two numbers?

  « 13,8 »
- Find the number that if it is added to its triple the result is 32 «8»

30

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Lesson Seven

- Find the number which if we subtract 9 from its triple, the result will be 6
- Three consecutive natural numbers whose sum is 213
  What are these numbers?

  « 70,71,72 »
- Find three consecutive odd numbers if their sum is 357 « 117, 119, 121 »
- 19 A man's age now is three times his son's age and after two years, the sum of their ages will be 52 years. What is the age of each now? « 12 years, 36 years »
- Three brothers, Amgad, Bassim and Ayman, the sum of their ages is 89 years.

  If Amgad was born before Bassim by 2 years and Bassim was born before Ayman by 6

  years, what is the age of each of them now?

  « 25 years, 31 years, 33 years »



21 Find in Q the S.S. of each of the following equations:

$$(1) \, 5 - \frac{6}{x} = -1$$

(2) 
$$-\frac{3}{5} + \frac{x}{10} = -\frac{1}{5} - \frac{x}{5}$$

22 Find in Q the S.S. of each of the following equations:

$$(1)(X+3)^2 - (X-2)^2 = 15$$

(2) 
$$(2 X + 3) (2 X - 1) - (2 X - 1)^2 = 14$$

- If the S.S. of the equation  $12 \times + 3 = 39$  in  $\mathbb{Q}$  equals the S.S. of the equation  $a \times 12 = a$  in  $\mathbb{Q}$ , find the value of a  $6 \times 6$
- If a + 1 is a solution of the equation  $(x + a)(x a) = x^2 ax + 3$  in  $\mathbb{Q}$ , find the value of a
- Three brothers were born in 1980, 1984 and 1986, the required is finding the year in which the sum of their ages became 41 years.

  « 1997 »

From the school book

#### 8 Exercise

#### On solving inequalities in $\mathbb Q$

 $\square$  Which number would you add to each side of the inequality to obtain X in one side of it?

$$(1) X + 5 > 9$$

$$(2) x - 4 < 6$$

(3) 
$$x - 7 < 3$$

$$(4) X + 9 > 12$$

(5) 
$$X - 1.5 \le 3.2$$

(6) 
$$4.8 \le X + 0.6$$

$$(7)$$
  $1\frac{1}{2} > x - 2\frac{1}{2}$ 

(7) 
$$1\frac{1}{2} > x - 2\frac{1}{2}$$
 (8)  $x + \frac{1}{3} > -\frac{1}{6}$ 

[2] Find the solution set of the inequality  $x + 3 \le 6$ , where:

(1) 
$$x \in \mathbb{Z}$$

then represent the solution set on the number line.

3 Find the solution set of the following inequalities in Q:

(1) 
$$X + 2 > 5$$

(2) 
$$\coprod x + 4 > 1$$

(3) 
$$\square$$
 y - 5 > 7

(4) 
$$\square$$
 19 < y + 14

$$(5)-1\geq X-3$$

(6) 
$$\square - 5\frac{1}{2} > a + 1\frac{1}{4}$$

$$(7) - 2 X < 12$$

$$\textcircled{B} \; \frac{2}{3} \; X \ge 1$$

(9) 
$$-\frac{1}{4} x \le \frac{1}{4}$$

4 Solve each of the following inequalities in Q:

$$(1) 3 x - 2 < 1$$

$$(2)2X+3<9$$

(3) 
$$4x + 2 \ge -10$$

(4) 
$$3x - 2 \ge 5$$

$$(5)3x-9<0$$

(6) 
$$1 + 2 \times \le -3$$

$$(7)9-6x<15$$

(B) 
$$2 - 3 \times 4$$

(9) 
$$\frac{3x-2}{5} \ge \frac{1}{2}$$

(10) 
$$\square$$
 8  $x - 3 x + 1 \le 29$ 

(11) 
$$\square 14n-2(n-1) \ge 0$$

(12) 
$$\square -3 m + 6 (m-4) > 9$$

5 Solve each of the following inequalities in Q:

(1) 
$$\square$$
 6 d + 1 ≤ 5 d - 3

(3) 
$$3x-2<5x-8$$

(5) 
$$5 X + 1 \ge 2 (X + 2)$$

(7) 
$$\square$$
 3  $(x+2) \ge -2(x+1)$ 

(9) 
$$\square$$
 3 (7 y  $-\frac{1}{3}$ )  $\leq$  20 y  $-1$ 

(11) 
$$\square 14-5(x-2) \le -2(-9+2x)$$

(13) 
$$\square$$
 1 - (4 d - 1) > 2 (d - 3)

(2) 
$$6 X + 2 \ge 14 + 5 X$$

$$(4)8-2X \le 5X$$

(6) 
$$\square$$
 3 (X + 2) <  $-$  X + 4

(8) 
$$2-3(X-5) \ge X+7$$

$$(10)\frac{x}{2} + 3 \le 2x + 1$$

(12) 
$$\square$$
 3 (y + 2) + 8 < 10 - (2 - y)

$$(14) x - 3 (2 x + 1) < 5 (1 + x) + 2$$

Find the S.S. of each of the following inequalities:

(1) 9 ≤ 4 
$$X$$
 + 1 ≤ 17,  $X$  ∈  $\mathbb{Z}$ 

(2) 
$$9 \le 3 \times + 2 < 12, \times \in \mathbb{Q}$$

(3) 
$$9 > x + 6 > 2$$
,  $x ∈ \mathbb{N}$ 

Lesson Eight

7		Complete	
---	--	----------	--

- (1) If X > y, then  $X + z \cdots y + z$
- (3) If X < y and y < z, then  $X < \cdots$
- (5) If a 3 < 0, then ..... > .....
- 7) If b < 0, then  $b + 3 \dots 3$
- (8) If X > y and z is positive (z > 0), then  $X z \cdots y z$
- (9) If X < y and z is negative (z < 0), then  $X z \cdots y z$

#### 8 Choose the correct answer from those given:

- (1) If: -x < 5, then ......
  - (a) X > 5
- (b) x > -5
- (c) X < 5
- (d) X < -5

(2) If X < y, then  $X + z \cdots y + z$ 

(6) If a + 5 > 0, then ..... > .....

(4) If z > y and y > X, then  $z > \cdots$ 

- (2) If  $X \in \mathbb{N}$ , then the S.S. of the inequality -X > 3 is .......

  - (a)  $\{4,5,\cdots\}$  (b)  $\{-4,-5,\cdots\}$  (c)  $\{-3\}$
- (d) Ø

- (3)  $\frac{x}{3}$  < 4 is equal to ......

  - (a)  $X > \frac{4}{3}$  (b)  $X < \frac{4}{3}$
- (c) X > 12
- (d) X < 12
- (4) If  $x \in \mathbb{Z}$ , then the S.S. of the inequality  $20 < 5 \times < 25$  is ......
  - (a)  $\{4\}$
- (b) {5}
- (c)  $\{4,5\}$
- (d) Ø
- (5) The S.S. of the inequality  $-2 \times < zero$  in  $\mathbb{Q}$  is ......
  - (a) Ø
- (b) Q<sub>+</sub>

- (c) Q
- (d) Z,
- (6) The number of solutions of the inequality  $\frac{1}{5} < x < \frac{2}{3}$ , where  $x \in \mathbb{Q}$  is .......
  - (a) zero

- (c) 2
- (d) an infinite number.
- (7) If X > y, then  $\frac{1}{x}$  ......  $\frac{1}{y}$ , where  $X \neq 0$ ,  $y \neq 0$ 
  - (a) >
- (b) <

- (c) =
- (d) ≥
- (8) The number 2 belongs to the S.S. of the inequality  $\cdots$  where x is an integer.
  - (a) X > 2
- (b) X < 2
- (c) -x > -3
- (d) x > 3

- (9) If X > 5, then -X.....
  - (a) < -9
- (b) ≥ -5
- (c) < -5
- (d) > -5

#### that a-c>b-d

- 10 Put (1) for the correct statement and (x) for the incorrect statement, when a statement is false, give an example that shows why it is false (given that x > y):

- (1) y < X ( ) 2x > 0 ( )  $3y^2 \ge 0$  ( )  $4y^2 > y$  ( ) (5) xy > 0 ( ) 6x + y > y ( )  $y^2 > x$  ( )  $y^2 > x$  ( )  $y^2 < xy$  ( ) (9)  $xy < x^2$  ( )  $x^3 < y^2$  ( )

33

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11 Hany wants to buy a pair of shoes and some shirts > if Hany has L.E. 200, the price of the pair of shoes is L.E. 70 and the price of one shirt is L.E. 40 What is the greatest number of shirts can Hany buy?



«3»



#### For excellent pupils

12 If the S.S. of the inequality  $a \le 3 x - 5 \le b$  in  $\mathbb{Q}$  is  $\{x : x \in \mathbb{Q}, 2 \le x \le 5\}$ , find the values of a and b «1,10»

13 If:  $-4 \le x \le 5$  and  $2 \le y \le 7$ , where  $x \in \mathbb{Q}$  and  $y \in \mathbb{Q}$ , find:

- (1) The greatest possible value of the expression X + y
- (2) The greatest possible value of the expression y X
- (3) The smallest possible value of the expression X y
- (4) The smallest possible value of the expression  $x^2 + y^2$

« 12 »

« 11 »

 $\sim -28$  »

« 0 »

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General excercises

#### General Exercises on Unit One "Numbers and Algebra"

#### First: Completion questions:

#### Complete the following:

(1) 
$$-3 \text{ a } \text{b}^2 \times 2 \text{ a}^2 \text{ b}^3 = \dots$$

(2) The additive inverse of 
$$\left(\frac{-2}{3}\right)^3$$
 is ......

(3) If: 
$$x = \frac{1}{4}$$
,  $y = \frac{1}{8}$ , then  $(x - y)^{-1} = \dots$ 

(4) 
$$3 \times 4 - 21 \div 7 = \cdots$$

$$(5)\sqrt{9+16} = \cdots$$

$$6)\sqrt{100-64} = \cdots$$

$$(7)\sqrt{10^2-6^2} = \cdots$$

(8) If we subtract twice the number 
$$x$$
 from 3, then the result is ........

(9) If: 
$$x + 9 = 11$$
, then  $7x = \dots$ 

(10) The S.S. of the equation: 
$$3x + 7 = 5$$
,  $x \in \mathbb{Q}$  is ......

(11) If: 
$$ac > bc$$
, then a ..... b (where  $c < 0$ )

#### Second: Multiple choice questions:

#### Choose the correct answer from those given:

$$(1) \frac{4 a^2 b^4}{2 a^3 b^3} = \dots$$

(b) 
$$2 a^5 b^7$$

(c) 
$$\frac{2b}{a}$$

$$(d) \frac{2}{ab}$$

(a) 2 a b (b) 2 
$$a^5 b^7$$
  
(2) If:  $a = b$ , then  $(\frac{3}{7})^{b-a} = \dots$ 

(c) 
$$\frac{3}{7}$$

(d) 
$$\frac{7}{3}$$

(3) 
$$2^4 \times 3^4 = \dots$$

(a) 
$$5^4$$

(b) 
$$6^4$$

(c) 
$$6^8$$

(d) 
$$6^{16}$$

**(4)** 
$$2^7 \times 3^7 = \cdots$$

(a) 
$$5^7$$

(b) 
$$6^7$$

(c) 
$$6^{14}$$

(d) 
$$6^{49}$$

(a) 
$$4^5$$

(b) 
$$4^{10}$$

(c) 
$$4^{19}$$

(d) 
$$2^{10}$$

(6) 
$$3^{10} + 3^{10} + 3^{10} = \dots$$

(a) 
$$3^{10}$$

(b) 
$$3^{11}$$

(c) 
$$3^{20}$$

(d) 
$$3^{30}$$

$$(7) 7.35 \times 10^{-4} = \cdots$$

Unit

- (8) Which of the following is the smallest number?
  - (a)  $314 \times 10^3$
- (b)  $3.14 \times 10^4$
- (c)  $31.4 \times 10^5$
- (d)  $0.314 \times 10^6$

- (9) If: x = 0.0009, then  $\sqrt{x} = \dots$ 
  - (a) 0.0003
- (b) 0.0081
- (c) 0.003
- (d) 0.03

- $(10)\sqrt{\left(-\frac{2}{3}\right)^2} = \cdots$ 
  - (a)  $\frac{-4}{9}$
- (b)  $\frac{-2}{3}$

- (c)  $\frac{2}{3}$
- (d)  $\frac{4}{9}$

- (11) If: -x < 3, then ......
  - (a) X > 3
- (b) X > -3
- (c) X < 3
- (d) X < -3
- (12) The age of Amer now is X years, then his age 5 years ago is .........
  - (a) 5 X
- (b) 5 + x
- (c) 5 X
- (d) X 5

#### Third: Essay questions

- Find the value of the following expression in the simplest form:  $\frac{5^{-2} \times 5^{5}}{5^{3}}$
- Put the following expression in the simplest form :  $\frac{7^{-3} \times 7^5}{7^2}$
- Put the expression :  $\left(\frac{1}{2}\right)^2 \times \left(-\frac{1}{2}\right)^3$  in the simplest form.
- 4 If:  $x = \frac{-3}{2}$ ,  $y = \frac{-4}{3}$ , find in the simplest form:  $\left(\frac{x}{y}\right)^2$
- If:  $x = \frac{-1}{2}$ ,  $y = \frac{3}{4}$ , find the numerical value of the expression:  $(\frac{y}{x^2})^{-2}$  in the simplest form.
- 6 If:  $300000 = 3 \times 10^{x}$  find the value of: x
- Find the solution set of the following inequality in  $\mathbb{Q}: 4x + 7 \le 3$
- Find in  $\mathbb{Z}$  the S.S. of the inequality:  $3-2 \times \ge 1$ , then represent it on the number line.
- **9** Find the S.S. of the following inequality in  $\mathbb{Q}: 1 < x 3 \le 6$
- 10 Three even consecutive numbers their sum is 204. Find these numbers.
- A man's age now is three times his son's age, and after two years, the sum of their ages will be 52 years. What is the age of each now?
- The length of a rectangle is twice its width. If the length decreases by 5 cm. and the width increases by 6 cm., the rectangle becomes a square. Find the area of the rectangle.

# Unit (2)

# Statistics and Probability

Lesson One : Samples :

- Systematic sample.
- Random sample.

Lesson Two: Probability:

- Experimental probability.
- Theoretical probability.

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III From the school book

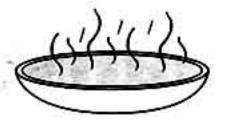
## Exercise

#### On samples

- 1 A factory's canteen service wanted to find the preferences of their 427 employees during their 15 - minute break. Each employee was given a number from 1 to 427 A 10% sample of the 427 were to be surveyed and asked to select a preference from:
  - Hot beverage.
  - Hot soup with bread.
  - · Cold drink with biscuits.
  - · Fruit with fresh water.

The sample were determined by selecting 43 sample numbers in the range using calculator. Identify the sample numbers using a calculator.









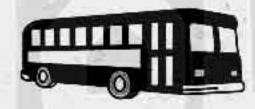




2 A school makes a study about how the pupils come to school. If the number of pupils in the school is 320, each pupil is given a number from 1 to 320 A sample of 10% from this number is selected as a sample to ask them how they come to school:



On foot



Public transport



Taxi





Private car

determine the number of the sample using the calculator.

- 3 A company makes a study about the best places which the workers in the company prefer to spend their annual holiday among:
  - Port Said
- Alexandria
- Matrouh

- The North Coast
- Ismailia

If the number of the workers in the company is 250 workers and a sample of 10% from the number of workers is selected to make a survey on it,

determine the numbers of the sample using the calculator.



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Lesson One

- 4 It is noticed that 230 persons use a public bus daily and the public transport authority wanted to collect some informations concerning with the using daily of this service. It is necessary to form a random sample representing 10% from the users of this bus to make a survey on them. Determine the numbers of this sample using the calculator.
- 5 A sports survey was to be carried out among 318 students in a district to help decide on the type of entertaining services which would satisfy community youth needs. Each student was given a number from 1 to 318

A sample of 10% of the 318 were to be surveyed and asked to select a preference from:

- Outdoor team games.
- Individual competitions. · Indoor games.

Determine the sample by selecting 31 sample numbers using the Excel programme described in the activity at the end of the book.

- 6 A construction company wanted to ask their 362 workers about (on site) safety measures in terms of:
  - Safety of emergency exit.
  - Scaffold erection and maintenance.
  - Rescue means positioning.

They asked 12% (to the nearest whole number) of their workforce with employment numbers from 20 to 382 to give their opinions. The employment numbers of the 12% were identified by using a computer programme. Use a computer programme to identify the target employment numbers for the survey.

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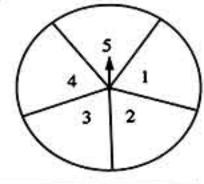
From the school book

## Exercise 10

#### On probability

#### First Problems on experimental probability

In the experiment of spinning game, roll the disc 50 times. In each time, record the number at which the pointer stops in the following table:



	1	2	3	156H 1511 15 4	5	Total
The tally sign	4					
Frequency		Da.				50

Calculate: (1) The probability that: The pointer stops at the number 2

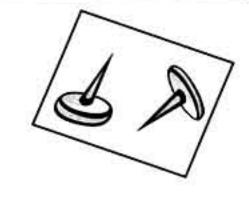
(2) The probability that: The pointer stops at the number 5

- (a) Draw six parallel lines with a distance of 2 cm. between each of them on a A<sub>4</sub> sheet of paper:
  - (b) Bring a piece of wood of length 2 cm.
  - (c) Slightly toss the piece of wood in the air so that it falls from a suitable height on to the A<sub>4</sub> sheet.
  - (d) Repeat the trial 50 times.
  - (e) Record the number of times that the piece of wood falls across the line and also between the lines.

a car garaga	Across	Between	Total
Tally			
Frequency			50

- (f) Deduce the probability of the piece of wood falling between the lines.
- (a) Drop a drawing pin 100 times from a suitable height.
  - (b) Record the number of times it lands with its point up and its point down :

	Up	Down	Total
Tally			
Frequency			100



(c) Deduce the probability of the drawing pin landing point "UP" and point "Down"

40

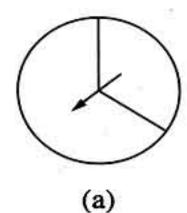
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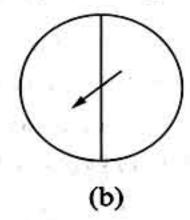
Lesson Two

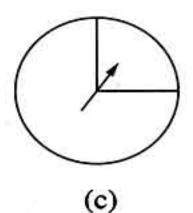
#### 4 In the spinner game :

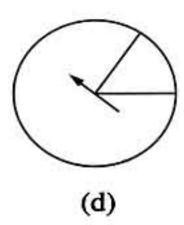
The disc is divided into two unequal parts X and Y The Pointer is rolled 800 times. It stands 197 times at the X-zone

In which of the following figures the pointer points to X-zone?









#### Second Problems on theoretical probability

- 1 As throwing a fair die and observing the upper face , complete the following :
  - (1) The probability of appearance a number greater than 2 = ......
  - (2) The probability of appearance a number less than 3 = .......
  - (3) The probability of appearance an even number = ......
  - (4) The probability of appearance the number 4 = ......
  - (5) The probability of appearance the number 7 = .......
  - (6) The probability of appearance a number less than or equal  $6 = \dots$
  - (7) The probability of appearance a prime number = ......
  - (8) The probability of appearance a prime even number = .......
  - (9) The probability of appearance a number divisible by 5 = .......
  - (10) The probability of appearance the number 5 or the number 6 = .......

#### 2 Complete the following:

- (1) The probability of occurring the impossible event = ......... and the probability of occurring the certain event = .........
- (2) If a coin is flipped once, then the probability of appearance of a head = .........
- (3) 10 cards numbered from 1 to 10. If a card is drawn randomly, then the probability that the card is numbered by an odd number = ........
- (4) A box has 5 white balls , 7 red balls , 3 blue balls. If a ball is drawn randomly from the box , then the probability that the ball is blue = ........
- (5) In the experiment of throwing a fair die once and observing the upper face, the probability that the apparent number is less than 1 = .........
- (6) If one of the digits of the number 867742231 is selected randomly, then the probability that the selected number is even equals .........

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(7) A box contains 48 oranges and 4 oranges of them are bad. If an orange is drawn
randomly, then the probability that the drawn orange is bad = and the
probability that the orange is good =

- (8) If the probability of occurring an event is  $\frac{5}{8}$ , then the probability that the event doesn't occur = .....
- (9) An activity room has 3 doors numbered from 1 to 3. If a student went out using one of them , then the probability that the student went out using the door number 2 is .......
- (10) If the probability that a person get infected (in a city whose number of inhabitants 200000) with a disease is 0.003, then the expected number of infected persons with the disease in this city is ..... persons.

#### Choose the correct answer from those given :

(1) Which of the	following is the	probability of	occurrence of	an event?
------------------	------------------	----------------	---------------	-----------

(a) 1.2

(b) - 0.4

(c) 315%

(d) 75%

(2) As throwing a fair die once, the probability of appearance of a number greater than 4

(a)  $\frac{1}{6}$ 

(b)  $\frac{1}{3}$ 

(c)  $\frac{1}{2}$ 

(d) 1

(3) A basket contains cards numbered from 1 to 20 If a card is drawn randomly, what is the probability that the number written on it is divisible by 6?

(a)  $\frac{3}{20}$ 

(b)  $\frac{4}{20}$ 

(c)  $\frac{3}{20}$ 

(4) A bag has 5 red balls and 3 white balls. If the balls are similar and a person draws a ball randomly, then the probability that the drawn ball is white = .........

(a)  $\frac{3}{5}$ 

(5) A letter is selected randomly from the name "ZAMALEK". The probability of selecting the letter A is .....

(a)  $\frac{1}{7}$ 

(b)  $\frac{2}{7}$ 

(c)  $\frac{3}{7}$ 

(d)  $\frac{4}{7}$ 

(6) A Rashad is in grade 7 in a class of 36 students. 16 of them are girls. If a student is selected randomly from the class, what is the probability that the student is a boy?

(a)  $\frac{4}{9}$ 

(c)  $\frac{5}{9}$ 

(d)  $\frac{1}{36}$ 

(7) A class has 25 boys and 20 girls. A pupil of them is selected randomly, then the probability that the pupil is a girl = .....

(a)  $\frac{1}{20}$ 

(b) 4

(c)  $\frac{1}{25}$ 

(d)  $\frac{5}{9}$ 

(B) If a die is tossed once, then the probability of getting a number satisfying the inequality 2 < x < 3 equals ......

(a)  $\frac{1}{2}$ 

(b)  $\frac{1}{3}$ 

(c)  $\frac{1}{4}$ 

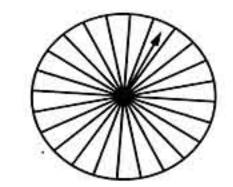
(d) zero

42

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

Lesson Two

(9) The opposite figure shows a spinner with 24 sectors. When someone spins the arrow it is likely equal to stop on any sector.  $\frac{1}{8}$  of sectors are blue,  $\frac{1}{3}$  are red,  $\frac{1}{2}$  are orange and  $\frac{1}{24}$  are purple. If a person spins the arrow, at which



(a) Blue.

(b) Purple.

colour of sector is the spinner least likely to stop?

(c) Orange.

(d) Red.

(10) If the probability of success of a student is 70%, then the probability of his failure = .....

(a) 0.7

(b) 0.07

(c) 0.3

(d) 0.03

A card is drawn from a bag of 25 cards numbered from 1 to 25 Calculate the probability that the drawn card carries:

(1) A number divisible by 5

(2) A number ≥ 20

(3) A perfect square number.

5 One card is selected randomly from 8 cards numbered from 1 to 8 Write down the sample space. Then find the probability of the following events:

(1) Getting an even number.

(2) Getting an odd number.

(3) Getting a number greater than or equal to 6

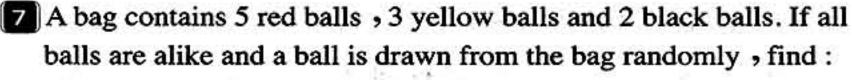
(4) Getting a number divisible by 3

6 A letter is selected randomly from the word "SAMEH" Calculate the probability of selecting the letter:

(1)S

(2)E

(3) R



- (1) The probability that the drawn ball is yellow.
- (2) The probability that the drawn ball is yellow or red.
- (3) The probability that the drawn ball is not yellow.



B A card is chosen randomly from ten cards numbered from 1 to 10. What is the probability that the selected card shows:

(1) An odd number.

(2) A prime number.

(3) An even number.

(4) An odd number greater than 3

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والعصوات

marbles of ther	n are drawn without r	eturning them to the bag	and the rest is red. If two and they were red. Then bability that the last marble
		of girls is less than the	
Choose the co	rrect answer from th	nose given :	
(1) A bowl cont	ains 32 coloured bea	ds. All beads are of the s	ame size. Some of them
are blue, s	ome are green, some	are red and the rest is y	ellow the probability of
drawing a b	lue bead is $\frac{3}{8}$ , how	many blue beads are in	the bowl?
(a) 4	(b) 8°	(c) 12	(d) 16
the bag, th	en the probability tha	t the drawn ball is not b	
(a) $\frac{1}{2}$	(b) $\frac{1}{3}$	(c) $\frac{2}{3}$	(d) $\frac{1}{6}$
	e . A ball is drawn ran	many and the contract of the c	the third is black and the bility that the drawn ball is (d) zero
20 yellow b		ty of drawing a yellow l	ow). If the box contains ball from the box randomly
(a) 5	(b) 25	(c) 60	(d) 80
a pupil who		equal to 13 is $\frac{1}{6}$ . What	e probability of choosing is the number of pupils
(a) 23	(b) 24	(c) 30	(d) 32
7:9. A stud	lent is selected rando ected student is a boy	mly from the pupils of the	ys to the number of girls is his school. The probability
(a) zero	(b) $\frac{7}{16}$	(c) $\frac{9}{16}$	(d) 7
A small tickets num	box contains 25 ticked bered from 1 to 50 wooxes. Which box wo	ithout looking at them,	25 A large box contains 50 a ticket is picked from one ce of picking a ticket with

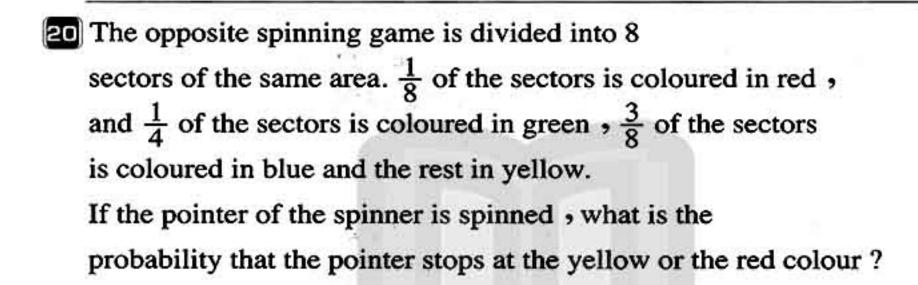
(a) The larger box.

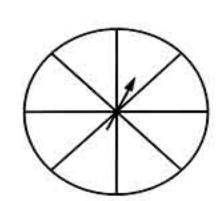
(b) The smaller box.

(c) Both would give the same chance.

(d) The given information is not enough.

- 19 The opposite figure represents the spinning game. Find:
  - (1) The probability that the pointer stops at.
    - (a) Red colour.
    - (b) Green colour.
    - (c) Yellow colour.
  - (2) The probability that the pointer does not stop at the red colour.





21 A class contains 40 students 30 of them succeeded in maths. 24 succeeded in science and 20 succeeded in both.

A student is chosen randomly. Find the probability that this student:

- (1) Succeeded in maths.
- (2) Succeeded in science.
- (3) Failed in science.
- (4) Failed in both maths and science.
- 22 Two players play in a football team. During training one of them shot 21 penalty kicks and he scored 18 goals and the other shot 32 penalty kicks and he scored 25 goals. which of them should you choose to shoot a penalty kick? Why?



- Maryam and Souad played together with two dice. If the product of the two apparent numbers on the upper face is even, then Souad wins the game. If the product of those numbers is odd , then Maryam wins :
  - (1) On your opinion, is this system of the game fair? Why?
  - (2) If it is not fair, determine which one of the two girls has the greater chance to win? Why?



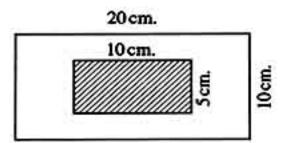
46

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أ

Lesson Two

[24] In the opposite figure:

If a person shot towards the drawn board, find the probability of shooting the shaded part.



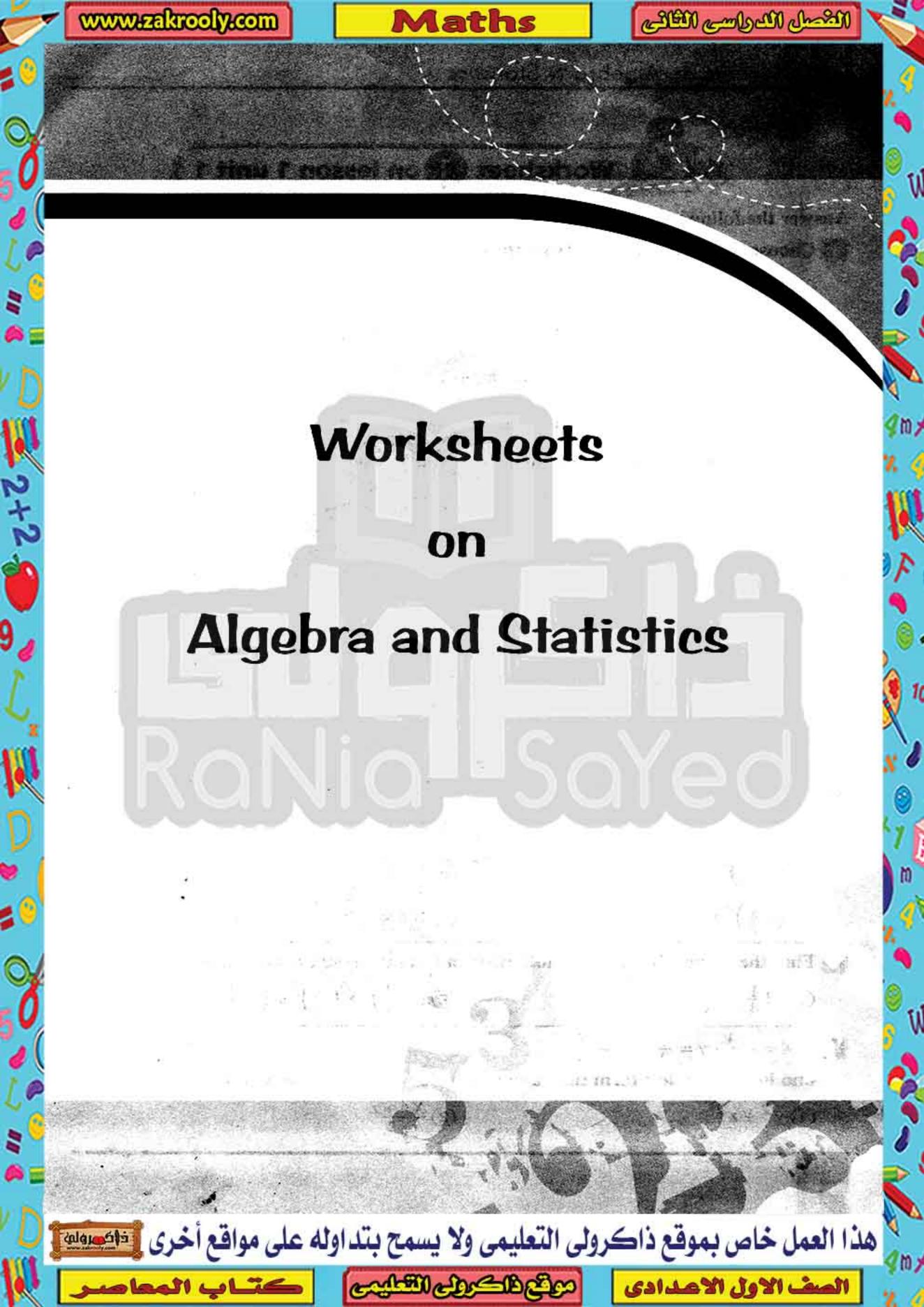


#### For excellent pupils

In the game of the target and the arrow, the target was in the shape of a rectangle divided into parts as shown in the opposite figure:

A	В	С	D
1		F	E

- (1) Find the probability of shooting the part E
- (2) Find the probability of shooting the part formed from A, B and C together.
- A bag contains a number of similar balls 5 of them are white and the rest are red. If the probability of drawing a red ball is  $\frac{2}{3}$ . Find the total number of balls.
- A card is drawn from a group of cards numbered from 1 to n. If the probability that the drawn card carries a number greater than 8 is  $\frac{1}{3}$ , then find the value of n
- When you throw a regular die two successive times and notice the upper face. Find the probability of appearance of the number 3 in the two times.





## Worksheet non lesson 1 unit 1

Answer the following questions:

#### 1 Choose the correct answer from those given:

(a) 
$$\frac{1}{27}$$

(b) 
$$\frac{4}{81}$$

(c) 
$$\frac{1}{81}$$

(d) 
$$\frac{4}{27}$$

(2) The multiplicative inverse of the number 
$$\left(-\frac{3}{4}\right)^{\text{zero}}$$
 is .......

$$(a) - 1$$

(b) 
$$-\frac{4}{3}$$

(c) 
$$\frac{4}{3}$$

(3) The additive inverse of the number 
$$(-2)^3 = \cdots$$

$$(b) - 8$$

$$(c) - 4$$

$$(4)\left(-1\frac{1}{4}\right)^3 = \cdots$$

(a) 
$$\frac{125}{64}$$

(b) 
$$-\frac{125}{64}$$

(c) 
$$\frac{25}{16}$$

(d) 
$$-\frac{1}{64}$$

(5) If 
$$a = b$$
, then  $(\frac{5}{7})^{a-b} = \dots$ 

(a) 
$$\frac{5}{7}$$

(b) 
$$\frac{7}{5}$$

(a) If 
$$x = -\frac{2}{3}$$
,  $y = 2$ , then  $x^y = \dots$ 

(a) 
$$\frac{4}{9}$$

(b) 
$$-\frac{4}{9}$$

(c) 
$$\frac{8}{27}$$

(d) 
$$-\frac{8}{27}$$

#### 2 Complete the following:

$$(1)\frac{64}{125} = (\frac{4}{5})^{\dots}$$

(3) 
$$\left(-\frac{1}{2}\right)^3 - \left(\frac{1}{2}\right)^2 = \dots$$

$$(4) 9 \times \left(\frac{1}{3}\right)^2 = \cdots$$

$$(5) \left(-\frac{1}{3}\right)^3 \times \left(\frac{3}{2}\right)^2 = \cdots$$

(6) If 
$$a = -3$$
,  $b = -2$ , then  $\left(\frac{b}{a}\right)^3 = \cdots$ 

#### Find the value of each of the following putting the result in the simplest form:

$$\textcircled{1}\left(2\frac{1}{4}\right) \div \left(-1\frac{1}{2}\right)^2$$

$$(2)(-\frac{2}{3})^3 \times (\frac{1}{3})^3 \div (-\frac{2}{9})^2$$

4 If 
$$x = -\frac{3}{2}$$
,  $y = \frac{1}{2}$ ,  $z = -\frac{3}{4}$ ,

find in the simplest form the numerical value of each of the following:

(1) 
$$y^2 \div z^2$$

$$2\frac{x^2+z}{y^2}$$

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق





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		me correct answe	er:
<b>(b)</b>	©	<b>d</b>	
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<b>b</b>	©	<b>d</b>	3
<b>b</b>	©	<b>a</b>	
Ъ	©	<b>d</b>	
Ъ	©	<b>d</b>	
	<ul><li>(b)</li><li>(b)</li><li>(b)</li><li>(c)</li></ul>	<ul> <li>Б</li> <li>С</li> <li>С</li> <li>Б</li> <li>С</li> <li>С</li></ul>	b       c       d         b       c       d         b       c       d         b       c       d

(z)		
(3)		 
<b>④</b> ······	 	 . 3
(5)		
<b>6</b> )	 	 )//



#### Worksheet 2 till lesson 2 unit 1

#### Answer the following questions:

#### 1 Choose the correct answer from those given:

$$(1) 5^2 \times 5^3 = \cdots$$

(a) 
$$5^6$$

(b) 
$$5^5$$

(d) 
$$5^{32}$$

(2) 
$$(a^2)^4 = \cdots$$

(3) 
$$\frac{(y^5)^2}{y^3} = \dots$$
,  $y \neq 0$ 

(a) 
$$y^4$$

(b) 
$$y^{13}$$

(c) 
$$y^{10}$$

(d) 
$$y^{7}$$

(4) The additive inverse of the number 
$$\left(-\frac{3}{4}\right)^2 = \cdots$$

(a) 
$$\frac{9}{16}$$

(b) 
$$-\frac{9}{16}$$

(c) 
$$-\frac{3}{4}$$

(d) 
$$\frac{3}{4}$$

(5) The quarter of the number 
$$4^{20} = \cdots$$

(a) 
$$4^5$$

(b) 
$$4^{10}$$

(c) 
$$4^{19}$$

(d) 
$$2^{10}$$

(6) 
$$2^5 + 2^5 + 2^5 + 2^5 = \cdots$$

(a) 
$$8^5$$

(b) 
$$2^{10}$$

(c) 
$$2^7$$

(d) 
$$2^{20}$$

#### 2 Calculate each of the following putting the result in the simplest form:

$$(1)(\frac{3}{5})^{\frac{7}{5}} \div (\frac{3}{5})^{5} \times \frac{3}{5}$$

(2) 
$$\frac{x^5 \times x^8}{x^3 \times x^2 \times x^4}$$
 where  $x \neq 0$ 

$$(3) \left(-\frac{c^2}{d}\right)^3$$

$$(4) \left( (-\frac{2}{3})^2 \right)^3$$

3 If 
$$a = -\frac{1}{2}$$
,  $b = 2$ ,  $c = \frac{3}{4}$ ,

#### find the numerical value of the expression: $a^3b^2 + b^2c - 8$ abc

# Reduce to the simplest form: $\frac{(-2x^2y)^3}{(-4xy)^2}$ where $xy \neq 0$ :

, then find the numerical value of the result if : 
$$x = 1$$
,  $y = 4$ 

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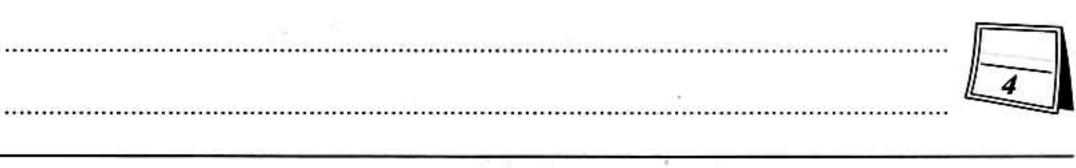


## The answer of worksheet



(1)(a)	Ъ	©	the correct answer	
(2) (a)	<b>(b)</b>	©	<b>d</b>	
(3) (a)	<b>(b)</b>	©	<b>d</b>	3
(4) (a)	<b>b</b>	©	d	
(5) (a)	Ъ	©	d	
(6) (a)	Ъ	©	<u>d</u>	
(1)				
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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى



#### Worksheet 3 till lesson 3 unit 1

#### Answer the following questions:

#### 1 Choose the correct answer from those given:

(1) If 
$$x^{-1} = \frac{1}{2}$$
, then  $x = \dots$ 

(a) 
$$\frac{1}{2}$$

(b) 
$$-\frac{1}{2}$$

$$(d) - 2$$

(2) 
$$\frac{(-2x^2y)^3}{(-4xy^2)^2} = \cdots , xy \neq 0$$

(a) 
$$\frac{x^3}{2 y}$$

(b) 
$$-\frac{x^4}{2y}$$

(c) 
$$\frac{x^5}{2y^2}$$

(d) 
$$\frac{x}{y}$$

(3) 
$$\frac{(7 \times y^{-2})^{zero}}{5^{zero} \times x^{-3} y^2} = \cdots$$
,  $x y \neq 0$ 

(a) 
$$\frac{y^2}{x^3}$$

(b) 
$$x^3 y^2$$

(c) 
$$\frac{1}{x^3 y^2}$$

(d) 
$$\frac{x^3}{y^2}$$

(4) 
$$(3^2)^5 = \cdots$$

(a) 
$$3^5$$

(b) 
$$3^3$$

(c) 
$$3^{10}$$

(d) 
$$3^7$$

(5) If 
$$x = \frac{1}{2}$$
,  $y = \frac{1}{4}$ , then  $x^2 + y = \dots$ 

(a) 
$$\frac{3}{4}$$

(b) 
$$\frac{1}{2}$$

(c) 
$$\frac{9}{16}$$

(6) 
$$\left(\frac{m^2}{n^{-3}}\right)^{-1} \times \left(\frac{3 \text{ m}^{-2}}{n^{-2}}\right)^{-2} = \dots \to \text{mn} \neq 0$$

(a) 
$$\frac{9 \text{ m}^2}{\text{n}^7}$$
.

(b) 
$$\frac{m^2}{9 n^7}$$

(c) 
$$\frac{m^2}{9n}$$

$$(d) \frac{9 \text{ m}^6}{\text{n}}$$

#### 2 Complete the following:

(1) 
$$2 x^{-4} = \frac{2}{\dots}$$

(2) 
$$2\frac{1}{4} = (\frac{3}{2})^{-1}$$

(3) 
$$5^6 \times 5^{-6} = 7$$
...

(1) 
$$2x^{-4} = \frac{2}{\dots}$$
  
(2)  $2\frac{1}{4} = (\frac{3}{2})^{\dots}$   
(3)  $5^6 \times 5^{-6} = 7^{\dots}$   
(4) If  $x = \frac{1}{4}$ ,  $y = \frac{1}{8}$ , then :  $(x - y)^{-1} = \dots$   
(5)  $5^{-3}(\frac{3}{2})^{\text{zero}} = \dots$   
(6)  $(3 \text{ a}^2)^{-1} = \frac{1}{\dots}$ 

(5) 
$$5^{-3} \left(\frac{3}{2}\right)^{\text{zero}} = \dots$$

**(B)** 
$$(3 \text{ a}^2)^{-1} = \frac{1}{\dots}$$

#### Calculate the value of each of the following:

(1) 
$$\frac{5^{-2} \times 5^5}{5^3}$$

$$2\left(\frac{3^4 \times 7^2}{7^3 \times 3^2}\right)$$

(1) 
$$\frac{5^{-2} \times 5^5}{5^3}$$
 (2)  $\left(\frac{3^4 \times 7^2}{7^3 \times 3^2}\right)^{-1}$  (3)  $\frac{x^2 y^2 \times x^2 y \times y^2}{x^2 \times y^2}$  (4)  $\left(-\frac{x^3}{y^2}\right)^{-2}$ 

$$(4)\left(-\frac{x^3}{y^2}\right)^{-2}$$

If 
$$x = \frac{2}{3}$$
,  $y = 6$ ,  $z = \frac{1}{3}$ , find the value of the expression:  $\frac{x^{-1}y}{z^{-1}}$  + y



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## The answer of worksheet



1	Shade	the circle	that represer	its your choice	for the	correct answer	::
---	-------	------------	---------------	-----------------	---------	----------------	----

- **1** (2)
- **(b)**
- (C)
- (d)

(2)(a)

(3)(a)

- **(b)**
- ©
- **(1)**

- (4)(a)
- **b**

**(b)** 

- 0
- **d**

- (5) (a)
- **b**
- 0
- **d**

- (6) (a)
- **(b)**
- (c)
- **d**

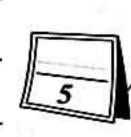


- - 3) ......
- **4** 
  - 5) .....
- **(B)** ....

3.1

- (S) ....
- ③ ...
- (4) ..

4



كراسة المعاصر رياضيات (لغات) / ١ إعدادي / تيرم ٢ (٢ : ٢)

ذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى [طعوري



#### Worksheet 4 till lesson 4 unit 1

#### Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The additive inverse of the number 3<sup>-1</sup> is .......
  - (a)  $\frac{1}{3}$

- (b)  $-\frac{1}{3}$
- (c) 3
- (d) 3

- (2)  $(2 \text{ a})^3 = \cdots$ 
  - (a)  $2 a^3$

(b) 8 a

- (c)  $8 a^3$
- (d) 32 a

- (3) Which of the following =  $\frac{1}{4}$  million?
  - (a)  $25 \times 10^5$
- (b)  $0.25 \times 10^5$
- (c)  $0.25 \times 10^6$
- (d)  $0.25 \times 10^7$

- (4)  $\left(\frac{2}{5}\right)^{-1} \div \frac{5}{2} = \dots$ 
  - (a) 1

(b)  $\frac{5}{2}$ 

- (c)  $\frac{25}{4}$
- (d)  $\frac{4}{25}$

- (5)  $2.37 \times 10^{-4} = \cdots$ 
  - (a) 0.00237
- (b) 0.000237
- (c) 23700
- (d) 0.0000237

- (a)  $3 y^{-1} = \dots y \neq 0$ 
  - (a)  $\frac{1}{3}$  y

(b)  $\frac{3}{v}$ 

- (c)  $y^{-3}$
- $(d) y^3$

#### 2 Write each of the following numbers on its standard form (scientific form):

(1) - 2540000

**(2)** 0.000046

(3)  $0.7 \times 10^{-7}$ 

 $(4) 0.0435 \times 10^9$ 

## [3] [a] If $a = -\frac{1}{2}$ , b = 2, $c = \frac{3}{2}$ , find the numerical value of the expression: $a^2b^3 + (a+c)^5$

#### [b] Calculate the value of each of the following:

(1)  $\frac{(3^{-2})^4}{3^{-5} \times 3^{-2}}$ 

- (2)  $(3^{\text{zero}} \times 2^{-2})^{-2}$
- (3)  $\frac{(-3)^7 \times (-3)^{-2}}{(-3)^5}$

#### 4 Write the result of each of the following on the standard form:

- (1)  $(5.8 \times 10^7) + (3.2 \times 10^5)$
- (2)  $(65.5 \times 10^{-2}) \div (5 \times 10^{2})$

(3) 60000 × 5000



## The answer of worksheet





1 Shade the circle that represents your choice for the correct answer:							
(1)(a)	<b>(b)</b>	(	<b>(d)</b>				

(2)(a)

(3) (a)

- **(b) (b)**
- ©
- **d**

**d** 

- (4) (a)
- **b**
- 0
- **d**

- (5) (a)
- **(b)**
- 0

(d)

**d** 

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	4	1

















#### Answer the following questions:

#### 1 Choose the correct answer from those given:

(1) If 
$$0.000237 = 2.37 \times 10^n$$
, then  $n = \dots$ 

$$(c) - 4$$

$$(d) - 2$$

(2) 
$$(x^{-2})^3 = \cdots$$
,  $x \neq 0$ 

(a) 
$$x^{-6}$$

(b) 
$$x^{-5}$$

(d) 
$$x^6$$

$$(3) - 11 + 3 \times 7 = \cdots$$

$$(c) - 56$$

$$(d) - 1$$

(4) 
$$3^2 + 3^2 + 3^2 = \cdots$$

(a) 
$$3^3$$

(b) 
$$3^8$$

(c) 
$$1^2$$

(d) 
$$3^6$$

(5) The number 
$$1\frac{9}{16} = (\cdots)^2$$

(a) 
$$1\frac{3}{4}$$

(b) 
$$\frac{4}{5}$$

(c) 
$$\frac{3}{4}$$

(d) 
$$\frac{5}{4}$$

(6) Twice the number 
$$2^{18} = \cdots$$

(a) 
$$2^9$$

(b) 
$$2^{36}$$

(c) 
$$2^{10}$$

(d) 
$$2^{19}$$

#### 2 Calculate the value of each of the following:

(1) 
$$8 \times 2^2 - 7 \times (4+1)$$

(2) 
$$2((5^2+1)-(4^2-1))$$

(3) 
$$\frac{5+2\times5}{2^2+1}$$
 +  $5^2$  - 5

(4) 
$$16 \div \frac{1}{4} - \frac{3}{4} \times 10^2 + 25$$

#### [3] [a] Find the result in the standard form : $(4.4 \times 10^3) \times (2 \times 10^5)$

[b] Find the value of : 
$$\frac{7^{-2} \times 7^5}{7^3}$$

[4] [a] If 
$$x = -\frac{1}{2}$$
,  $y = \frac{3}{4}$ , find the numerical value of :  $x^3$  y<sup>2</sup>

[b] If 
$$x = 5$$
, find the value of the expression:  $2\left(\frac{3x+6}{4x-13}\right)$ 



(2)(a)

(4)(a)

#### The answer of worksheet

Total 15

1	Shade	the	circle	that	repres	ents y	our	choice	for	the	correct	answer	r:

- (1) (a) (b) (c) (d)
  - © (d)
- (3) (a) (b) (c) (d)

**b** 

**b** 

- (c) (d)
- (5) a (b) (c) (d)
- (6) (a) (b) (c) (d)

2 (1)	 	 
(6)		# #

- 3
- **4**



[b]

1.3



#### Worksheet 6 till lesson 6 unit 1

#### Answer the following questions:

#### Choose the correct answer from those given:

$$(1)\sqrt{(-7)^2} = \cdots$$

$$(c) - 7$$

$$(d) \pm 7$$

$$(2)\sqrt{10^2-8^2} = \cdots$$

$$(c) \pm 2$$

$$(d) \pm 6$$

(3) 
$$4 + 2 \times 3 = \cdots$$

(a) 
$$\frac{1}{3}$$

(c) 
$$\frac{1}{9}$$

$$(d)$$
 3

#### (5) If the thickness of a piece of paper = 0.012 cm., then which of the following is the height of a ream of 600 pieces of paper?

(a) 
$$(72 \times 10^{-3})$$
 cm.

(b) 
$$(72 \times 10^{-2})$$
 cm.

(d) 
$$(7.2 \times 10^{zero})$$
 cm.

(6) 
$$\sqrt{16} = \cdots$$

#### 2 Complete the following:

(1) 
$$\frac{5^{-2} \times 5^3}{5^4} = 5$$
...

(2) 
$$-\sqrt{9+16} = -3 + \cdots$$

(3) 
$$\left(4\frac{1}{2}\right)^3 \div \left(2\frac{1}{4}\right)^3 = \cdots$$

(4) A square is of side length 
$$\frac{2x}{3}$$
 length unit, then its area is ...... square unit.

(5) If 
$$X = \frac{1}{2}$$
,  $y = \frac{1}{4}$ , then  $(X - y)^{-1} = \dots$ 

(6) 
$$2^5 \times \dots = 2^{10}$$

#### [3] [a] A circle whose area is 154 cm. Find the length of its radius

[b] Reduce to the simplest form : 
$$\left(-\frac{1}{2}\right)^3 \times \sqrt{\frac{25}{9}} \times \sqrt{\left(\frac{8}{5}\right)^2} \times 3^{-1}$$

[4] [a] If 
$$a = \frac{1}{3}$$
,  $b = -\frac{2}{3}$ , find the value of :  $(a^3 \div b^3)^{-1}$ 

[b] Calculate the value of : 
$$5((2^2-1)-(2^2-2))$$



#### The answer of worksheet



				mark
hade the circle	that represents	your choice for	the correct answ	er :
1) (a)	<b>(b)</b>	©	<b>d</b>	
2) (a)	ъ (b)	©	d	
3) (a)	<b>b</b>	©	<b>d</b>	3
4) (a)	<b>b</b>	©	<u>d</u>	
5) <b>a</b>	ь	0	<b>d</b>	
6) (a)	<b>b</b>		<b>d</b>	
2) ····································				3
5) ····································				
b]				4
b]	2 Vy 3 -1 1 70			

[b]

15

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى والعصولية



#### Answer the following questions:

#### 1 Choose the correct answer from those given:

$$(1)\sqrt{10^2-6^2} = \cdots$$

(a) 4

(b) 8

- $(c) \pm 4$
- $(d) \pm 8$

- (2) The number 0.0000014 = ...
  - (a)  $1.4 \times 10^{-5}$
- (b)  $1.4 \times 10^5$
- (c)  $1.4 \times 10^{-6}$
- (d)  $1.4 \times 10^6$

(3) 
$$\frac{9}{x^{-2}} \times \frac{x^{-4}}{3} = \dots$$

- (a)  $3 x^{-6}$
- (b)  $\frac{3}{x^2}$
- (c)  $\frac{3}{x^6}$
- (d)  $\frac{3}{x^8}$

- (4) The S.S. of the equation: 2 x = -6 in  $\mathbb{Z}$  is ....
  - (a)  $\{-3\}$
- (b) Ø

- (c)  $\{-6\}$
- $(d) \{0\}$

- (5)  $(a^3)^4 = \cdots$ 
  - (a)  $a^{43}$

(b)  $a^7$ 

- (c)  $a^{-1}$
- (d)  $a^{12}$

- (6) If: 3 y = 6, then  $6 y = \dots$ 
  - (a) 2

(b) 3

- (c) 6
- (d) 12

#### 2 Complete the following:

$$(1)\sqrt{36} + \sqrt{16} = \sqrt{\dots}$$

- (2) If the middle number of three consecutive natural numbers is X, then the sum of these three numbers in the simplest form = .....
- (3)  $(2b^{-1})^{-1} = \cdots$
- $(4)2 \times 6 4 \div 2$
- [3] [a] Two natural numbers, the difference between them is 5 and their sum is 15 find the two numbers.
  - [b] Reduce to the simplest form :  $\sqrt{\frac{49 x^2 y^2}{35}}$
- [a] Find the S.S. of the following equation in  $\mathbb{Q}$ : 3 (2 x 1) = 15
  - [b] Find the value of :  $(-\frac{1}{3})^2 + \sqrt{\frac{64}{81}} (\frac{3}{7})^{\text{zero}}$

Worksheets on Algebra & Statistics



## The answer of worksheet



1 Shade the circle that represents your choice for the correct answer:					
(1)(a)	<b>(b)</b>	©	<b>d</b>		

(2)(a)	<b>(b)</b>	©	<b>d</b>	
(3)(a)	Ъ	©	<b>d</b>	
(4)(a)	ь	©	d	

(5) (a)	<b>(b)</b>		d
<b>6 a</b>	Ď	©	<b>d</b>

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Worksheets on Algebra & Statistics



2 ①

## The answer of worksheet



1 Shade the circ	le that represents	your choice for the	correct answe	r:
(1)(a)	<b>(b)</b>	© **	<b>d</b>	= 22
(2) (a)	<b>(b)</b>	© 2	<b>d</b>	
(3) (a)	Ъ	© 1	<b>d</b>	3
(4) (a)	Ъ	©	<b>d</b>	

		7 7		N
<b>6 a</b>	<b>(b)</b>	© 1	<b>d</b>	
(5)(a)	ъ -	(C)	(d)	25.

a]		
b]		
b]		

[a]	1 (0)440 (1)		 
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	1 32 31 4	36000	
b]			
		0	

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■ Worksheets on Algebra & Statistics



### Answer the following questions:

### 1 Choose the correct answer from those given:

- (1) If  $2 \times = 3 \times$ , then  $\times = \cdots$ 
  - (a) 2

- (b) 2
- (c) zero
- (d) 1

- (2) If  $x = 28 \div 4 + 3 2 \times 5$ , then  $x = \dots$ 
  - (a) 6

(b) 12

- (c) 10
- (d) zero

- (3) Twice the number  $2^{18} = \cdots$ 
  - (a)  $2^9$

(b)  $2^{26}$ 

- (c)  $2^{10}$
- (d)  $2^{19}$

- (4)  $x^4 \div x^{-2} = \cdots$ 
  - (a)  $x^2$

- (b)  $x^{-6}$
- (c)  $x^{-8}$
- (d)  $x^6$
- (5) As flipping a fair coin once, the probability of appearing a head is .........
  - (a) 5

- (b) 5 %
- (c) 50 %
- (d) =

- (6) The probability of the impossible event = ......
  - (a) 1

(b) 2

- (c) zero
- (d)  $\frac{1}{2}$

### 2 Complete the following:

- (1)  $2^3 \times 2^{-3} = 5$
- (2) If x > 4, then -x (-4)
- (3) Half a million = ..... (in the standard form).
- (4) If the probability of occurring an event is  $\frac{3}{8}$ , then the probability of not occurring of the same event = .....
- [3] [a] The sum of three consecutive natural numbers is 33. Find these numbers.
  - [b] Reduce to the simplest form  $\frac{x^2 \times x^7}{x^3 \times x^2}$ 
    - , then find the value of the result when : x = -3
- [a] Half of the area of a square is 18 cm. Find its side length.
  - [b] A card is drawn randomly from 8 cards numbered from 1 to 8 Write the sample space , then find the probability of each of the following :
    - (1) Appearing an even number.
- (2) Appearing a number divisible by 3



هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخر الصف الاول الاعدادي صحيحاكيكي كالمحيولية العليمي كالمحيولية العام العمادة المحاددي المحيولية العمادة المحاددي المحيولية المحيولية العمادة المحيولية المحيولية

بذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى [طعمولية

### Model Examinations of the school book

### Model

Answer the following questions:

### 1 Complete:

Complete: 
$$(1) 2 \times 6 - 4 \div 2 = \dots$$

(2) If: 
$$7 - 2 \times = 3$$
, then  $\times = \dots$ 

(3) If: 
$$3 X + 1 \ge 10$$
, then  $X \ge \dots$ 

- (4) The standard form of the number  $0.7 \times 0.005 = \cdots$
- (5) A class has 36 students, the number of boys are 20, if a student is chosen randomly , then the probability that the student is a girl = .....

### Choose the correct answer:

(1) The sum of the probabilities for all possible outcomes of a randomly experiment is ........

(a) zero

- (b) 1
- (c) > 1
- (d) < 1

(2) If:  $3 = \sqrt{4} b$ , then  $\frac{a}{b} = \dots$ 

- (a) 2:3
- (b) 3:2
- (d) 4:3

(3)  $\left(\frac{-2}{3}\right)^{-3}$  equals .....

(a)  $\frac{-27}{8}$ 

- (b)  $\frac{-8}{27}$
- (c)  $\frac{8}{27}$
- (d)  $\frac{27}{8}$

(4) There are 21 boys and 15 girls in a classroom, one pupil is chosen randomly, the probability that the chosen pupil is a girl = ........

(a)  $\frac{5}{12}$ 

- (b)  $\frac{7}{12}$

(d)  $\frac{5}{6}$ 

Simplify to the simplest form :  $\left(-\frac{3}{7}\right)^0 \times \left(\frac{-2}{5}\right)^2 \times \sqrt{6\frac{1}{4}}$ 

### 4 [a] Find in Q the S.S. of the following:

- (1)  $3 \times + 1 = 25$
- (2)2X+5<16

[b] The population of a city has been growing according to the rule:

 $y = 3 (1.02)^n$  million. Calculate the population that will be in 2 years in the standard form.

## 5 A factory of a tire record the distance that traveled by a certain type of them before damage for 800 units of this type as following.

The distance in thousand (km.)	Less than 50	50 to 100	More than 100 till 150	I was the increase of contract of the contract of
The number of damage tire	80	120	280	320

If you bought the type of this tyre , what is the probability of change it :

- (1) Before traveled 50 thousand km.
- (2) After traveled more than 100 thousand km.

## Model

Answer the following questions:

### 1 Complete:

(1) 
$$\left(\frac{-2}{3}\right)^0 = \dots$$
 (2)  $\sqrt{\frac{16}{49}} = \dots$ 

$$2\sqrt{\frac{16}{49}} = \cdots$$

- (3) The probability of impossible event = ......
- (4) 1, 2, 3, 5, 8, ...... (In the same pattern)
- (5) If the probability that the student is absent in a school is 0.15, if the number of students of this school is 600, then the number of the present student that day is ......

### Choose the correct answer:

$$(1) 2^3 \times 2^5 = \cdots$$

(a) 
$$2^2$$

(b) 
$$2^8$$

which had willing a series

(d) 
$$2^{53}$$

(2) Which of the following the greatest? ......

(a) 
$$2.3 \times 10^4$$

(b) 
$$2.3 \times 10^5$$

(c) 
$$3.2 \times 10^4$$

(d) 
$$3.2 \times 10^5$$

(3) The side length of a square whose area  $9 \times 2 \text{ cm}^2$  is .......... cm.

(a) 
$$3 X$$

(b) 
$$3 x^2$$

(c) 
$$9 X$$

(d) 
$$9x^2$$

(4) Which of the following may be probability of an event ? ......

$$(a) - 0.25$$

Two integers number the smaller one is 2 x and the greater is 5 x, if the difference between them is 30 Find the two numbers.



هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

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[a] Find in Q the S.S. of each of the following:

(1) 
$$(3 \times + 2) + 5 = 13$$

(2) 
$$2 \times + 15 < 19$$

[b] Find the value of the expression in simplest form:

$$\left(\frac{-2}{3}\right)^2 + \sqrt{\frac{64}{81}} - \left(\frac{3}{7}\right)^0$$

- 5 If a regular die is thrown once and observed the number on upper face, find the probability of each of the following:
  - (1) Getting prime even number.
  - (2) Getting odd number less than 4

Answer the following questions:

1 Complete:

- (1) The probability of the certain event = .....
- (2)  $\frac{1}{9}$ ,  $\frac{1}{8}$ ,  $\frac{1}{7}$ ,  $\frac{1}{6}$ , ...... (In the same pattern)
- (3) The S.S. in  $\mathbb{Q}$  for the equation :  $2 \times + 3 = 4$  is ......
- (4)  $0.00037 = 3.7 \times 10^{n}$ , the value of  $n = \dots$

2 Choose the correct answer:

(1) The multiplicative inverse of the number:  $\sqrt{\frac{9}{16}}$  is ......

(a) 
$$\frac{-4}{3}$$

(b) 
$$\frac{-3}{4}$$

(c) 
$$\frac{3}{4}$$

(d) 
$$\frac{4}{3}$$

(2)  $\frac{x}{2}$  < 5 equivalent .....

(a) 
$$x < \frac{5}{2}$$

(a) 
$$x < \frac{5}{2}$$
 (b)  $x > \frac{5}{2}$ 

(c) 
$$X < 10$$

(d) 
$$x > 10$$

(3)  $3^{x} + 3^{x} + 3^{x}$  equals : ......

(b) 
$$3^{x+1}$$

(d) 
$$3 x^3$$

- (4) There are 480 pupils in a school, 120 of them failed. A pupil is chosen at random, then the probability that the pupil is succeeded
  - (a) 0.25 %
- (b) 0.75
- (c) 0.8

(d) 0.667

3 What is the number which if we add it to its three times, the result is 28?

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

[a] Find in Q the solution set of the following:

$$\bigcirc 3 \times + 5 = 11$$

(2) 
$$2x + 3 \le 7$$

- [b] If the distance between the sun and the earth is  $1.44 \times 10^8$  km. and the light velocity is  $3 \times 10^8$  m/sec. Calculate the elapsed time that the light takes to reach from the sun to the earth.
- [a] Find the result of the expression:  $(5.4 \times 10^4) + (3.7 \times 10^5)$  in the form  $a \times 10^n$ where n is integer number.

[b] A coin is tossed twice calculate the probability:

- (1) The two faces are similar.
- (2) Appearance only one tail.

## Model

### Answer the following questions:

1 Complete:

- (1) When a coin is tossed once then the probability of appearance of a head is .
- (2)  $\frac{1}{1000}$ ,  $\frac{1}{100}$ ,  $\frac{1}{10}$ , ................. (In the same pattern)
- (3) The S.S. of the inequality  $2 < x \le 4$  in N is .......
- (4)  $\frac{1}{2}$ ,  $\frac{3}{4}$ ,  $\frac{7}{8}$ ,  $\frac{15}{16}$ , .....

2 Choose the correct answer:

- (1) The S.S. of the equation : x + 3 = 3 in N is .......
  - (a) Ø

- (b) {0}.
- (c)  $\{3\}$
- $(d) \{6\}$

(2) The number which in the standard form between the following numbers is ........

- (a)  $11 \times 10^8$
- (b)  $9.7 \times 10^{-5}$
- (c)  $10.3 \times 10^{-3}$
- (d)  $0.87 \times 10^8$
- (3) If a coin is tossed 160 times then the approximate expected number of the appearance of a head is ......
  - (a) 60

(b) 78

(c) 90

(d) 159

(4) The number √0.09 is .....

- (a) natural.
- (b) positive integer.
- (c) negative integer.
- (d) rational.

(5) If:  $\frac{6x}{5} = -2$ , then  $x^2 = \dots$ 

- (a)  $\frac{-25}{9}$
- (b)  $\frac{5}{9}$  (c)  $\frac{25}{9}$
- (d)  $\frac{25}{3}$



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- [3] [a] If:  $x = \frac{3}{4}$ ,  $y = \frac{-3}{2}$  Find the numerical value of the expression  $\left(\frac{x^2}{3}\right)^2$ 
  - [b] The sum of two natural number is 15 and the difference between them is 5 Find the two number.
- 4 Find in Q the solution set for each of the following:
  - (1)  $3 \times + 2 = 8$

- (2)4x-3<7
- 5 A coin is tossed twice Calculate the probabilities:
  - (1) The appearance of at least one head.
    - (2) The appearance of at most one head.

Model

Answer the following questions:

- 1 Complete:
  - (1) In the experiment of tossing a die once then the probability of appearance even number is .....

② If: 
$$\frac{x}{y} = \frac{7}{2}$$
, then  $\frac{2x}{7y} = \dots$ 

- (4) The result of the expression:  $\left(\frac{-1}{2}\right)^2 \left(\frac{-1}{2}\right)^3 = \cdots$
- (5) Quarter of 4<sup>20</sup> equals ......
- 2 Choose the correct answer:
  - (1) The S.S. of the inequality x < 2 in N is .......
    - (a)  $\{0\}$
- (b) {1}
- (c)  $\{0, 1\}$
- $(d) \emptyset$

- (2) If:  $\frac{26}{x} + 1 = 14$ , then  $x = \dots$ 
  - (a) 2

- (b) 10
- (c) 13
- (d) 20

- (3) If:  $5 \times = 35$ , then  $2 \times + 1 = \dots$ 
  - (a) 7

(b) 8

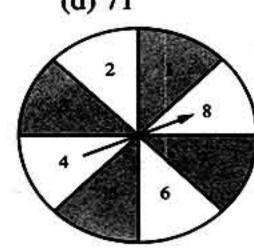
- (c) 15
- (d) 71

(4) In the opposite figure:

The probability that the pointer stop at a number greater than 6 equals ......

(c)  $\frac{3}{8}$ 

(d)  $\frac{3}{4}$ 



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Final Examinations

Find the value of the expression:  $12 \times (2)^2 \div 24 + 3^2$ 

[4] [a] Find in Q the solution set of each of the following:

$$\bigcirc 3 - 4x = -5$$

(2) 
$$2x - 1 \ge 5$$

[b] Simplify: 
$$\frac{n}{2}[3n-6] + \frac{1}{2}[6-2n]$$
, then find its value when  $n = 1$ 

- [5] [a] The sum of the age of 3 sisters now is 25 years. If the eldest was born before the middle by 3 years, and the middle was born before the youngest by 2 years.

  Find the age of each of them now.
  - [b] A box contains 4 white , 5 red and 6 blue balls. A ball is drawn randomly from the box. Calculate the probabilities of the following events.
    - 1) The ball is red.
    - (2) The ball is white or red.



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### **School Examinations**

## Cairo Governorate Nasr City Educational Zone

### St. Fatima Language School

Answer the following questions:

- 1 Choose the correct answer from those between brackets:
  - (1) Half the number  $2^{20} = \dots$

(a) 
$$2^{10}$$

(b) 
$$2^{21}$$

$$(2)\left(\frac{2}{3}\right)^{-2} = \cdots$$

(a) 
$$\frac{4}{9}$$
 (b)  $\frac{9}{4}$ 

(b) 
$$\frac{9}{4}$$

(c) 
$$\frac{-4}{9}$$

resolved 4

(c) 
$$\frac{-4}{9}$$
 (d)  $-\frac{9}{4}$ 

(3) If: 
$$5 X = 20$$
, then  $X + 3 = \dots$ 

$$(4) * \sqrt{\left(-\frac{5}{6}\right)^2} = \cdots$$

(a) 
$$\frac{5}{6}$$

(b) 
$$-\frac{5}{6}$$

(c) 
$$\pm \frac{5}{6}$$

(d) 
$$\frac{25}{36}$$

(5) In an experiment of tossing a metal coin once, the probability of appearance of a head is .....

(a) 
$$\frac{1}{2}$$

(d) 
$$\frac{1}{3}$$

## 2 Complete:

(1) 
$$*\sqrt{16+9} = \cdots$$

(2) If: 
$$a - 3 < 0$$
, then ........

(3) If: 
$$0.00052 = 5.2 \times 10^n$$
, then  $n = \dots$ 

(4) The additive inverse of 
$$\left(-\frac{2}{5}\right)^2$$
 is ......

- (5) The probability of the impossible event is ........
- [3] [a] Solve each of the following inequalities and represent the solution set on the number line where  $x \in \mathbb{Z}$ :

(1) 
$$8 X - 3 X - 1 \le 29$$

(2) 
$$X + 4 > 1$$

[b] Find each of the following:

$$(1)\left(-\frac{2}{3}\right)^2 \times \frac{9}{4} \times \left(-\frac{1}{4}\right)^0$$

(2) 
$$\left(-\frac{2}{3}\right)^6 \div \left(-\frac{2}{3}\right)^7$$

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## Maths

### \_Final Examinations

[4] [a] Two natural numbers, one of them is twice the other and their sum is 45 Find the two numbers.

[b] If:  $x = \left(-\frac{1}{2}\right)$ ,  $y = \left(\frac{4}{3}\right)$ ,  $z = \left(\frac{1}{5}\right)$ , then find the numerical value of  $x^3$  y<sup>2</sup> z

- [5] [a] \* Arrange in an ascending order:  $2.7 \times 10^{-4}$ ,  $7.3 \times 10^{-5}$ ,  $10^{-4}$ ,  $0.25 \times 10^{-2}$ 
  - [b] One card is selected randomly from 8 cards number from 1 to 8 Write down the sample space , then find the probability of each of following event :
    - (1) Getting an even number.
    - (2) Getting a number greater than or equal to 6

## Cairo Governorate

### **El-Zeitoun Education Zone**

### **El-Salam Experimental Language School**

Answer the following questions:

- 1 Choose the correct answer:
  - (1) The third of  $3^{20} = \dots$ 
    - (a)  $3^{10}$
- (b)  $3^{19}$

- (c)  $3^{18}$
- (d)  $3^{17}$
- (2) If a die is tossed once then the probability of getting a number satisfies the inequality 2 < x < 3 equals ......
- (b)  $\frac{1}{3}$

- (c)  $\frac{1}{4}$
- (d) zero

- (c)  $\frac{3}{6}$
- (d) otherwise

 $(4)\left(\frac{-1}{2}\right)^0 = \cdots$ 

- (a) 1
- (b)  $\frac{-1}{2}$

- (c) 1
- (5) The solution set of the equation :  $-2 \times + 1 = -3$  in N is ......
  - (a)  $\{1\}$
- (b)  $\{2\}$

- (c)  $\{3\}$

- 2 Complete the following to get a right statement :
  - (1) If the age of a man now is X years, then his age 3 years ago is ...........
  - (2)  $\sqrt{(91)^2 91 \times 2 + 1} = \cdots$
  - (3) The probability of the impossible event is ........

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(4) If:  $0.000024 = 2.4 \times 10^n$ , then  $n = \dots$ 

(5) If: 
$$\frac{x}{5} = \frac{8}{5}$$
, then  $\frac{1}{4}x = \dots$ 

[3] [a] If: 
$$x = -\frac{3}{2}$$
,  $y = \frac{1}{2}$  and  $z = -\frac{4}{3}$ , find the numerical value of:  $x^2 - yz^2$ 

[b] Solve the inequality in  $\mathbb{Q}$ : 3(x+2) < -x+4

### [a] Solve the equation: $5 \times + 8 = 13 - 2 \times$ , where $X \subseteq \mathbb{Q}$

- [b] A card is chosen at random from ten cards numbered from 1 to 10, what is the probability that the selected card shows:
  - (1) An odd number.

- (2) A prime number.
- (3) An odd number greater than 3

## [5] [a] Calculate: $\frac{7^{-2} \times 7^5}{7^3}$

[b] The length of a rectangle exceeds its width by 4 metres and its perimeter is 68 metres. Find the dimenions of the rectangle.

## Giza Governorate

### **Omrania Directorate**

El-Sadat Exp. Lang.Sch.

Answer the following questions:

- 1 Choose the correct answer from the given ones:
  - (1) 0.00000027 = .....

(In the standard form)

- (a)  $2.7 \times 10^{-6}$
- (b)  $2.7 \times 10^6$
- (c)  $2.7 \times 10^{-7}$
- (d)  $2.7 \times 10^7$

- (2) \*  $\frac{5 a^0}{b^{-2}} = \dots , a \neq 0 , b \neq 0$ 
  - (a)  $5 b^2$
- (b)  $\frac{b^2}{5}$
- (c)0
- (d) 1
- (3) If the age of Ahmed now is X years then this age 10 years ago is ...... years.
  - (a) 10 X
- (b) X + 10
- (c) 10 X
- (d) x 10
- (4) As throwing a fair die once, the probability of appearance of prime number on the upper face is .....
  - (a)  $\frac{1}{2}$

- (b) \frac{1}{5}
- (c)  $\frac{5}{6}$
- (d)  $\frac{1}{3}$

- (5) If: 5 X = 20, then  $X + 5 = \dots$ 
  - (a) 10

- (b) 15
- (c) 9
- (d) 20

2 Complete each of the following:

- (1) The multiplicative inverse of  $\sqrt{6\frac{1}{4}}$  is ......
- (3) The probability of the impossible event = ........
- (4)  $2 \times 6 4 \div 2 = \cdots$
- (5) If: X < y and z is negative then X z .......... yz

[3] [a] Simplify each of the following:

(1) 
$$\left(\frac{-2}{3}\right)^2 \times \sqrt{\frac{9}{4}} \times \left(\frac{2}{7}\right)^0$$
 (2)  $\frac{(2)^5 \times (-2)^4}{(2)^9}$ 

(2) 
$$\frac{(2)^5 \times (-2)^4}{(2)^9}$$

[b] Three consecutive natural numbers their sum is 33 Find these numbers.

Find the solution set of each of the following where  $x \in \mathbb{Q}$ :

(1) 
$$2 X + 1 = 13$$

(2) 
$$3x - 1 \le 2x + 4$$

[5] [a] If:  $x = \frac{-2}{3}$ ,  $y = \frac{1}{2}$  and  $z = \frac{-4}{3}$  Find the value of:  $x^2 - y^2 z$ 

[b] A box contains 5 white , 4 black and 7 red balls. A ball is drawn randomly from the box find the probabilities of the following events:

(1) The ball is black.

(2) The ball is not white.

## Giza Governorate

Kerdasa E. Directorate

### **Mathematics directing**

Answer the following questions:

1 Choose the correct answer from the given ones:

(a) 
$$\left(\frac{x}{y}\right)^{n+}$$

(b) 
$$\left(\frac{x}{y}\right)^{n-n}$$

(a) 
$$\left(\frac{x}{y}\right)^{n+m}$$
 (b)  $\left(\frac{x}{y}\right)^{n-m}$  (c)  $\left(\frac{x}{y}\right)^{m-n}$  (d)  $\left(\frac{x}{y}\right)^{\frac{n}{m}}$ 

(d) 
$$\left(\frac{x}{y}\right)^{\frac{n}{m}}$$

$$\sqrt{\left(\frac{-5}{6}\right)^2} = \cdots$$

(a) 
$$\frac{-5}{6}$$

(b) 
$$\frac{5}{6}$$

(c) 
$$\pm \frac{5}{6}$$
 (d)  $\frac{2}{6}$ 

(d) 
$$\frac{2}{6}$$

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(4) \* If:  $-2 \times < 6$ , then ......

- (a) X < 3
- (b) x < 4
- (c) x > 3
- (d) x > -3

(5) A class contains 20 boys and 15 girls. If a pupil is chosen randomly then the probability that the pupil is a boy = ........

(a)  $\frac{1}{20}$ 

- (b)  $\frac{1}{15}$
- (c)  $\frac{3}{7}$
- (d)  $\frac{4}{7}$

2 Complete each of the following :

(1) 
$$4 + 2 \times 3 = \cdots$$

- (2) The additive inverse of the number  $\left(\frac{-1}{2}\right)^2$  is .......
- (3) \* If your age now is X years then your age 5 years ago was ...... years.
- (4) \* 2 x = 9, then 4  $x 1 = \dots$
- (5)  $\sqrt{16+9} = \cdots$

[3] [a] Find the S.S. of each of the following:

- (1)  $8 \times 4 = 12$  where  $x \in \mathbb{Z}$  (2)  $2 \times 4 \le 7$  where  $x \in \mathbb{N}$
- [b] \* If:  $a = \frac{1}{3}$ ,  $b = -\frac{2}{3}$  Find the value of:  $(a^3 + b^3)^{-1}$

[4] [a] Simplify to it's simplest form:

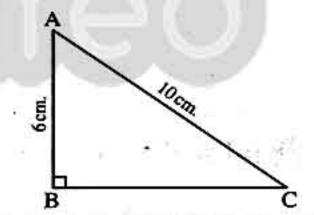
$$(2)(\frac{-5}{4})^2 \times \sqrt{\frac{25}{16}} \times (\frac{-4}{5})^3$$

[b] In the opposite figure:

$$m (\angle B) = 90^{\circ} , AB = 6 cm.$$

and 
$$AC = 10 \text{ cm}$$
.

Find the length of BC



[a] Three consecutive odd natural numbers are with sum 117 Find this numbers.

[b] A card is drawn randomly from 8 cards numbered from 1 to 8 write down the sample space then find the probability of each of the following events:

- (1) A = event of getting an even number.
- (2) B = event of getting a prime number.
- (3) C = event of getting a number divisible by 3

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## Alexandria Governorate

### El-Montaza Education Zone

### Victory College

Answer the following questions:

- Choose the correct answer:
  - (1) \* The S.S. of: -x < 0 in  $\mathbb{Z}$  is ......
    - (a) Z
- (b) Z\_\_

- (c) Z\_
- (d) Z\*

- (a) If: a = -3, then  $a^{-2} = \cdots$ 
  - (a)  $-\frac{1}{9}$
- (b)  $\frac{1}{9}$

- (c) 9
- (d) 9

- (3) If:  $3 \times = 5$ , then the value of  $12 \times = \cdots$ 
  - (a) 4

(b) 36

- (c) 20
- (d) 60
- (4) A regular die is rolled, the probability of getting a number less than 3 is .........
  - (a)  $\frac{1}{2}$

- (c)  $\frac{2}{3}$
- (d)  $\frac{1}{6}$

- (5) Third of  $3^{12} = \cdots$ 
  - (a)  $3^{-1}$
- (b)  $3^{-11}$
- (c)  $3^{11}$
- (d) 1

2 Complete the following:

$$(1)\sqrt{\frac{81}{25}} \div \left(\frac{3}{5}\right)^2 = \dots$$

- (2) If:  $0.000028 = 2.8 \times 10^n$ , then  $n = \dots$
- (3) If:  $x \in \mathbb{N}$ , then the solution set of the equation: x + 7 = 1 is ........
- (4)  $x = \frac{1}{2}$  and  $y = \frac{3}{4}$ , then the numerical value of :  $x^2 + y = \cdots$
- (5)  $2^3 \div 4 \times 3 + (2-1) = \cdots$
- [a] \* Find the result of :  $\frac{2^3 \times 2^{-4}}{2^{-2} \times 2^5}$ 
  - [b] Find the solution set of the following  $(x \in \mathbb{Q})$ :
    - (1) 2x 5 = 1
- (2)4X+9≤1
- 4 [a] The age of a man is three times the age of his son, if the sum of their ages is 60 years. Find the age of each of the man and his son.
  - [b] If:  $x = \frac{1}{2}$ ,  $y = \frac{4}{3}$  and  $z = \frac{3}{2}$  Find the numerical value of:  $8 x^3 y z^2$
- **5** [a] Calculate :  $\left(\frac{1}{3}\right)^2 + \sqrt{\frac{64}{81}} \left(\frac{2}{5}\right)^0$

[b] A ball was drawn randomly from a sack containing 8 balls numbered from 1 to 8 Find the probabilities of drawing a balls numbered with:

- (1) A number that is divisible by 3
- (2) A prime number.

## Kalyoubia Governorate

West Shubra El-Kema Educational Zone

Answer the following questions:

1 Choose the correct answer:

(1) 
$$2^6 \div 2^3 = \cdots$$

- (a)  $3^9$

- (d) 8

(2) 
$$3^3 \times 3^{\text{zero}} = \dots$$

(b) 27

(c) 1

(d) zero

(3) 
$$1\frac{9}{16} = \left(\cdots\right)^2$$

- (a)  $1\frac{3}{4}$
- (b)  $\frac{4}{5}$

- (c)  $\frac{3}{4}$
- (d)  $1\frac{1}{4}$

(4) A class contain 15 girls and 10 boys if a pupil is go out, then the probability that the pupil is a girl is ......

- (a)  $\frac{1}{15}$

- (c)  $\frac{10}{25}$
- (d)  $\frac{3}{5}$

(5) \* If: X = y, then  $3^{X-y} = \dots$ 

(a) 1

(b) 3

- (c)  $3^x$
- $(d) 3 \chi y$

2 Complete:

(1) If the probability of success of a students is 90%, then the probability of his failure

(2) The multiplicative inverse of  $\sqrt{\frac{16}{25}}$  is ......

- (3) If: -x < 5, then x (-5)
- (4) \* If: x + 9 = 11, then the value of  $7x = \dots$
- (5) The standard form of the number 7 millions is .......

[3] [a] \* Simplify to the simplest form:  $\frac{x^2 \times x^7}{x^3 \times x^2}$ , then find its numerical value when X = -3

[b] Calculate the value of :  $20 \div 5 + 8 - (4 - 1)$ 

- [4] [a] Find the solution set of the inequality:  $3 \times -2 > \times +4$ , where  $x \in \mathbb{Q}$ 
  - [b] Find the solution set of the equation :  $3 \times -1 = 5$  in  $\mathbb{Q}$
- [a] \* The sum of three consecutive even numbers is 966 Find them.
  - [b] A bag contains 5 red balls, 3 white balls and 2 blue balls. If all balls are a like and a ball is drawn from the bag randomly , find:
    - (1) The probability that the drawn ball is red.
    - (2) The probability that the drawn ball is white.
    - (3) The probability that the drawn ball is not blue.

## El-Kalyoubia Governorate

### Kalyoub Educational Zone

Answer the following questions:

### 1 Choose the correcte answer:

(1)  $5^{-1} = \cdots$ 

(a) - 1

(b) 5

(c) - 5

(d)  $\frac{1}{5}$ 

(a)  $2 \times 5 - 6 \div 2 = \dots$ 

(a) 2

(b) 8

(c) 7

(d)  $\frac{1}{2}$ 

(3) The multiplicative inverse of  $\left(\frac{2}{3}\right)^0$  is ......

(a)  $\frac{3}{2}$ 

(b)  $-\frac{2}{3}$ 

(c) 1

(d)0

(4) The probability of the impossible event =

(a) 1

(b) 0

(c)  $\frac{1}{2}$ 

(5) If: x + 3 > 5, then x may be equal

(a) 5

(b) 1

(c) - 5

(d) - 2

### 2 Complete:

(1) 
$$\# \sqrt{6^2 + 8^2} = \cdots$$

(a) If: 
$$2700 = 2.7 \times 10^n$$
, then  $n = \dots$ 

(3) If: 
$$x + 9 = 11$$
, then the value of  $7x = \dots$ 

(4) \* 
$$\left(\frac{-2}{5}\right)^6 \div \left(\frac{2}{5}\right)^4 = \dots$$

[3] [a] Find the result in the simplest form :  $\frac{4}{3} \times \sqrt{\frac{9}{25}} \times \left(-\frac{1}{2}\right)^2$ 

- [b] \* The length of a rectangle exceeds its width by 4 metres and its perimeter is 68 metres. Find the dimensions of the rectangle.
- [4] [a] Simplify:  $\frac{x^7 \times x^5}{x^8}$ , then find the numerical value of the result at x = -2
  - [b] Find in  $\mathbb{Q}$  the S.S. of the equation :  $3 \times 7 = 13$
- [a] Find in  $\mathbb{Z}$  the S.S. of the inequality: x-1<3, then represent the solution on number line.
  - [b] When a die is tossing once then find the probability of the event A appearing an odd number on the upper face.

## El-Sharkia Governorate

#### Omar El-Farouk E.L.S.

Answer the following questions:

1 Choose the correct answer:

$$\boxed{1}\sqrt{36+64}=6+\cdots$$

- (a) 10
- (b) 4

- (c) 8
- (d) 6
- (5) The solution set of: -2x + 1 = -3 in  $\mathbb{Z}$  is ......
  - (a)  $\{2\}$
- (b)  $\{-2\}$
- (c)  $\{-4\}$
- (d) Ø
- (3) The probability of the possible event could be ......
  - (a) 0.9
- (b) 1.2

- (c) 16 %
- (d) 5

- (4) The multiplicative inverse of  $\left(-\frac{3}{4}\right)^2$  is ......
  - (a)  $\left(\frac{4}{3}\right)^2$
- (b)  $\left(-\frac{4}{3}\right)^2$  (c)  $\left(\frac{3}{4}\right)^2$
- (d)  $-\left(\frac{3}{4}\right)^2$
- (5) Ali's age 2 years ago was X, then his age now is ...... years.
- (a) X + 2 (b) X 2 (c) 2 X
- (d) 2 X

2 Complete :

- (1)  $\# 2 \times 6 4 \div 2 = \dots$
- (2) The probability of the sure event is .......
- (3) The solution set of:  $1 > x \ge -2$  in N is .......

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## Maths

### Final Examinations

(4) 
$$0.000237 = \dots \times (10)^{\dots}$$
 (in the standard form)

(5) 
$$(2 a^{-1})^{-1} = \cdots$$
 (In the simplest form).

[3] [a] A box contains 2 red balls , 6 white balls and 4 green balls. A ball is drawn randomly. Find the probability that the drawn ball is:

(1) Black.

(2) Not red.

[b] If: 
$$\frac{a}{b} \in \mathbb{Q}$$
,  $\frac{a^2}{b^2} = 0.16$ , Find the value of:  $\left(\frac{a}{b}\right)^3$ 

[4] [a] Simplify:  $\frac{y^3 \times y^{-4}}{y^{-2} \times y^5}$ , then find its numerical value at y = -1

[b] Find S.S. of:  $3 x - 2 \le 3 - 2 x$  in Q

- [a] Two consecutive even numbers, their sum is 150 Find them
  - [b] \* The population of city has been growing according to the rule:
    y = 3 (1.02)<sup>n</sup> million. Calculate the population that will be in 2 years in the standard form.

## 9 El-Beheira Governorate

### **Damanhour Educational**

### Safwa Language Schools

### Answer the following questions:

### 1 Complete:

(1) 
$$\left(\frac{-3}{7}\right)^7 \div \left(\frac{3}{7}\right)^5 = \dots$$
 (In the simplest form).

(2) If: A = 0.000625, then:  $\sqrt{A} = 2.5 \times 10$ .....

(3) If: z > y and y > x, then  $z > \dots$ 

(4) \* The multiplicative inverse of  $\sqrt{\frac{4}{9}}$  is .......

### 2 Choose the correct answer:

(1) 
$$\left(\frac{2 \text{ ab}^{-2}}{3^0 \text{ a}_3^{-2} \text{ b}}\right)^0 = \dots$$

(a)  $\frac{a^3}{3 b^3}$ 

(b)  $a^2$ 

(c) 1

(d)  $\frac{a^2}{b}$ 

(2)  $12(2^2) \div 24 + 3^2 = \cdots$ 

(a) 4

(b) 5

(c) 11

(d) 13

(3) \* The third of the number  $3^{18} = \cdots$ 

(a)  $3^6$ 

(b)  $3^9$ 

(c)  $3^{17}$ 

(d)  $3^{18}$ 

(4) The solution set of the equation :  $3 \times -13 = 26$  in  $\mathbb{Q}$  is ......

(a)  $\{36\}$ 

(b) {13}

(c)  $\{3\}$ 

(d)  $\{31\}$ 

(5) Ebrahim is in a grade 7 class of 36 students and 16 of them are girls. If a student is selected at random from the class, what is the probability that the student is a boy?

(a)  $\frac{4}{9}$ 

(b)  $\frac{1}{2}$  (c)  $\frac{3}{9}$ 

(d)  $\frac{1}{36}$ 

3 Two natural numbers, one of them is twice the other and their sum is 108 Find the two numbers.

[4] [a] If:  $x = \frac{-1}{2}$ ,  $y = \frac{3}{4}$  and  $z = \frac{-3}{2}$ , then find:  $x^3 \div y^2 z^2$ 

[b] Solve the following inequality in  $\mathbb{Q}: 1-(4 \times -1) > 2 \times (-3)$ 

[a] Without using calculator find in form  $a \times 10^n$ ,  $n \in \mathbb{Z}$ :

 $(3.8 \times 10^8) \div (1.9 \times 10^6)$ 

[b] A sample consists of 100 persons who watch T.V. , if some of was selected at random.

What is the probability of that person's preference:

Programs	Documentaries	Drama	News	Sport
Viewers	12	31	21	36

(1) Sport

(2) Not watch news

(3) Documentaries

(4) all of them

## El-Dakahlia Governorate

M.L.S

Answer the following questions:

Complete:

(1) The additive inverse of  $\left(\frac{-2}{3}\right)^2$  is ......

 $(2)\sqrt{6^2+8^2}=6+\cdots$ 

(3) \* The probability of the impossible event = .......

(4)  $0.00000027 = \dots$  (In the standard form)

(5) A cubic die with numbers 1 to 6 is rolled once. The probability of rolling an even number is .....

### 2 Choose the correct answer:

(1) If: X > Y, then -X - Y

(a) =

(c) >

(d) <

(2)  $*\sqrt{(-5)^2} = \cdots$ 

(c) 10

(d) | -5 |

(a) -5 (b) 25 (3)  $\left(\frac{1}{2}\right)^5 \div \left(\frac{1}{2}\right)^3 = \cdots$  $(\frac{1}{2}) \div (\frac{1}{2}) = \dots$ (a)  $\frac{1}{32}$  (b)  $\frac{1}{8}$  (c)  $\frac{1}{4}$ 

(d)  $\frac{1}{16}$ 

(4) If the area of a square is 100 cm<sup>2</sup>, then its side length = ...... cm.

(a) 10

(b) 12

(c) 13

(d) 25

(5) The solution set of the equation:  $2 \times + 1 = -3$  in N is ......

(a)  $\{1\}$ 

(b) {2}

(d) Ø

3 [a] Evaluate:  $\left(\frac{5}{4}\right)^2 \times \sqrt{\frac{16}{25}} \times \left(\frac{-4}{5}\right)^0$ 

[b] Solve the inequality:  $5x-7 \le 3$ ,  $x \in \mathbb{Q}$ 

[a] Find the result of :  $\frac{(-2)^6 \times (-2)^4}{(-2)^8}$ 

[b] The sum of three consecutive numbers is 42 Find them.

[5] [a] \* If:  $x = \frac{3}{4}$  and  $y = -\frac{3}{2}$  Find the numerical value of the expression:  $\left(\frac{x^2}{3}\right)^2$ 

[b] A box contains 3 white , 5 black and 7 red balls. A ball is drawn randomly from the box. Calculate the probabilities of the following events:

(1) The ball is red.

(2) The ball is not white.

## El-Monoufia Governorate

Al-Shohada Directorate

### **Danasor Experimental Language School**

### Answer the following questions:

### 1 Choose the correct answer:

(1) 0.00000052 = .....

(a)  $5.2 \times 10^{-6}$  (b)  $5.2 \times 10^{-7}$ 

(d)  $5.2 \times 10^2$ 

(2)  $\left(-\frac{1}{3}\right)^{-1} = \cdots$ 

(a)  $\frac{-1}{3}$ 

(b) - 3

(c) 3

(d)  $\frac{1}{3}$ 

$$\sqrt{\left(\frac{3}{4}\right)^2} = \cdots$$

- (a)  $\frac{3}{4}$
- (b)  $-\frac{6}{16}$
- (c)  $\pm \frac{3}{4}$

- (4) If: -x < 3, then x 3
  - (a) <
- (b) =

- (c) >
- (d) ≤
- (5) \* The side length of a square whose area 9  $\chi^2$  cm<sup>2</sup> is .......
  - (a) 3 X
- (b)  $3 x^2$
- (c) 9 X
- (d)  $9 x^2$

### 2 Complete with the correct answer:

- (1) \* If: 3 x = 6, then 5  $x = \dots$
- (a)  $* 2^x \times 2^{1-x} \times \frac{1}{2} = \dots$
- (3) The probability of the impossible event = ......
- (4)  $3 x^0 = \dots$
- (5)  $2 \times 6 4 \div 2 = \dots$

### [3] [a] Find in the simplest form:

$$(1) \left(\frac{-2}{3}\right)^2 \times \sqrt{\frac{9}{4}} \times \left(\frac{1}{4}\right)^0$$
 
$$(2) \left(\frac{-2}{3}\right)^6 \div \left(\frac{-2}{3}\right)^4$$

$$\left( \frac{-2}{3} \right)^6 \div \left( \frac{-2}{3} \right)^4$$

[b] Find the solution set of the inequality, where  $x \in \mathbb{Z}: 4x + 5 \ge 1$ 

### [4] [a] Solve the equation: 3x - 3 = 9, where $x \in \mathbb{Q}$

[b] \* The sum of the age of 3 sisters now is 25 years. If the eldest was born before the middle by 3 years, and the middle was born before the youngest by 2 years. Find the age of each of them now.

## [5] [a] Find the result of: $\frac{3^3 \times 3^{-4}}{3^{-2} \times 3^{5}}$

- [b] One card is selected randomly from 8 cards numbered from 1 to 8, write down the sample space, then find the probability of each of the following events:
  - (1) Getting an odd number.
  - (2) Getting a number divisible by 3

## El-Gharbia Governorate

### East-Tanta Educational Directorate

### **Al-Salam Language School**

Answer the following questions:

- 1 Complete each of the following:
  - (1) The probability of the impossible event is .........
  - $(2)\sqrt{(-9)^2} = \dots$
  - (3) If the age of Ahmed now is X years, then his age after three years is ...... years.
  - (4) \*  $\frac{(-2)^6 \times 3^5}{3^4 \times 2^7} = \dots$
  - (5) If:  $3 \times 2 = 6$ , then  $6 \times 2 = \dots$
- 2 Choose the correct answer:
  - (1) \* Half the number 2<sup>20</sup> = ......
    - (a)  $2^{10}$

- (b)  $2^{21}$
- (c)  $2^{19}$
- (d) 40

- (a) If:  $-2 \times < 4$ , then ......
  - (a) X < -2
- (b) X < -6
- (c) X < 2
- (d) x > -2

- (3)  $2.37 \times 10^{-4} = \cdots$ 
  - (a) 0.00237
- (b) 0.000237
- (c) 23700
- (d) 0.0000237
- (4) As tossing a fair die once , the probability of appearance of an even number is ........
  - (a)  $\frac{1}{2}$

(c)  $\frac{1}{5}$ 

(d) =

- (5)  $3^7 \times 3^{-5} = \dots$ 
  - (a) 9
- (b) 9

(c) 3

- (d) 3
- [a] The length of a rectangle exceeds its width by 4 meters and its perimeter is 68 meters Find the dimensions of the rectangle.
  - [b] Solve the equation:  $3 \times -3 = 9$ , where  $X \in \mathbb{Q}$
- [a] Solve the inequality:  $4 \times + 5 \ge -3$  and represent the solution set on the number line where  $x \in \mathbb{N}$ 
  - **[b] Simplify**:  $2^3 + [4 + (2^2 \div 2)]$
- [5] [a] A card is drawn randomly from 10 cards numbered from 1 to 10 Find the probability of that card is numbered:
  - (1) An even number.
- (2) A number divisible by 5
- [b] Simplify:  $\sqrt{3 \times 7 15 \div 3}$

## El-Ismailia Governorate

### **Directorate of Education**

### El-Manar language School

Answer the following questions:

### 1 Choose the correct answer:

$$(1)\sqrt{(-5)^2} = \cdots$$

(a) - 5

(b) 25

(c) 10

(d)5

(2) If the probability of success of a student is  $\frac{1}{10}$ , then the probability of failure is .........

(a) 0.7

(b)  $\frac{1}{10}$ 

(c) 1

(d)  $\frac{3}{10}$ 

(3) 12 ÷ 3 + 3 × 2 = ········

(a) 10

(b) 4

(c) 24

(d) 1

(4)  $* 7.5 \times 10^{-3} = \dots$ 

(a) 0.075

(b) 0.0075

(c) 7500

(d) 0.00075

(5) The S.S. of X + 1 = 9 in N is ......

(a)  $\{9\}$ 

(b) {10}

(c)  $\{8\}$ 

(d) Ø

### 2 Complete each of the following:

(1) The probability of the impossible event = .......

(2) The multiplicative inverse of  $\left(\frac{-2}{3}\right)^2$  ......

(3)√16+9=4+.....

(4) If:  $3 \times = 6$ , then  $5 \times = \dots$ 

(5) \* The S.S. of the inequality: -2 x>4 in N is ........

# [3] [a] Find the result of : $\left(\frac{-2}{3}\right)^2 \times \sqrt{\frac{9}{4}} \times \left(\frac{-1}{4}\right)^{\text{zero}}$

[b] Answer the following:

If:  $a = \frac{-1}{2}$ , b = 2,  $c = \frac{3}{4}$ , then find the numerical value of:  $a^2 b^3 + b^2 c$ 

### 4 Find in Q the S.S of:

(1)  $4x - 1 \ge 7$ 

(2) 
$$2(X+5) = 16$$

[a] \* Two complementary angles , whose measures are 2  $\times$  and (2  $\times$  – 18°)

Find the measure of each of them.

[b] A box contains 2 red balls , 6 white balls and 4 green balls. A ball is drawn randomly. Find the probability that the drawn ball is:

(1) Red

(2) Green

(3) Black

## Assiut Governorate

### **Assiut Educational Zone**

### **Al-Tahreer Language School**

Answer the following questions:

1 Complete:

- (1) The multiplicative inverse of  $\sqrt{\frac{10}{25}}$  is ..........
- (2) The probability of the impossible event = ......
- (3) \* If:  $x \in \mathbb{Z}$ , then the solution set of the inequality:  $20 < 5 \times < 25$  is .......
- (4) If the age of Mona now is X years, then her age 5 years ago is ...... years.
- (5)  $3 \times 7 15 \div 3 = \cdots$

2 Choose the correct answer from the given ones:

- (1) If:  $(0.0005)^2 = 25 \times 10^n$ , then  $n = \dots$ 
  - (a) 4

(b) 8

(c) - 8

(d) - 6

- (2)  $\left(\frac{2}{3}\right)^{-2} = \dots$ 
  - $(a)\frac{4}{9}$

(b)  $\frac{9}{4}$ 

(3) Half the number  $2^{20} = \dots$ 

(a)  $2^{10}$ 

- (b) 2<sup>21</sup>
- (c)  $2^{19}$

(d) 40

(4) A letter is selected at random from the word "Nora" the probability of selecting the letter N is .....

(a)  $\frac{1}{4}$ 

(b)  $\frac{2}{4}$ 

(c)  $\frac{3}{4}$ 

(d)  $\frac{4}{4}$ 

(5) If X is an odd natural number then the next odd number directly is .........

- (a) X + 1
- (b) X + 2
- (c) 2 X + 1
- (d)  $2 \times$

3 [a] Find: (1)  $\left(\frac{-5}{8}\right)^0 \times \sqrt{6\frac{1}{4} \times \left(\frac{-2}{5}\right)^2}$ 

[b] Three consecutive even numbers are of sum 78 Find these numbers.

[4] [a] Solve the equation:  $3 \times + 5 = 26$ , where  $X \in \mathbb{Z}$ 

[b] A box contains 5 white , 4 black and 7 red balls , a ball is drawn randomly from the box. Calculate the probabilities of the following events:

- (1) The drawn ball is white.
- (2) The drawn ball is red.

[5] [a] Solve the inequality:  $4x-7 \ge 1$ , where  $x \in \mathbb{Q}$ 

[b] If:  $a = \frac{1}{2}$ , b = 2 and  $c = \frac{3}{4}$ , then find the numerical value of:  $a^2 b^3 + b^2 c$ 

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

## Qena Governorate

### **Qena Directorate of Education**

Answer the following questions:

### 1 Choose the correct answer:

- (1) \* The S.S. of the inequality:  $-2 \times <$  zero in  $\mathbb{Q}$  is .......
  - (a) Ø

(b) Q

(c) Q

(d) Z,

- (a) 0.00000032 = ·······
  - (a)  $3.2 \times 10^{-6}$
- (b)  $3.2 \times 10^6$
- (c)  $3.2 \times 10^{-7}$
- (d)  $3.2 \times 10^7$
- (3) If the age of Mohamed now is X years then his age after five years is ...... years.
  - (a) 5 X

- (b) X + 5
- (c) X 5
- (d)  $x^5$

- (4)  $\frac{1}{2}$  (2<sup>20</sup>) = ......
  - (a)  $2^5$

- (b)  $2^{10}$
- (c)  $2^{19}$
- (d)  $2^{18}$

- - (a)  $\frac{3}{2}$

- (b)  $\frac{-3}{2}$
- (c)  $\frac{2}{3}$
- $(d)^{\frac{-2}{3}}$

### 2 Complete each of the following:

- (1)  $2 + 3 \times 6 \div 3 = \cdots$
- (2)  $\left(\frac{2}{3}\right)^6 \div \left(\frac{2}{3}\right)^4 = \dots$
- (3) The probability of the impossible event = ......
- (4) \* If:  $2 \times + 3 = 27$ , then the value of  $\frac{1}{3} \times = \dots$
- (5) The multiplicative inverse of  $\sqrt{\frac{25}{64}}$  is ......

### [a] Find the solution set of each of the following in $\mathbb{Z}$ :

(1)  $2 \times 14 = 12$ 

- (2)  $3 X + 1 \le 7$
- [b] Simplify:  $\frac{5^6 \times 5^2 \times 5^3}{5^4 \times 5^5}$
- 4 [a] If:  $a = -\frac{2}{3}$ ,  $b = \frac{3}{4}$  and  $c = \frac{1}{2}$  Find the value of:  $(ab)^2 c^2$ 
  - [b] A card is drawn randomly from 10 cards numbered from 1 to 10 Find the probability of that card numbered by:
    - (1) An even number.
- (2) A number divisible by 5
- **5** [a] Find the value of :  $\left(\frac{5}{8}\right)^0 \times \sqrt{6\frac{1}{4} \times \left(-\frac{2}{5}\right)^2}$ 
  - [b] The sum of three consecutive numbers is 33 Find the three numbers.

### Model Examinations of the School Book

## Model

Answer the following questions:

### 1 Complete:

(1)  $2 \times 6 - 4 \div 2 = \dots$ 

(2) If:  $7-2 \times = 3$ , then  $\times = \dots$ 

(3) If:  $3 \times + 1 \ge 10$ , then  $\times \ge \dots$ 

(4) The standard form of the number  $0.7 \times 0.005 = \cdots$ 

(5) A class has 36 students, the number of boys are 20, if a student is chosen randomly, then the probability that the student is a girl = ......

### 2 Choose the correct answer:

1 The sum of the probabilities for all possible outcomes of a randomly experiment is .........

(a) zero

(b) 1

(c) > 1

(d) < 1

(2) If: 3 a =  $\sqrt{4}$  b, then  $\frac{a}{b}$  = ......

(a) 2:3

(b) 3:2

(c) 3:4

(d) 4:3

 $\left(\frac{-2}{3}\right)^{-3}$  equals .....

(a)  $\frac{-27}{8}$ 

(b)  $\frac{-8}{27}$ 

(c)  $\frac{8}{27}$ 

(d)  $\frac{27}{8}$ 

(4) There are 21 boys and 15 girls in a classroom, one pupil is chosen randomly, the probability that the chosen pupil is a girl = ......

(a)  $\frac{3}{12}$ 

(b)  $\frac{7}{12}$ 

(c)  $\frac{4}{7}$ 

(d)  $\frac{5}{6}$ 

(5)  $\sqrt{(-8)^2 + (-6)^2} = \dots$ 

(a) |-10|

(b)  $\pm 10$ 

(c) 14

(d) - 14

[3] [a] Simplify to the simplest form :  $\left(-\frac{3}{7}\right)^0 \times \left(\frac{-2}{5}\right)^2 \times \sqrt{6\frac{1}{4}}$ 

[b] Find the numerical value of the expression:

3 ab + 8 a  $\div$  (4b) when a = 4, b = -2

### 4 [a] Find in Q the S.S. of the following:

(1)  $3 \times + 1 = 25$ 

(2) 2x + 5 < 16

[b] The population of a city has been growing according to the rule:

 $y = 3 (1.02)^n$  million. Calculate the population that will be in 2 years in the standard form.

### A factory of a tire record the distance that traveled by a certain type of them before damage for 800 units of this type as following.

The distance in thousand (km)	Less than 50	50 to 100	More than 100 till 150	More than 150
The number of damage tire	80	120	280	320

### If you bought the type of this tyre, what is the probability of change it:

- (1) Before traveled 50 thousand km.
- (2) After traveled more than 100 thousand km.

## Model

### Answer the following questions:

### 1 Complete:

$$2\sqrt{\frac{16}{49}} = \cdots$$

- (3) The probability of impossible event = ·······
- (4) 1, 2, 3, 5, 8, ..... (In the same pattern)
- (5) If the probability that the student is absent in a school is 0.15, if the number of students of this school is 600, then the number of the present student that day is .......

### 2 Choose the correct answer:

(a) 
$$2^2$$

(b) 
$$2^8$$

(c) 
$$2^{15}$$

(d) 
$$2^{53}$$

(2) Which of the following the greatest? .......

(a) 
$$2.3 \times 10^4$$

(b) 
$$2.3 \times 10^5$$

(c) 
$$3.2 \times 10^4$$

(d) 
$$3.2 \times 10^5$$

(3) The side length of a square whose area  $9 \times 2 \text{ cm}^2$  is ...... cm.

(a) 
$$3 X$$

(b) 
$$3 x^2$$

(d) 
$$9 x^2$$

(4) Which of the following may be probability of an event? ......

$$(a) - 0.25$$

(5) If: -x > 4, then:

(a) 
$$X > -4$$

(b) 
$$X > 4$$

(c) 
$$X < -4$$

(d) 
$$X < 4$$

- [3] [a] Two integers number the smaller one is 2  $\times$  and the greater is 5  $\times$ , if the difference between them is 30 Find the two numbers.
  - [b] Find the value of  $\frac{5^{-4} \times 5^7}{5^3}$  in the simplest form.

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[a] Find in Q the S.S. of each of the following:

(1) 
$$(3 \times + 2) + 5 = 13$$

(2) 
$$2 \times + 15 < 19$$

[b] Find the value of the expression in simplest form:

$$\left(\frac{-1}{3}\right)^2 + \sqrt{\frac{64}{81}} - \left(\frac{3}{7}\right)^0$$

[a] If a regular die is thrown once and observed the number on upper face, find the probability of each of the following:

(1) Getting prime even number.

(2) Getting odd number less than 4

[b] If the length of a rectangle is twice its width, its area is 12.5 cm. Calculate its length, its width.

## Model

Answer the following questions:

1 Complete:

(1) The probability of the certain event = ......

(2)  $\frac{1}{9}$ ,  $\frac{1}{8}$ ,  $\frac{1}{7}$ ,  $\frac{1}{6}$ , ............ (In the same pattern)

(3) The S.S. in  $\mathbb{Q}$  for the equation:  $2 \times + 3 = 4$  is ......

(4) If:  $x = \frac{1}{2}$ ,  $y = \frac{1}{4}$ , then  $(x + y)^{-1} = \dots$ 

(5)  $0.00037 = 3.7 \times 10^{n}$ , the value of  $n = \dots$ 

2 Choose the correct answer:

1) The multiplicative inverse of the number:  $\sqrt{\frac{9}{16}}$  is .........

(a) 
$$\frac{-4}{3}$$

(b) 
$$\frac{-3}{4}$$

(c) 
$$\frac{3}{4}$$

(d) 
$$\frac{4}{3}$$

(2)  $\frac{x}{2}$  < 5 equivalent .....

(a) 
$$X < \frac{5}{2}$$

(a) 
$$X < \frac{5}{2}$$
 (b)  $X > \frac{5}{2}$ 

(c) 
$$X < 10$$

(d) 
$$X > 10$$

(3)  $3^{x} + 3^{x} + 3^{x} + 3^{x}$  equals .......

(b) 
$$3^{x+1}$$

(d) 
$$3 x^3$$

(4) There are 480 pupils in a school, 120 of them failed. A pupil is chosen at random, then the probability that the pupil is succeeded ......

(a) 0.25 %

(b) 0.75

(c) 0.8

(d) 0.667

(5) If: X = y, then  $\left(\frac{3}{5}\right)^{x-y} = \dots$ 

(a) 0

(b) 1

(c)  $\frac{3}{5}$ 

... (d)  $\frac{5}{3}$ 

- [3] [a] What is the number which if we add it to its three times, the result is 28?
  - [b] If the area of a Square equals the area of a triangle whose base length is 9 cm, its height is 8 cm. Find the Side length of the square.
- [4] [a] Find in Q the solution set of the following:

① 
$$3 \times + 5 = 11$$

(2) 
$$2 X + 3 \le 7$$

- [b] If the distance (s) between the sun and the earth is  $1.44 \times 10^8$  km. and the light velocity (v) is  $3 \times 10^8$  m/sec. Calculate the elapsed time (t) that the light takes to reach from the sun to the earth. (given that :  $s = v \times t$ )
- [5] [a] Find the result of the expression:  $(5.4 \times 10^4) + (3.7 \times 10^5)$  in the form a  $\times 10^n$ where n is integer number.
  - [b] A coin is tossed twice calculate the probability:

1) The two faces are similar.

(2) Appearance only one tail.

## Model

### Answer the following questions:

### 1 Complete:

- (1) When a coin is tossed once then the probability of appearance of a head is ........
- ② $\frac{1}{1000}$ ,  $\frac{1}{100}$ ,  $\frac{1}{10}$ , .......... (In the same pattern)
- (4) The additive inverse of  $\sqrt{\left(-\frac{2}{5}\right)^2}$  is ......
- (5)  $\frac{1}{2}$ ,  $\frac{3}{4}$ ,  $\frac{7}{8}$ ,  $\frac{15}{16}$ , .....
- 2 Choose the correct answer:
  - (1) The S.S. of the equation : x + 3 = 3 in  $\mathbb{N}$  is ......
    - (a) Ø

- (b)  $\{0\}$
- $(c) \{3\}$
- $(d) \{6\}$
- (2) The number which in the standard form between the following numbers is ..........
  - (a)  $11 \times 10^8$
- (b)  $9.7 \times 10^{-5}$
- (c)  $10.3 \times 10^{-3}$
- (d)  $0.87 \times 10^8$

(3) If a coin is tossed 160 times then the approximate expected number of the appearance of a head is .........

(a) 60

(b) 78

(c) 90

(d) 159

(4) The number  $\sqrt{0.09}$  is ......

- (a) natural.
- (b) positive integer.
- (c) negative integer.
- (d) rational.

(5) If:  $\frac{6x}{5} = -2$ , then  $x^2 = \dots$ 

- (a)  $\frac{-25}{9}$
- (b)  $\frac{5}{9}$

- (c)  $\frac{25}{9}$
- (d)  $\frac{25}{3}$

[3] [a] If:  $x = \frac{3}{4}$ ,  $y = \frac{-3}{2}$  Find the numerical value of the expression  $\left(\frac{x^2}{v^3}\right)^2$ 

[b] The sum of two natural number is 15 and the difference between them is 5 Find the two number.

[4] [a] Find in Q the solution set for each of the following:

 $\bigcirc 3 x + 2 = 8$ 

(2)4x-3<7

[b] If  $\frac{3}{4}$  of the area of a square is  $1\frac{11}{64}$  m<sup>2</sup>. Find its side length.

[5] [a] A coin is tossed twice Calculate the probabilities:

① The appearance of at least one head. ② The appearance of at most one head.

[b] Find the value of  $\left(\frac{7^4 \times 7^{-2}}{7^3}\right)^{-2}$ 

### Model

Answer the following questions:

1 Complete :

1 In the experiment of tossing a die once then the probability of appearance even number is ..........

(2) If:  $\frac{x}{y} = \frac{7}{2}$ , then  $\frac{2x}{7y} = \cdots$ 

(4) The result of the expression :  $\left(\frac{-1}{2}\right)^2 - \left(\frac{-1}{2}\right)^3 = \cdots$ 

(5) Quarter of 4<sup>20</sup> equals ......

### 2 Choose the correct answer:

- (1) The S.S. of the inequality x < 2 in  $\mathbb{N}$  is ......
  - (a)  $\{0\}$
- (b) {1}
- (c)  $\{0, 1\}$
- (d) Ø

- ② If:  $\frac{26}{x} + 1 = 14$ , then  $x = \dots$ 
  - (a) 2

(b) 10

(c) 13

(d) 20

- (3) If:  $5 \times = 35$ , then  $2 \times + 1 = \dots$ 
  - (a) 7

(b) 8

(c) 15

(d) 71

### (4) In the opposite figure:

The probability that the pointer stop at a number greater than 6 equals ......

(c)  $\frac{3}{8}$ 

- (5)  $\sqrt{100 (-6)^2} = \cdots$ 
  - (a) 4

(b) 8

(c) - 8

(d) 16



[b] If: 
$$x = -\frac{1}{2}$$
,  $y = \left| \frac{-3}{4} \right|$ , find the numerical value of  $\left( \frac{y}{x^2} \right)^{-2}$ 

[4] [a] Find in Q the solution set of each of the following:

$$(1)3-4x=-5$$

(2) 
$$2x - 1 \ge 5$$

[b] Simplify: 
$$\frac{n}{2}$$
 [3 n - 6] +  $\frac{1}{2}$  [6 - 2 n], then find its value when n = 1

[a] The sum of the age of 3 sisters now is 25 years. If the eldest was born before the middle by 3 years, and the middle was born before the youngest by 2 years.

Find the age of each of them now.

- [b] A box contains 4 white , 5 red and 6 blue balls. A ball is drawn randomly from the box. Calculate the probabilities of the following events.
  - (1) The ball is red.

② The ball is white or red.

### **School Examinations**

## Cairo Governorate

### Maadi Educational Zone

### Victory College Maadi

### Answer the following questions:

### 1 Choose the correct answer:

(1) The multiplicative inverse of  $\left(\frac{-3}{4}\right)^2$  is .........

(a) 
$$\left(\frac{4}{3}\right)^2$$

(b) 
$$-\left(\frac{4}{3}\right)^2$$
 (c)  $\left(\frac{3}{4}\right)^2$ 

(c) 
$$\left(\frac{3}{4}\right)^2$$

$$(d) - \left(\frac{3}{4}\right)^2$$

(2) Ahmed's age 3 years ago was X, then his age now is ...... years.

(a) 
$$X + 3$$

(b) 
$$x - 3$$

(c) 
$$3 - X$$

(d) 
$$3 \times$$

(a) 
$$\frac{2}{5}$$

(b) 
$$\frac{5}{2}$$

(4) A regular die is rolled once, the probability of getting a number less than 3 is .........

(a) 
$$\frac{1}{2}$$

(b) 
$$\frac{1}{3}$$

(c) 
$$\frac{2}{3}$$

(d) 
$$\frac{1}{6}$$

(5) The solution set of :  $-2 \times + 1 = -3$  in  $\mathbb{Z}$  is .......

(a) 
$$\{2\}$$

(b) 
$$\{-2\}$$

(c) 
$$\{-4\}$$

### 2 Complete each of the following:

- 1) The additive inverse of  $\left(\frac{-5}{7}\right)^2$  is ........
- (2) The probability of the impossible event = ......

$$(3)\sqrt{16+9}=4+\cdots$$

(4) If: 
$$x + 3 = 5$$
, then  $3x = \dots$ 

(5) If: 
$$0.000035 = 3.5 \times 10^k$$
, then  $k = \dots$ 

### [3] [a] Find the S.S. of: $5 \times +3 > 15 + \times$ , where $\times \in \mathbb{Q}$

[b] Simplify: 
$$\frac{a^5 \times a^7}{a^8}$$

4 [a] If: 
$$a = \frac{-1}{2}$$
,  $b = \frac{3}{4}$ ,  $c = \frac{-3}{2}$ 

Find the value of : 
$$a^3 \div b^2 c^2$$

[b] A box contains 8 white , 7 black and 5 red balls. A ball is drawn randomly from the box.

### Find the probability of the following events:

(1) The ball is red.

(2) The ball is not black.

- [5] [a] Find the solution set of:  $3 \times + 17 = 38 \times \times \in \mathbb{Q}$ 
  - [b] Find the result in the simplest form :  $\frac{4}{3} \times \sqrt{\frac{9}{25}} \times \left(\frac{-1}{2}\right)^2$

## Cairo Governorate

### **El-Zeitoun Directorate**

Answer the following questions:

1 Choose the correct answer:

(1) Third of 3<sup>20</sup> is ......

- (a)  $3^{10}$
- (b)  $3^{19}$
- (c)  $3^{18}$
- (d) 60

- (2)  $\sqrt{\frac{25}{36}} = \dots$ 
  - $(a) \frac{\pm 5}{6}$
- (b)  $\frac{-5}{6}$
- (c)  $\frac{5}{6}$
- (d) otherwise.
- (3) As throwing a fair die once, the probability of appearance of prime number on the upper face is .....
  - (a)  $\frac{1}{2}$
- (b)  $\frac{1}{6}$
- (c)  $\frac{5}{6}$
- (d)  $\frac{1}{3}$

- (4) If:  $2 \times = 12$ , then  $3 \times = \cdots$ 
  - (a) 6
- (b) 4
- (c)3
- (d) 18

- (5) If:  $(0.0005)^2 = 25 \times 10^n$ , then  $n = \dots$ 
  - (a) 4
- (b) 8
- (c) 8
- (d) 6

### 2 Complete each of the following:

- (1) The probability of impossible event = .......
- (2) The multiplicative inverse of  $\left(\frac{-2}{3}\right)^2$  is .........
- (3) If the age of a man now is X years, then his age after 5 years is .........
- (4)  $3 \times 7 15 \div 3 = \cdots$
- (5) The solution set of :  $2 \times = 10$  in N is ......
- 3 Simplify each of the following:

(1) 
$$\left(\frac{-2}{3}\right)^2 \times \sqrt{\frac{9}{4}} \times \left(\frac{2}{7}\right)^0$$

$$(2)^{5} \times (-2)^{4}$$

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4 Find the solution set in Z:

(1) 
$$2 \times + 14 = 12$$

(2) 
$$3 X + 1 \le 7$$

[5] [a] If: 
$$a = \frac{-2}{3}$$
,  $b = \frac{3}{4}$ ,  $c = \frac{1}{2}$ 

Find the numerical value of  $(ab)^2 - c^2$ 

[b] A box contains 3 white , 5 black and 7 red balls. A ball is drawn randomly.

Find the probability of getting:

(1) red ball.

2 not white ball.

## Cairo Governorate

### Hel. Educ. Administration

St. Joseph's School

Answer the following questions:

1 Choose the correct answer:

- (1) If a coin is flipped once , then the probability of appearance of a tail = .........
  - (a) 1

- (b) 0.5
- (c)0

(d) 2

(2) If: X + 8 = 12, then:  $9X = \dots$ 

(a) 1

- (b) 9
- (c)36
- (d) 72

(3) If:  $-2 \times \ge 1$ , then:  $\times \cdots$ 

- (a) ≥  $-\frac{1}{2}$  (b) ≤  $-\frac{1}{2}$
- (c) ≥ -2
- $(d) \ge -1$

(4) If:  $(AB)^2 = 9$ ,  $(BC)^2 = 25$  and  $B \in \overline{AC}$ , then the length of  $\overline{AC} = \cdots \cdots$  cm.

- (a) 34
- (b) 2

(c) 8

(d) 16

(5) If: X = y, then  $\left(\frac{4}{9}\right)^{X-y}$ equals .....

(a) 1

- (b) 0
- (c)  $\frac{4}{9}$
- (d)  $\frac{9}{4}$

2 Complete:

- (1) The set {2,3,5} is used in writing a 2-digit number, the probability of the event: both of the two digits are even = ......
- (2) 0.0007 in the standard form (a  $\times$  10<sup>n</sup>, n  $\in$  Z) is 7  $\times$  .......
- (3)  $2 \times 6 4 \div 2 = \cdots$
- (4)  $(a^{-1})^{-3} = a$  .....
- (5) If:  $\chi^2 + y^2 = 7$ , then the value of  $\frac{\chi^3 y + \chi y^3}{\chi y} = \cdots$

[3] [a] Solve the equation:  $5 \times + 8 = 13 - 2 \times$ , where  $\times \in \mathbb{Q}$ 

[b] Put the result of:  $\left(-\frac{1}{2}\right)^3 \div \left[8 \times \left(-\frac{1}{2}\right) \times \frac{3}{4}\right]$  in the simplest form.

[4] [a] If:  $a = -\frac{1}{2}$ , b = 2, and  $c = \frac{3}{4}$ , Find the numerical value of:  $a^3b^2 + b^2c - 8$  abc

[b] If: x = 0.000625, find  $\sqrt{x}$  in the standard form (a × 10<sup>n</sup>, n  $\in \mathbb{Z}$ )

[5] [a] Solve the inequality:  $3 \times -1 \le 2 \times +3$ ,  $x \in \mathbb{Q}$ 

[b] A bag contains 40 cards numbered from 1 to 40, Mirna picked one randomly, it was an even number. She picked another one without replacing the first card. Find the probability to get a card with an odd number.

# Giza Governorate

Experimental Language Schools

### Answer the following questions:

1 Choose the correct answer:

(1)  $2 x^{-1} = \cdots$ 

(a) - 2X

- (b) 2 X
- (c)  $\frac{1}{2x}$
- (d)  $\frac{2}{x}$

(2) The additive inverse of  $\left(-\frac{2}{5}\right)^{\text{zero}}$  is ......

- (a)  $\frac{2}{5}$
- (b)  $-\frac{2}{5}$
- (c) 1
- (d) 1

(3) The probability of the impossible event = ......

(a) 1

- (b) 0
- (c)  $\frac{1}{2}$
- (d) 1

(4) If: x-2=3, then the value of  $5x=\cdots$ 

- (a) 5
- (b) 3
- (c) 25
- (d) 10

(5)  $3 \times 2 - 16 \div 8 = \cdots$ 

- (a) 4
- (b) 6
- (c) 2
- (d) 3

### 2 Complete:

 $(1)\sqrt{3^2+4^2}=3+\cdots$ 

(2)  $\left(-\frac{3}{2}\right)^4 \div \left(\frac{3}{2}\right)^2 = \cdots$ 

(3) If: x + 1 > 3, then the solution set in  $\mathbb{N} = \dots$ 

(4) When a coin is tossing once, then the probability of getting a head = ........

(5) If:  $0.00032 = 3.2 \times 10^n$ , then  $n = \dots$ 

3 [a] Simplify:  $\frac{x^3 \times x^4}{x^5}$ 

- , then find the numerical value of the result at x = -3
- [b] Find in  $\mathbb{Q}$  the solution set of the inequality :  $2 \times -3 \le 1$
- [4] [a] Find the result in the simplest form :  $\left(\frac{3}{4}\right)^{\text{zero}} \times \sqrt{\frac{81}{64}} \times \left(-\frac{2}{3}\right)^3$ 
  - [b] Find in  $\mathbb{Q}$  the solution set of the equation :  $2 \times -3 = 6$
- [5] [a] Two integers the smaller one is 3  $\times$  and the greater is 5  $\times$ . If the difference between them is 20 find the two numbers.
  - [b] A fair die rolled once , find sample space and calculate the probability of rolling
    - An even number.

# (2) A number greater than 1

# Giza Governorate

### Inspection of mathematice

### **Experimental Directorate**

Answer the following questions:

- 1 Choose the correct answer:
  - (1) Half the number  $2^{20} = \cdots$ 
    - (a)  $2^{10}$
- (b)  $2^{21}$
- (c)  $2^{19}$
- (d) 40

- (2) If:  $-2 \times < 4$ , then ......

  - (a) x < -2 (b) x < -6
- (c) x < 2
- (d) x > -2

- (3)  $2.37 \times 10^{-4} = \dots$ 
  - (a) 0.00237
- (b) 0.000237
- (c) 23700
- (d) 0.0000237
- (4) As tossing a fair die once, the probability of appearance of an even number is ........
- (a)  $\frac{1}{2}$
- $_{*}(b) \frac{1}{4}$
- (c)  $\frac{1}{5}$
- (d)  $\frac{5}{6}$

- (5)  $3^7 \times 3^{-5} = \dots$ 
  - (a) 9
- (b) 9
- (c) 3
- (d) 3

2 Complete:

- (1) The multiplicative inverse of  $\sqrt{\frac{10}{2.5}}$  is ......
- (2) The probability of the impossible event = ........
- (3) If:  $x \in \mathbb{Z}$ , then the solution set of the inequality:  $20 < 5 \times < 25$  is .......

- (4) If the age of Mona now is X years, then her age 5 years ago is ...... years.
- (5) 3 × 7 15 ÷ 3 = ·······
- 3 [a] Find :

$$\textcircled{1}\left(\frac{-5}{8}\right)^0 \times \sqrt{6\frac{1}{4}} \times \left(\frac{-2}{5}\right)^2$$

② 
$$\frac{3^4 \times 3^3}{3^6}$$

- [b] Three consecutive even numbers their sum is 78 Find these numbers.
- [4] [a] Solve the equation:  $3 \times + 5 = 26$ , where  $\times \in \mathbb{Z}$ 
  - [b] A box contains 5 white , 4 black and 7 red balls. A ball is drawn randomly from the box. Calculate the probabilities of the following events:
    - (1) The drawn ball is white.

- ② The drawn ball is red
- [5] [a] Solve the inequality:  $4 \times -7 \ge 1$ , where  $\times \in \mathbb{Q}$ 
  - [b] If:  $a = \frac{1}{2}$ , b = 2 and  $c = \frac{3}{4}$ , then find the numerical value of:  $a^2b^3 + b^2c$

# Alexandria Governorate

### **East Education Zone**

### **Inspectorate of Math**

Answer the following questions:

- 1 Choose the correct answer:
  - (1) The S.S. of equation: x + 5 = 5 in N is ......
    - (a) Ø
- (b)  $\{0\}$
- (c)  $\{5\}$
- (d)  $\{10\}$

- (2) The S.S. of inequality  $1 < x \le 3$  is ......
  - (a) Ø
- (b)  $\{3\}$
- (c)  $\{2,3\}$  (d)  $\{1,3\}$
- (3) The number which is in the standard form between the following numbers is ........
  - (a)  $1.1 \times 10^8$
- (b)  $27 \times 10^{-5}$
- (c)  $10 \times 10^{-3}$
- (d)  $0.87 \times 10^8$

- (4) The number  $\sqrt{0.09}$  is ......
  - (a) natural.
- (b) positive integer. (c) negative integer. (d) rational.
- (5) The additive inverse of  $\sqrt{\frac{9}{25}}$  is ......
  - (a)  $\frac{-3}{5}$
- (b)  $\frac{3}{5}$
- (c)  $\frac{9}{25}$

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى والعمولية العمل المعاصر المعاصر

### 2 Complete:

- (1) The probability of impossible event = .......
- (2)  $\left(\frac{-4}{5}\right)^{zero} = \cdots$
- (3) If:  $0.0027 = 2.7 \times 10^n$ , then  $n = \dots$
- (4)  $\frac{1}{1000}$ ,  $\frac{1}{100}$ ,  $\frac{1}{10}$ , ..... (in the same pattern).
- (5) When a coin is tossed once, then the probability of appearance of a head is ........
- [3] [a] If:  $x = \frac{3}{4}$ ,  $y = \frac{-3}{2}$ , then find the numerical value of  $\left(\frac{x^2}{y^3}\right)^2$ 
  - [b] Find the value of expression  $12 \times 2^2 \div 24 + 3^2$
- 4 If:  $x \in \mathbb{Q}$  Find the S.S. of each of the following:
  - $\bigcirc$  4  $\times$  + 3 = 11

- (2)6x-2<7
- 5 A card is drawn randomly from 8 cards are numbered from 1 to 8, find the probability of each of the following event:
  - (1) Getting even number greater or equal to 6
  - (2) Getting number =  $2^n$  ( $n \in \mathbb{Z}$ , n < 4)

# Alexandria Governorate

### Borg Elarab Admin.

Answer the following questions:

- 1 Complete each of the following:
  - (1) If:  $x = \frac{1}{4}$ ,  $y = \frac{1}{8}$ , then  $(x y)^{-1} = \cdots$
  - (2) The probability of the certain event = ......
  - (3)  $0.00037 = 3.7 \times 10^n$ , the value of  $n = \dots$
  - (4) 3  $\chi^0 = \cdots$
  - $(5)\sqrt{(-9)^2} = \cdots$

### 2 Choose the correct answer:

- (1) If:  $2^4 \times 3^4 = \cdots$ 
  - (a)  $5^4$
- (b)  $6^4$
- (c)  $6^8$
- (d)  $6^{16}$
- (2) The side length of square whose area  $\sqrt{9x^2}$  cm<sup>2</sup> is ...... cm.
  - (a) 3x
- (b) 3  $\chi^2$
- (c) 9X
- (d) 9  $\chi^2$
- (3) The multiplicative inverse of the number  $\sqrt{\frac{9}{16}}$  is .......
  - (a)  $\frac{-4}{3}$
- (b)  $\frac{-3}{4}$
- (c)  $\frac{3}{4}$
- (d)  $\frac{4}{3}$

- (4) The S.S. of:  $-2 \times + 1 = -3$  in  $\mathbb{Z}$  is ......

  - (a)  $\{2\}$  (b)  $\{-2\}$  (c)  $\{-4\}$
- $(d) \emptyset$

- (5)  $\left(\frac{-1}{3}\right)^{-1} = \dots$ 
  - (a)  $\frac{-1}{3}$  (b) -3
- (c)3

(d)  $\frac{1}{3}$ 

- [3] [a] Find the result of:  $\frac{2^3 \times 2^{-4}}{2^{-2} \times 2^5}$ 
  - [b] Find the S.S. of the inequality:  $3 \times -2 > \times +4$ , where  $\times \in \mathbb{Q}$
- [4] [a] Simplify:  $2^3 + [4 + (2^2 \div 2)]$ 
  - [b] Adie is tossing once , find the probability of the event (A) appearing an odd number on the upper face.
- [5] [a] Find the value of :  $\left(\frac{5}{8}\right)^0 \times \sqrt{6\frac{1}{4} \times \left(-\frac{2}{5}\right)^2}$ 
  - [b] If:  $x = -\frac{1}{2}$ ,  $y = \frac{3}{4}$ , Find the numerical value of:  $x^3$  y<sup>2</sup>

# El-Kalyoubia Governorate

### Inspectorate of Math

Answer the following questions:

- 1 Choose the correct answer:
  - ① Quarter of the number  $4^{20} = \cdots$ 
    - (a)  $4^5$
- (b)  $4^{10}$
- (c)  $4^{19}$
- (d)  $2^{10}$

- (2) 2.37 × 10<sup>-4</sup> = ·······
  - (a) 0.00237
- (b) 0.000237
- (c) 23700
- (d) 0.0000237
- (3) The age of Ahmed now is X years, then his age 5 years ago is ...... years.
  - (a) 5 X
- (b) 5 + X
- (c) 5 X
- (d) X-5

- (4) If: -x < 3, then ......
  - (a) X > 3
- (b) x > -3
- (c) x < 3
- (d) X < -3

- (b)  $\frac{-2}{3}$
- (c)  $\frac{2}{3}$
- (d)  $\frac{4}{9}$ .

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى

2 Complete :

- (1) The probability of the impossible event = ........
- (a)  $3 \times 4 21 \div 3 = \cdots$
- (3) The additive inverse of the number  $\left(\frac{-4}{5}\right)^2 = \cdots$
- (4) If a coin is tossed once the probability of appearance of a head = .........
- (5)  $\frac{1}{9}$ ,  $\frac{1}{8}$ ,  $\frac{1}{7}$ , ...... (in the same pattern).

[3] [a] Find in the simplest form:  $\frac{7^{-3} \times 7^5}{7^2}$ 

- [b] If the regular die is thrown once and observed the number on upper face, find the probability of each of the following:
  - (1) Getting even number

(2) Getting odd number less than 4

[4] [a] Find the solution set of the following equation in  $\mathbb{Q}: 3 \times + 9 = 11$ [b] If:  $x = \frac{-3}{2}$  and  $y = \frac{-4}{3}$ , then find in the simplest form  $\left(\frac{x}{y}\right)^2$ 

[5] [a] Find the solution set of the following inequality in  $\mathbb{Z}$ :  $2 \times + 3 \leq 7$ 

[b] If:  $\overline{XY}$  is a line segment such that  $(XY)^2 = 25$  cm<sup>2</sup> and z is a midpoint of  $\overline{XY}$ Calculate the length of XZ

El-Monofia Governorate

El-Bagor Educational zone

Answer the following questions:

1 Choose the correct answer:

- $\bigcirc 8 + 14 \div 2 5 = \cdots$ (a) 6
- (c) 10
- (d) 12

(2)  $\sqrt{10^2 - 6^2} = \dots$ 

- (a) 4
- (b) 8
- (c)  $\pm 4$
- $(d) \pm 8$

 $3^7 + 3^7 + 3^7 = \cdots$ 

- (a)  $3^7$
- (b)  $3^{21}$
- (c)  $(27)^7$
- $(d) 3^8$
- (4) In an experiment of throwing a regular die once , the probability of appearance a number greater than 6 is ......
  - (a) zero
- (b) 1
- (c)  $\frac{1}{6}$
- (d)  $\frac{1}{4}$
- (5) The multiplicative inverse of  $\left(\frac{-3}{5}\right)^2$  is ......
  - (a)  $\frac{9}{25}$
- (b)  $\frac{-5}{3}$
- (c)  $\frac{25}{9}$
- (d) 1 ...

كراسة المعاصر رياضيات (لغات) / ١ إعدادي / تيرم ٢ (٢ : ١٠)

### 2 Complete the following:

- (1)  $\frac{1}{8}$ ,  $\frac{1}{7}$ ,  $\frac{1}{6}$ ,  $\frac{1}{5}$ , ..... in the same pattern.
- (2) If:  $\frac{x}{y} = \frac{8}{5}$ , then  $\frac{5x}{8y} = \dots$
- (3) If the standard form of the number  $0.00057 = 5.7 \times 10^n$ , then  $n = \dots$
- (4) The probability of the certain event = ......
- (5) The S.S. of: -x > 1 in  $\mathbb{Z}$  is ......

# [3] [a] Put the expression: $\left(\frac{-2}{5}\right)^2 \times \sqrt{6 \frac{1}{4} \times \left(\frac{-5}{8}\right)^{\text{zero}}}$ in the simplest form.

[b] Find in  $\mathbb{Q}$  the solution set of the following inequality:  $3 \times + 8 \le 1$ 

### [4] [a] Find in $\mathbb{Q}$ the solution set of the following equation: $2 \times 4 = 17$

[b] A man's age now is three times son's age and after five years, the sum of their ages will be 58 years, what the age of each now?

[5] [a] If: 
$$x = \frac{-3}{2}$$
 and  $y = \frac{3}{4}$ . Find the numerical value of expression  $\left(\frac{x^3}{y^2}\right)^2$ 

- [b] A box contains 4 white , 5 red and 6 blue balls. A ball is drown randomly from the box. Calculate the probabilities of the following events:
  - (1) The ball is red.
- (2) The ball isn't blue.
- 3 The ball is green.

# Port Said Governorate

### **Education Directorate**

### South Education Administration

### Answer the following questions:

### 1 Complete:

$$1\sqrt{9+40} = \cdots$$

- (2) The probability of the impossible event = ........
- (3) The additive inverse of  $(\frac{-2}{3})^0$  is .......

**4** 
$$2 \times 6 - 4 \div 2 = \cdots$$

(5) If: 
$$x + 9 = 11$$
, then  $7x = \dots$ 

# 2 Choose the correct answer:

(1) 
$$2^3 \times 2^5 = \cdots$$

(a) 
$$2^2$$

(b) 
$$2^8$$

(c) 
$$2^{15}$$

(d) 
$$2^{35}$$

(2) The multiplicative inverse of the number 
$$\sqrt{\frac{4}{25}}$$
 is:.......

(a) 
$$\frac{2}{25}$$

(b) 
$$\frac{25}{2}$$

(c) 
$$\frac{5}{2}$$

∴ (d) 
$$\frac{2}{5}$$

(3)  $10^{-3} = \frac{1}{}$ 

- (a) 30
- (b) 1000
- (c)  $10^2$
- (d) 31

(4) The number 600000 in the standard form  $a \times 10^n$ ,  $n \in \mathbb{Z}$  is .......

- (a)  $6 \times 10^5$
- (b)  $6 \times 10^4$
- (c)  $6 \times 10^6$
- (d)  $6 \times 10^{10}$

(5) The S.S. of the inequality : x < 2 in  $\mathbb{N}$  is ......

- (a)  $\{0\}$
- (b)  $\{1\}$
- (c)  $\{0,1\}$
- (d)  $\{0, 1, -1, ...\}$

Find in Q the solution set of each of the following in:

$$(1) - 3 + x = 5$$

[4] [a] If:  $x = \frac{1}{4}$ ,  $y = \frac{1}{8}$  Find the numerical value of:  $(x + y)^{-1}$ 

[b] Simplify to the simplest form :  $(\frac{-3}{7})^0 \times (\frac{-2}{5})^2 \times \sqrt{\frac{25}{4}}$ 

[a] Find the product:  $3 \text{ ab}^2 \times 2a^2b^3$ 

[b] A card is drawn randomly from 10 cards numbered from 1 to 10, then calculate the probability of drawing.

(1) Card carries an odd number greater than 10

- (2) Card carries an even number and less than 10
- (3) Card carries a prime number.

# Kafr El-Sheikh Governorate

General Math Supervision ELS

Answer the following questions:

1 Choose the correct answer:

- (1) 0.00000092 = .....
  - (a)  $9.2 \times 10^{-6}$  (b)  $9.2 \times 10^{6}$
- (c)  $9.2 \times 10^{-7}$
- (d)  $9.2 \times 10^7$

(2)  $\frac{1}{3}$  of  $3^{30} = \cdots$ 

- (a)  $3^5$
- (b)  $3^{10}$
- (c)  $3^{27}$
- (d)  $3^{29}$

(3)  $\sqrt{16+9} = 4 + \dots$ 

- (a) 1
- (b) 3
- (c) 5
- (d) 25

(4) As tossing a coin once. The probability of appearance of a head is ......

- (a)  $\frac{1}{2}$
- (b)  $\frac{5}{6}$
- (c)  $\frac{1}{3}$
- (d)  $\frac{1}{6}$

(5) If: X = y, then  $5^{y-X} = \dots$ 

- (a) zero
- (b) 9
- (c) 5
- (d) 1

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

### 2 Complete each of the following:

- (1) The S.S. of the inequality:  $-x \le -4$  in  $\mathbb{N}$  is x 4
- (2) The multiplicative inverse of  $\sqrt{81} = \cdots$
- (3) If: x + 7 = 10, then the value of  $4x = \dots$
- (4)  $2 \times 6 4 \div 2 = \cdots$
- (5) The probability of success of a students is 85 %, then the probability of his failure is .....

### [3] [a] Solve the equation: $3 \times -5 = 4$ (Where $X \subseteq \mathbb{Z}$ )

[b] Solve the inequality:  $-2x-3 \ge 1$  (Where  $x \in \mathbb{Z}$ ) and represent the solution on number line.

### 4 Find each of the following:

$$\bigcirc \left(\frac{4}{5}\right)^2 \times \sqrt{\frac{25}{16}} \times \left(\frac{1}{4}\right)^0$$

$$(-3)^6 \times (3)^{-3}$$

[5] [a] If: 
$$x = \frac{1}{2}$$
,  $y = \frac{4}{5}$ ,  $z = \frac{5}{2}$ , then find  $x^2$  y z

[b] A box contain 10 balls numbered from 1 to 10 If a ball is drawn randomly, then find:

- The probability of getting a number is divisible by 7
- (2) The probability of getting an even number.
- (3) The probability of getting a number less than 8

# 12 Beni Suef Governorate

### Directorate Language School

### **Education Administration**

### Answer the following questions:

### 1 Choose the correct answer:

① 
$$2^7 \times 3^7 = \cdots$$

(a) 
$$5^7$$

(b) 
$$6^7$$

(c) 
$$6^{14}$$

$$(2)(\frac{1}{3})^{-2} = \cdots$$

(a) 
$$\frac{1}{9}$$

(c) 
$$-\frac{1}{9}$$

 $(3)\left(-\frac{3}{7}\right)^7 \div \left(\frac{3}{7}\right)^5 = \cdots$ 

(a) 
$$\frac{9}{49}$$
 (b)  $-\frac{9}{49}$  (c)  $\pm \frac{9}{49}$ 

(b) 
$$-\frac{9}{49}$$

(c) 
$$\pm \frac{9}{49}$$

(d) 
$$\frac{3}{7}$$

(4)  $\pm \sqrt{\frac{4}{9}} = \dots$ 

(a) 
$$-\frac{4}{9}$$
 (b)  $-\frac{2}{3}$ 

(b) 
$$-\frac{2}{3}$$

(c) 
$$\pm \frac{2}{3}$$

(d) 
$$\frac{2}{3}$$

(5) If: -x < 3, then ......

(a) 
$$X > 3$$

(b) 
$$x < -3$$

(c) 
$$X < 3$$

(d) 
$$x > -3$$

2 Complete:

(1) If:  $0.00037 = 3.7 \times 10^n$ , then the value of  $n = \dots$ 

(2) If: x + 9 = 11, then the value of  $7x = \dots$ 

(3) The multiplicative inverse of  $\sqrt{\frac{25}{36}}$  is ..... in its simplest form.

(4) The probability of the impossible event = ......

(5) If a coin is tossed once , then the probability of appearance of a head = .........

3 Find in Q the solution set of each of the following :

① 
$$4x-1 \ge 7$$

(2) 
$$2(x+4) = 15$$

[4] [a] If:  $a = \frac{-1}{2}$ , b = 2 and  $c = \frac{3}{4}$ , then find in simplest form the numerical value of:  $a^2b^3 + b^2c$ 

[b] Find the value of the following expression in simplest form:  $144 - 8 \div 2^3$ 

[5] [a] Find the value of the expression in simplest form :  $\frac{7^{-2} \times 7^5}{7^3}$ 

[b] One card is selected randomly from 10 cards numbered from 1 to 10 Find the probability of the following events:

Getting an even number.

(2) Getting a number divisible by 5

El-Menia Governorate

**El-Minia Educational Directorate** 

Answer the following questions:

1 Choose the correct answer:

(1) If 
$$\left(\frac{4}{9}\right)^x = \left(\frac{9}{4}\right)^4$$
, then  $x = \dots$ 

(a) zero

(b) 1

(c) 4

···(d) -4

- (2) The probability of the impossible event = ........
  - (a) zero
- (b) 1
- (c) Ø
- (d)  $\frac{1}{2}$

- (3) The half of the number  $2^{20} = \cdots$ 
  - (a)  $2^{40}$
- (b)  $4^{20}$
- (c)  $2^{19}$
- (d)  $2^{21}$

- (4)  $(7x)^{zero} = \cdots$  where  $x \neq zero$ .
  - (a) 1

- (b) zero
- (c) 5
- (d) 5
- (5) The number 750000 is written in its scientific notation =  $7.5 \times 10^{n}$ , n = ......
  - (a) 4

- (b) 5
- (c) 4
- (d) 5

### 2 Complete the following:

- (1) If the probability of success of a student is 0.7, then the probability of his failure = .....
- (2) √25-9 = ········
- (3) 7 3 × 2 + 6 = .....
- (4) If:  $-2 \times > -8$ , then  $\times < \cdots$
- (5) The S.S of the equation  $3 \times = 6$  in N is ......
- [3] [a] Find the solution set of the inequality:  $3 \times -5 > 13$ , where  $\times \in \mathbb{N}$ 
  - [b] Find in simplest form :  $\left(\frac{4}{3}\right)^2 \times \sqrt{\frac{81}{16}} \times \left(\frac{3}{5}\right)^{\text{zero}}$
- 4 [a] Find the value of:  $12 \times 2^2 + 24 + 3^2$ 
  - [b] Find the S.S of the equation:  $3 \times -13 = 26$ , where  $\times \in \mathbb{N}$
- [5] [a] Find the value:  $\frac{(2)^7 \times (2)^5}{(2)^6 \times (2)^3}$ 
  - [b] For one roll of a fair die , Calculate the probability of :
    - (1) Getting a prime number.
- (2) Getting a number more than 6

# **Assiut Governorate**

**Educational Expirementals unit** 

...

Answer the following questions:

- 1 Complete each of the following:
  - (1) If: x = y, then  $5^{x-y} = \dots$
  - $(2)\sqrt{6^2+8^2} = \cdots$

78

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى المعن الاعدادي مواقع أخرى المعن الاعدادي معنى المعنى المعن

(3) The probability of the impossible event = ........

- (4) If:  $3 \times = 4$ , then  $12 \times -2 = \dots$
- (5) 1, 2, 3, 5, 8, ..... in the same pattern.

2 Choose the correct answer from the given :

- (1)  $3^5 \times 2^5 = \cdots$ 
  - (a)  $5^5$
- (b)  $6^5$
- (c)  $6^{10}$
- (d)  $5^{25}$

(2)  $\frac{4 a^2 b^4}{2 a^3 b^3} = \dots$  where  $ab \neq 0$ 

- (a) 2 ab
- (b)  $2a^5 b^7$
- (c)  $\frac{2b}{a}$
- $(d)\frac{2}{ab}$

(3) If the probability that a pupil succeed is 75 %, then the probability of his failure is

- (a) 0.75
- (b) 0.25
- (c) 0.75
- (d) 1.25

(4)  $x < \frac{5}{2}$  equivalent .....

- (a)  $x < \frac{5}{2}$  (b)  $x > \frac{5}{2}$
- (c) X < 10
- (d) x > 10

(5) If: -x < 5, then x - 5

- (a) <
- (b) >
- (c) =

(d) ≤

[3] [a] Find the solution set of each of the following where  $x \in \mathbb{Q}$ :

(1)  $3x-1 \le 2x+3$ 

(2)  $(3 \times + 2) + 5 = 13$ 

[b] Find the value of the expression in the simplest form :  $\left(\frac{-1}{3}\right)^2 + \sqrt{\frac{64}{81}} - \left(\frac{3}{7}\right)^0$ 

[4] [a] Two integers the smaller one is 2  $\times$  and the greater is 5  $\times$ , if the difference between them is 30 find the two numbers.

[b] Simplify:  $\left(-\frac{4}{5}\right)^6 \div \left(\frac{4}{5}\right)^4$ 

[5] [a] Find the result of the expression:  $(5.4 \times 10^4) + (3.7 \times 10^5)$  in the form  $a \times 10^n$ where n is integer number.

[b] A box contains 4 white , 5 red and 6 blue balls. A ball is drawn randomly from the box. Calculate the probabilities of the following events:

1) The ball is red.

(2) The ball is white or red.

# **Qena Governorate**

Math's S.V

Answer the following questions:

### 1 Choose the correct answer:

(1) 
$$37 \times 10^3 = \dots$$
 (In the standard form)

(a) 
$$0.37 \times 10^5$$
 (b)  $37 \times 10^3$ 

(b) 
$$37 \times 10^3$$

(c) 
$$3.7 \times 10^4$$

(d) 
$$0.37 \times 10^{-3}$$

(2) The additive inverse of 
$$\left(-\frac{2}{5}\right)^2$$
 is ......

(a) 
$$\frac{2}{5}$$

(b) 
$$\frac{4}{25}$$

(c) 
$$\frac{-4}{25}$$

$$3\sqrt{10^2-8^2} = \cdots$$

(b) 
$$10 - 8$$

$$(d) =$$

### (5) Which of the following number is the probability of occurrence of an event?

$$(b) - 0.4$$

### 2 Complete each of the following:

$$(1)\sqrt{(-4)^2} = \cdots$$

(2) The age of boy now is 
$$X$$
 years, then his age after 5 years is ...... years.

(4) If: 
$$2 \times 2 = 8$$
, then  $\times 1 = \dots$  (5)  $\left(\frac{2}{7}\right)^{-1} = \dots$ 

### [3] [a] Find the S.S. for the equation: $5 \times -6 = 34$ , $x \in \mathbb{Q}$

[b] Find: 
$$\left(\frac{4}{3}\right)^2 \times \sqrt{\frac{9}{16}} \times \left(\frac{4}{3}\right)^{-1}$$

### [4] [a] Find the S.S. for the inequality in N:

$$5X-2 \ge 2X+1$$

[b] If: 
$$x = -\frac{1}{2}$$
,  $y = \frac{3}{4}$ . Find the value of:  $y \div x^2$ 

# [5] [a] Find the value of : $\frac{7^3 \times 7^{-4}}{(-7)^4 \times 7^{-3}}$

### [b] A card is selected randomly from 10 cards numbered from 1 to 10 What is the probability that elected card shows:

# Answers of school book models in algebra and statistics

# Model

- (1)10
- (2) 2
- (3)3
- (4)  $3.5 \times 10^{-3}$  (5)  $\frac{4}{9}$

- (1)(b)
- (2) (a)
- (3) (a)
- (4) (a)

3  $1 \times \frac{4}{25} \times \sqrt{\frac{25}{4}} = 1 \times \frac{4}{25} \times \frac{5}{2} = \frac{2}{5}$ 

- [a] (1) ::  $3 \times + 1 = 25$
- $\therefore 3 \times = 24$

- $\therefore x = 8$
- :. The S.S. = {8}
- (2):2X+5<16
- :. 2 X < 11
- $\therefore x < \frac{11}{2}$
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x < \frac{11}{2}\}$
- [b] The population that will be in 2 years  $= 3 (1.02)^2 \times 70^6 = 3.1212 \times 10^6$  people

5

- (1) The probability of change it before travelled 50 thousand km. =  $\frac{80}{800} = \frac{1}{10}$
- (2) The probability of change it after travelled more than 100 thousand km. =  $\frac{600}{800} = \frac{3}{4}$

### Model

- (1) 1
- (2)  $\frac{4}{7}$
- (3) zero
- (4) 13,21
- (5) 510 students

2

- (1) (b)
- (2)(d)
- (3) (a)

 $\therefore$  3 x = 30

(4) (b)

 $3 : 5 \times -2 \times = 30$ 

 $\therefore x = 10$ 

.. The two numbers are: 20,50

- [a] (1) :: 3x + 7 = 13 :: 3x = 6
  - $\therefore x = 2$
- $\therefore$  The S.S. =  $\{2\}$

- (2) :  $2 \times 15 < 19$
- $\therefore 2X < 4$

- $\therefore x < 2$
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x < 2\}$
- **[b]**  $\frac{1}{9} + \frac{8}{9} 1 = 1 1 = zero$

- (1) The probability of getting a prime even number =  $\frac{1}{6}$
- (2) The probability of getting an odd number less than  $4 = \frac{2}{6} = \frac{1}{3}$

# Model

1

- (1)1
- (2)  $\frac{1}{5}$ ,  $\frac{1}{4}$  (3)  $\{\frac{1}{2}\}$
- (4) 4

m)

2

- (1) (d)
- (2)(c)
- (3) (b)
- (4) (b)

3 Let the number be X

- :. Its three times = 3 X
- $\therefore X + 3X = 28$
- $\therefore 4 x = 28$
- $\therefore x = 7$
- ... The number = 7

- [a] (1) ::  $3 \times + 5 = 11$
- $\therefore 3 X = 6$
- $\therefore x = 2$
- :. The S.S. =  $\{2\}$
- (2) :  $2X + 3 \le 7$
- :. 2 X ≤ 4
- ∴ X ≤ 2
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \le 2\}$

[b] The time elapsed

- $= \frac{d}{v} = \frac{1.44 \times 10^8 \times 1000}{3 \times 10^8}$
- = 480 seconds = 8 minutes

- [a]  $(5.4 \times 10^4) + (3.7 \times 10^5)$ 
  - $=10^4 (5.4 + 3.7 \times 10)$
  - $=10^4 (5.4 + 37)$
  - $= 10^4 \times 42.4 = 4.24 \times 10^5$
- [b] (1) The probability of the two faces are similar
  - (2) The probability of appearance only one tail  $=\frac{2}{4}=\frac{1}{2}$

# Model

- (1)  $\frac{1}{2}$
- (5) [
- (a)  $\{3,4\}$  (d)  $\frac{31}{32},\frac{63}{64}$

- (1) (b)
- (a) (p)
- (3) (b) (4) (d)
  - (5) (c)

$$[3] [a] \left(\frac{\chi^2}{y^3}\right)^2 = \left(\left(\frac{3}{4}\right)^2 \div \left(-\frac{3}{2}\right)^3\right)^2$$
$$= \left(\frac{9}{16} \div \left(-\frac{27}{8}\right)\right)^2$$
$$= \left(\frac{9}{16} \times \left(-\frac{8}{27}\right)\right)^2 = \left(-\frac{1}{6}\right)^2 = \frac{1}{36}$$

- [b] Let the great number be X
  - $\therefore$  Th small number = x 5
  - x + x 5 = 15
- 2x-5=15
- $\therefore 2 \times = 20$
- $\therefore x = 10$
- .. The two numbers are: 10,5

- (1) : 3x + 2 = 8
- $\therefore 3 \times = 6$

 $\therefore x = 2$ 

- $\therefore \text{ The S.S.} = \{2\}$
- (2):4x-3<7
- :. 4 X < 10

 $\therefore x < \frac{10}{4}$ 

- $\therefore x < \frac{5}{2}$
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x < \frac{5}{2}\}$

- (1) The probability of the appearance of at least one head =  $\frac{3}{4}$
- (2) The probability of the appearance of at most one head =  $\frac{3}{4}$

### Model

- 1) 1/2
- (2) 1
- (3) 2
- $(4)\frac{3}{8}$
- (5) 4<sup>19</sup>

### 5

- (1)(c)
- (2) (a)
- (3)(c)
- (4) (b)

$$3 12 \times 4 \div 24 + 9 = 48 \div 24 + 9 = 2 + 9 = 11$$

- [a] (1) :: 3-4x=-5
  - 3 + 5 = 4x
- $\therefore 4 \times = 8$

x = 2

- $\therefore$  The S.S. =  $\{2\}$
- (2) :  $2x 1 \ge 5$
- ∴ 2 X ≥ 6

- ∴ x≥3
- $\therefore$  The S.S. =  $\{x : x \in \mathbb{Q}, x \ge 3\}$

**[b]** 
$$\frac{3 n^2}{2} - 3 n + 3 - n = \frac{3 n^2}{2} - 4 n + 3$$

The value = 
$$\frac{3 \times 1^2}{2} - 4 \times 1 + 3 = \frac{3}{2} - 4 + 3 = \frac{1}{2}$$

- [a] Let the age of the eldest sister be X years
  - $\therefore$  Let the age of the middle sister = (x-3) years
  - Let the age of the youngest sister = (x 5) years
  - x + x 3 + x 5 = 25
  - $\therefore 3 \times -8 = 25$
  - $\therefore 3 X = 33$
- x = 11
- .. The ages of three sisters are :
  - 6 years , 8 years and 11 years
- [b] (1) The probability the ball is red =  $\frac{5}{15} = \frac{1}{3}$ 
  - (2) The probability the ball is white or red

$$=\frac{9}{15}=\frac{3}{5}$$

## Answers of school examinations in Algebra and Statistics

# Cairo

- (1)(c)
  - (a) (p)
- (3) (d)
- (4) (a)
- (5) (a)

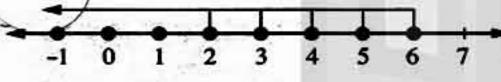
### 5

- **(1)5**

- (2) 3 > a (3) -4 (4)  $-\frac{4}{25}$  (5) zero

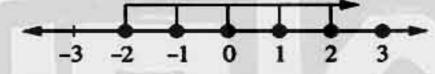
### 3

- [a] (1)  $: 5x 1 \le 29$   $: 5x \le 30$ 
  - ∴ X≤6
  - : The S.S. =  $\{6, 5, 4, 3, 2, ...\}$



- (2) : x+4>1 : x>-3

  - ... The S.S. =  $\{-2, -1, 0, 1, ...\}$



- [b] (1)  $\frac{4}{9} \times \frac{9}{4} \times 1 = 1$ 
  - (2)  $\left(-\frac{2}{3}\right)^6 \div \left(-\frac{2}{3}\right)^7 = \left(-\frac{2}{3}\right)^{6-7} = \left(-\frac{2}{3}\right)^{-1} = -\frac{3}{2}$

- [a] Let the two numbers be X and 2 X
  - $\therefore x + 2x = 45 \qquad \therefore 3x = 45$
  - $\therefore x = 15$
  - .. The two numbers are: 15 and 30

[b] 
$$x^3 y^2 z = \left(-\frac{1}{2}\right)^3 \times \left(\frac{4}{3}\right)^2 \times \left(\frac{1}{5}\right)$$
  
=  $-\frac{1}{8} \times \frac{16}{9} \times \frac{1}{5} = -\frac{2}{45}$ 

### 5

- [a] The order is:  $7.3 \times 10^{-5}$ ,  $10^{-4}$ ,  $2.7 \times 10^{-4}$ and  $0.25 \times 10^{-2}$
- [b]  $S = \{1, 2, 3, 4, 5, 6, 7, 8\}$ 
  - (1) The probability of getting an even number  $=\frac{4}{9}=\frac{1}{2}$
  - (2) The probability of getting a number greater than or equal to  $6 = \frac{3}{8}$

# Cairo

- (1) (b)
- (b) (s)
- (3)(c)
- (4)(c)
- (5) (b)

- (1) (X-3) years (2) 90 (3) zero (4) -5 (5) 2

- [a]  $x^2 y z^2 = \left(-\frac{3}{2}\right)^2 \left(\frac{1}{2}\right) \times \left(-\frac{4}{3}\right)^2$  $=\frac{9}{4}-\frac{1}{2}\times\frac{16}{9}=\frac{9}{4}-\frac{8}{9}=\frac{49}{36}$
- [b] : 3x+6<-x+4
  - 3x + x < 4 6
  - $\therefore 4 \times < -2 \qquad \therefore \times < -\frac{2}{4} \qquad \therefore \times < -\frac{1}{2}$
- $\therefore \text{ The S.S.} = \left\{ x : x \in \mathbb{Q}, x < -\frac{1}{2} \right\}$

- [a] :  $5 \times + 8 = 13 2 \times$ 
  - $\therefore 5x + 2x = 13 8 \therefore 7x = 5$
  - $\therefore x = \frac{3}{7}$
- $\therefore \text{ The S.S.} = \left\{ \frac{5}{7} \right\}$
- [b] (1) The probability that the selected card shows an odd number =  $\frac{5}{10} = \frac{1}{2}$ 
  - (2) The probability that the selected card shows a prime number =  $\frac{4}{10} = \frac{2}{5}$
  - (3) The probability that the selected card shows an odd number greater than  $3 = \frac{3}{10}$

- [a]  $\frac{73}{73} = 1$
- [b] Let the length of the rectangle = x metres
  - $\therefore$  the width of the rectangle = (x 4) metres
  - → the perimeter = (length + width) × 2
  - $\therefore 68 = (X + X 4) \times 2$
- $34 = 2 \times -4$
- $\therefore 2 x = 38$
- $\therefore x = 38 \div 2 = 19$  metres
- .. the dimensions of the rectangle are 19 metres , 15 metres

# Giza

- (1)(c)
- (2) (a)
- (3) (d)
- (4) (a)
- (5) (c)

- $0^{\frac{2}{5}}$
- (2)-2
- (3) zero
- **4**) 10
- **(5)**>

[a] (1) 
$$\frac{4}{9} \times \frac{3}{2} \times 1 = \frac{2}{3}$$

(2) 
$$\frac{(2)^5 \times (2)^4}{(2)^9} = 2^{5+4-9} = 2^0 = 1$$

[b] Let the three consecutive natural numbers be x, X+1 and X+2

$$\therefore X + X + 1 + X + 2 = 33$$

$$\therefore 3 \times + 3 = 33$$

$$\therefore 3 \times = 30$$

$$\therefore x = 10$$

.. The three numbers are: 10, 11, 12

- (1) : 2x + 1 = 13 : 2x = 12

  - $\therefore X = 6 \qquad \qquad \therefore \text{ The S.S.} = \{6\}$
- (2) :  $3x 1 \le 2x + 4$ 
  - $\therefore 3x-2x \le 4+1 \therefore x \le 5$
  - $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \le 5\}$

[a] 
$$x^2 - y^2 Z = \left(\frac{-2}{3}\right)^2 - \left(\frac{1}{2}\right)^2 \times \left(\frac{-4}{3}\right)$$
  
=  $\frac{4}{9} - \frac{1}{4} \times \left(\frac{-4}{3}\right) = \frac{4}{9} + \frac{1}{3} = \frac{7}{9}$ 

[b] (1) The probability of the ball is black =  $\frac{4}{16} = \frac{1}{4}$ 

(2) The probability of the ball is not white  $=\frac{4+7}{16}=\frac{11}{16}$ 

### Giza

- ①(b) (b)
- (3) (b)
- (4) (d)
- (5) (d)

5

- ① 10
- 2-1
- 3 X-5 (4) 17
- **(5)** 5

3

- [a] (1) :: 8x + 4 = 12 :: 8x = 8

  - $\therefore x = 1$
- ∴ The S.S. = {1}
  - (2) :  $2x + 3 \le 7$  :  $2x \le 4$ 

    - $\therefore x \le 2 \qquad \therefore \text{ The S.S.} = \{2, 1, 0\}$

**[b]** 
$$(a^3 + b^3)^{-1} = \left( \left( \frac{1}{3} \right)^3 + \left( -\frac{2}{3} \right)^3 \right)^{-1}$$
  
=  $\left( \frac{1}{3} - \frac{8}{3} \right)^{-1} = \left( -\frac{7}{3} \right)^{-1}$ 

$$=\left(\frac{1}{27}-\frac{8}{27}\right)^{-1}=\left(-\frac{7}{27}\right)^{-1}=-\frac{27}{7}$$

[a] (1) 
$$\frac{(-3)^3 \times (-3)^5}{(-3)^6} = (-3)^{3+5-6} = (-3)^2 = 9$$

(2) 
$$\left(\frac{-5}{4}\right)^2 \times \sqrt{\frac{25}{16}} \times \left(\frac{-4}{5}\right)^3 = \left(\frac{5}{4}\right)^2 \times \frac{5}{4} \times -\left(\frac{5}{4}\right)^{-3}$$
$$= -\left(\frac{5}{4}\right)^{2+1-3} = -1$$

[b] : 
$$(BC)^2 = (AC)^2 - (AB)^2 = (10)^2 - (6)^2$$
  
=  $100 - 36 = 64$ 

∴ BC = 
$$\sqrt{64}$$
 = 8 cm.

- [a] Let the three odd consecutive numbers:  $x \cdot x + 2 \cdot x + 4$ 
  - x + x + 2 + x + 4 = 117
  - $\therefore 3x + 6 = 117$   $\therefore 3x = 111$
  - $\therefore x = 37$
  - .. The three numbers are: 37 , 39 and 41
- [b]  $S = \{1, 2, 3, 4, 5, 6, 7, 8\}$ 
  - (1) The probability of  $A = \frac{4}{8} = \frac{1}{2}$
  - (2) The probability of B =  $\frac{4}{8} = \frac{1}{2}$
  - (3) The probability of  $C = \frac{2}{8} = \frac{1}{4}$

# Alexandria

- (1) (b)
- (5) (p)
- (3) (c)
- (4) (b)
- (5) (c)

2

- 1)5
- (2)-5
- (3)Ø
- (4) I
- (5)7

- [a]  $\frac{2^3 \times 2^{-4}}{2^{-2} \times 2^5} = 2^{3-4+2-5} = 2^{-4} = \frac{1}{16}$
- [b] (1) : 2x-5=1 : 2x=6

  - $\therefore x = 3 \qquad \therefore \text{ The S.S.} = \{3\}$
  - (2):4x+9≤1
- $\therefore 4x \leq -8$
- ∴ X≤-2
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \le -2\}$

- [a] Let the age of the son be X years
  - $\therefore$  The age of the man = 3  $\times$  years
  - $\therefore x + 3x = 60$
- $\therefore 4 \times = 60$
- $\therefore X = 15$
- .. The age of man = 45 years
- The age of his son = 15 years

[b] 
$$8 x^3$$
 y  $z^2 = 8 \times \left(\frac{1}{2}\right)^3 \times \frac{4}{3} \times \left(\frac{3}{2}\right)^2$   
=  $8 \times \frac{1}{8} \times \frac{4}{3} \times \frac{9}{4} = 3$ 

[a] 
$$\frac{1}{9} + \frac{8}{9} - 1 = \frac{9}{9} - 1 = 1 - 1 = 0$$

- [b] (1) The probability of drawing a ball numbered with a number that is divisible by  $3 = \frac{2}{8} = \frac{1}{4}$ 
  - (2) The probability of drawing a ball numbered with a prime number =  $\frac{4}{8} = \frac{1}{2}$

# El-Kalyoubia

- (1) (d)
- (a) (p)
- (3) (d)
- (4) (d)
- (5) (a)

- (1) 10 % (2) <sup>5</sup>/<sub>4</sub>
- (3)>
- (4) 14
- $(5)7 \times 10^6$

[a] 
$$\frac{x^2 \times x^7}{x^3 \times x^2} = x^{2+7-3-2} = x^4$$

The value =  $(-3)^4 = 81$ 

### [b] 9

[a] : 
$$3x-2>x+4$$
 :  $3x-x>4+2$ 

$$\therefore 3X - X > 4 + 2$$

- $\therefore 2x > 6$
- :. X>3
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x > 3\}$
- [b] : 3x 1 = 5
  - $\therefore 3x = 6$
  - $\therefore x = 2$
- $\therefore \text{ The S.S.} = \{2\}$

[a] Let the three consecutive even numbers be :

$$x, x+2, x+4$$

- $\therefore x + x + 2 + x + 4 = 966$
- $\therefore 3 \times + 6 = 966$
- $\therefore 3 x = 960$
- x = 320
- .. The three numbers: 320, 322, 324
- [b] (1) The probability that the drawn ball is red  $=\frac{5}{10}=\frac{1}{2}$ 
  - (2) The probability that the drawn ball is white
  - (3) The probability that the drawn ball is not blue  $=\frac{5+3}{10}=\frac{8}{10}=\frac{4}{5}$

# El-Kalyoubia

- (1) (d)
- (2)(c)
- (3)(c)
- (4)(b)
- (5) (a)

### 2

- (1) 10
- (2) 3
- (3) 14
- $(4)\frac{4}{25}$
- (5)  $\frac{1}{2}$

### 3

[a] 
$$\frac{4}{3} \times \frac{3}{5} \times \frac{1}{4} = \frac{1}{5}$$

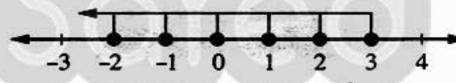
- **[b]** Let length of the rectangle = x metres
  - $\therefore$  the width of the rectangle = (x 4) metres
  - , : the perimeter = (length + width) × 2
  - $\therefore 68 = (x + x 4) \times 2$
- $\therefore 34 = 2 \times -4$
- $\therefore 2 x = 38$
- $\therefore x = 38 \div 2 = 19$  metres
- .. the dimensions of the rectangle are 19 metres , 15 metres

[a] 
$$\frac{x^7 \times x^5}{x^8} = x^{7+5-8} = x^4$$

The value =  $(-2)^4 = 16$ 

- **[b]** :  $3 \times 7 = 13$ 
  - $\therefore 3x = 6$
  - $\therefore x = 2$
- $\therefore \text{ The S.S.} = \{2\}$

- [a] : x 1 < 3
- :. X < 4
- :. The S.S. =  $\{3, 2, 1, 0, -1, ...\}$



**[b]** The probability of the event  $A = \frac{3}{6} = \frac{1}{2}$ 

# El-Sharkia

### 1

- (1) (b)
- (2)(a)
- (3)(c)
- (4) (a)
- (5) (a)

### 5

- (1)10(2) I
- (3)  $\{0\}$  (4) 2.37, -4 (5)  $\frac{a}{2}$

- [a] (1) The probability that the drawn ball is black  $=\frac{0}{12}=0$ 
  - (2) The probability that the drawn ball is not red  $=\frac{6+4}{12}=\frac{10}{12}=\frac{5}{6}$

**[b]** 
$$\because \frac{a^2}{b^2} = 0.16$$

**[b]** : 
$$\frac{a^2}{b^2} = 0.16$$
 :  $\left(\frac{a}{b}\right)^2 = \frac{16}{100} = \frac{4}{25}$ 

$$\therefore \frac{a}{b} = \pm \frac{2}{5}$$

$$\therefore \frac{a}{b} = \pm \frac{2}{5} \qquad \qquad \therefore \left(\frac{a}{b}\right)^3 = \left(\pm \frac{2}{5}\right)^3 = \pm \frac{8}{125}$$

[a] 
$$\frac{y^3 \times y^{-4}}{y^{-2} \times y^5} = y^{3-4+2-5} = y^{-4} = \frac{1}{y^4}$$
  
The value  $= \frac{1}{y^4} = \frac{1}{y^4}$ 

The value = 
$$\frac{1}{(-1)^4} = \frac{1}{1} = 1$$

[b] 
$$: 3x - 2 \le 3 - 2x : 3x + 2x \le 3 + 2$$

$$\therefore 5 \times \leq 5$$

$$\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \le 1\}$$

[a] Let the two consecutive even numbers be:  $x \cdot x + 2$ 

$$\therefore x + x + 2 = 150 \quad \therefore 2x + 2 = 150$$

$$\therefore 2 X = 148$$

$$\therefore x = 74$$

[b] In 2 years the population will be  $3(1.02)^2 \times 10^6$  $=3.1212\times10^{6}$ 

# El-Beheira

$$9 (2) - 2 (3)x (4) \frac{3}{2}$$

$$(4)\frac{3}{2}$$

### 2

### 3

Let the two natural numbers be  $x \rightarrow 2x$ 

$$\therefore x + 2x = 108$$

$$\therefore 3 x = 108$$

$$\therefore x = 36$$

.. The two numbers are: 36 and 72

[a] 
$$\therefore x^3 \div y^2 z^2 = \left(\frac{-1}{2}\right)^3 \div \left[\left(\frac{3}{4}\right)^2 \times \left(-\frac{3}{2}\right)^2\right]$$
  
=  $-\frac{1}{8} \div \left[\frac{9}{16} \times \frac{9}{4}\right] = -\frac{1}{8} \div \frac{81}{64}$   
=  $-\frac{1}{8} \times \frac{64}{81} = -\frac{8}{81}$ 

**[b]** 
$$1-4x+1>2x-6$$

$$\therefore 2-4x > 2x-6 \therefore 2+6 > 2x+4x$$

$$\therefore \frac{8}{5} > x$$

$$\therefore x < \frac{4}{3}$$

$$\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x < \frac{4}{3}\}$$

[a] 
$$(3.8 \times 10^8) \div (1.9 \times 10^6)$$

$$=\frac{3.8}{1.9}\times\frac{10^8}{10^6}=2\times10^2$$

- [b] (1) The probability of that person's preference sport =  $\frac{36}{100}$  = 0.36
  - (2) The probability of that person's preference not watch news =  $\frac{12 + 31 + 36}{100} = \frac{79}{100} = 0.79$
  - (3) The probability of that person's preference documentaries =  $\frac{12}{100}$  = 0.12
  - (4) The probability of that person's preference all of them =  $\frac{12 + 31 + 21 + 36}{100} = \frac{100}{100} = 1$

# 10 El-Dakahlia

$$(1)^{\frac{-4}{9}}$$

(2) 4 (3) zero (4) 
$$2.7 \times 10^{-7}$$
 (5)  $\frac{1}{2}$ 

# 2

[a] 
$$\frac{25}{16} \times \frac{4}{5} \times 1 = \frac{5}{4}$$

$$\therefore x \leq 2$$

[a] 
$$\frac{(-2)^6 \times (-2)^4}{(-2)^8} = (-2)^{6+4-8} = (-2)^2 = 4$$

[b] Let the three consecutive numbers be  $x \cdot x + 1$ ,x+2

$$x + x + 1 + x + 2 = 42$$

$$\therefore 3 \times + 3 = 42$$

$$\therefore 3 \times = 39$$

$$\therefore x = 13$$

.. The three numbers are: 13, 14, 15

[a] 
$$\left(\frac{x^2}{y^3}\right)^2 = \left(\left(\frac{3}{4}\right)^2 \div \left(-\frac{3}{2}\right)^3\right)^2 = \left(\frac{9}{16} \div \frac{-27}{8}\right)^2$$
  
=  $\left(\frac{9}{16} \times \frac{-8}{27}\right)^2 = \left(-\frac{1}{6}\right)^2 = \frac{1}{36}$ 

- [b] (1) The probability of the ball is red =  $\frac{7}{15}$ 
  - (2) The probability of the ball is not white  $=\frac{5+7}{15}=\frac{12}{15}=\frac{4}{5}$

# El-Monofia

- (1) (b)
- (a) (p)
- (3) (a)
- (4)(c) (5) (a)

- ① 10
- (2) 1
- (3) zero (4) 3
- (5) 10

[a] (1)  $\frac{4}{9} \times \frac{3}{2} \times 1 = \frac{2}{3}$ 

(2) 
$$\left(\frac{-2}{3}\right)^6 \div \left(\frac{-2}{3}\right)^4 = \left(\frac{-2}{3}\right)^{6-4} = \left(\frac{-2}{3}\right)^2 = \frac{4}{9}$$

- [b] :: 4x+5 ≥ 1
- : 4 X≥-4
- $\therefore x \ge -1$
- .. The S.S. =  $\{-1, 0, 1, 2, 3, ...\}$

- [a] : 3x 3 = 9
  - 2.3 x = 12
  - $\therefore x = 4$
- $\therefore$  The S.S. =  $\{4\}$
- [b] Let the age of the eldest sister be X years
  - $\therefore$  Let the age of the middle sister be = (x-3) years
  - Let the age of the youngest sister be = (x 5) years
  - x + x 3 + x 5 = 25
  - $\therefore 3 \times -8 = 25$
- $\therefore 3 \times = 33$
- $\therefore x = 11$
- .. The ages of three sisters are: 6 years > 8 years and 11 years

- [a]  $\frac{3^3 \times 3^{-4}}{3^{-2} \times 3^{-5}} = 3^{3-4+2-5} = 3^{-4} = \frac{1}{81}$
- [b] (1) The probability of getting an odd number  $=\frac{4}{8}=\frac{1}{2}$ 
  - (2) The probability of getting a number divisible by  $3 = \frac{2}{8} = \frac{1}{4}$

# El-Gharbia

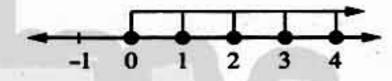
- 1) zero
- **2**9
- $3x+3 = \frac{3}{2}$
- (5) 12

- (1) (c)
- (a) (d)
- (3) (b)
- (4) (a)
- (5) (b)

- [a] Let the length of the rectangle = X metres
  - $\therefore$  the width of the rectangle = (x-4) metres
  - : the perimeter = (length + width) × 2
  - $\therefore 68 = (X + X 4) \times 2$
- $34 = 2 \times -4$

- $\therefore 2 \times = 38$
- $\therefore x = 38 \div 2 = 19$  metres
- .. the dimensions of the rectangle are 19 metres , 15 metres
- [b] :: 3x 3 = 9
- $\therefore 3 \times = 12$
- $\therefore x = 4$
- $\therefore$  The S.S. =  $\{4\}$

- [a]  $: 4x+5 \ge -3$   $: 4x \ge -8$   $: x \ge -2$
- $\therefore$  The S.S. =  $\{0, 1, 2, 3, ...\}$



**[b]** 9 + [4 + (4 + 2)] = 9 + [4 + 2] = 15

- [a] (1) The probability of that card is numbered an even number =  $\frac{5}{10} = \frac{1}{2}$ 
  - (2) The probability of that card is numbered a number divisible by  $5 = \frac{2}{10} = \frac{1}{5}$
- $[b]\sqrt{21-5} = \sqrt{16} = 4$

# 13 El-Ismailia

- ① (d)
- (b) (s)
- (3) (a)
- (4) (b)
- (5) (c)

- (1) zero
- (2) <del>4</del>
- (3)1
- (4) 10 (5)Ø

- [a]  $\frac{4}{9} \times \frac{3}{2} \times 1 = \frac{2}{3}$
- **[b]**  $a^2 b^3 + b^2 c = \left(\frac{-1}{2}\right)^2 \times (2)^3 + (2)^2 \times \frac{3}{4}$  $=\frac{1}{4}\times8+4\times\frac{3}{4}=2+3=5$

(1) 
$$: 4x-1 \ge 7$$
  $\therefore 4x \ge 8$ 

$$\therefore 4 \times \times 8$$

$$\therefore \text{ The S.S.} = \{x, x \in \mathbb{Q}, x \ge 2\}$$

(2) 
$$\therefore$$
 2 (X + 5) = 16  $\therefore$  2 X + 10 = 16

$$2x + 10 = 16$$

$$\therefore 2 \times = 16 - 10 = 6 \therefore \times = 3 \therefore \text{ The S.S.} = \{3\}$$

$$\therefore \text{ The S.S.} = \{3\}$$

[a] 
$$\therefore 2 \times 2 \times -18^{\circ} = 90^{\circ}$$

$$\therefore 4 \times -18^{\circ} = 90^{\circ} \quad \therefore 4 \times = 108^{\circ}$$

$$\therefore 4 X = 108^{\circ}$$

$$\therefore x = 27^{\circ}$$

[b] (1) The probability that the drawn ball is red 
$$= \frac{2}{12} = \frac{1}{6}$$

(2) The probability that the drawn ball is green 
$$= \frac{4}{12} = \frac{1}{3}$$

(3) The probability that the drawn ball is black 
$$= \frac{0}{12} = 0$$

# Assiut

$$\frac{1}{2}$$

$$(4)x-5 (5)16$$

[a] (1) 
$$\left(\frac{-5}{8}\right)^0 \times \sqrt{\frac{25}{4}} \times \left(\frac{-2}{5}\right)^2 = 1 \times \frac{5}{2} \times \frac{4}{25} = \frac{2}{5}$$

(2) 
$$\frac{3^4 \times 3^3}{3^6} = 3^{4+3-6} = 3$$

[b] Let the three consecutive even numbers be :

$$x, x+2, x+4$$

$$x + x + 2 + x + 4 = 78$$

$$\therefore 3 \times + 6 = 78$$
  $\therefore 3 \times = 72$ 

$$\therefore 3 \times = 72$$

$$\therefore x = 24$$

.. The three numbers are: 24, 26, 28

[a] : 
$$3x + 5 = 26$$
 :  $3x = 21$ 

$$\therefore 3 \times = 21$$

$$\therefore x = 7$$

$$\therefore x = 7 \qquad \therefore \text{ The S.S.} = \{7\}$$

**[b]** (1) The probability of the drawn ball is white 
$$=\frac{5}{16}$$

(2) The probability of the drawn ball is red = 
$$\frac{7}{16}$$

[a] 
$$: 4x - 7 \ge 1$$
  $\therefore 4x \ge 8$ 

$$\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \ge 2\}$$

**[b]** 
$$a^2 b^3 + b^2 c = \left(\frac{1}{2}\right)^2 \times (2)^3 + (2)^2 \times \frac{3}{4}$$

$$= \frac{1}{4} \times 8 + 4 \times \frac{3}{4} = 2 + 3 = 5$$

### 15 Qena

2

3

[a] (1) : 
$$2x + 14 = 12$$
 :  $2x = -2$ 

$$\therefore x = -1$$

$$\therefore X = -1 \qquad \therefore \text{ The S.S.} = \{-1\}$$

(2) 
$$\therefore 3x+1 \le 7$$
  $\therefore 3x \le 6$ 

$$\therefore 3x \le 6$$

$$\therefore \text{ The S.S.} = \{2, 1, 0, -1, -2, ...\}$$

[b] 
$$\frac{5^6 \times 5^2 \times 5^3}{5^4 \times 5^5} = 5^{6+2+3-4-5} = 5^2 = 25$$

[a] 
$$(ab)^2 - c^2 = \left(-\frac{2}{3} \times \frac{3}{4}\right)^2 - \left(\frac{1}{2}\right)^2$$

$$=\left(-\frac{1}{2}\right)^2-\left(\frac{1}{2}\right)^2=\frac{1}{4}-\frac{1}{4}=0$$

[b] (1) The probability of that card numbered by an even number =  $\frac{5}{10} = \frac{1}{2}$ 

(2) The probability of that card numbered by a number divisible by  $5 = \frac{2}{10} = \frac{1}{5}$ 

[a] 
$$\left(\frac{5}{8}\right)^0 \times \sqrt{\frac{25}{4}} \times \frac{4}{25} = 1 \times \frac{5}{2} \times \frac{4}{25} = \frac{2}{5}$$

[b] Let the three consecutive numbers be:

$$x, x+1, x+2$$

$$x + x + 1 + x + 2 = 33$$

$$\therefore 3 \times + 3 = 33 \qquad \therefore 3 \times = 30$$

$$\therefore$$
 3  $x = 30$ 

$$\therefore x = 10$$

## Answers of school book models in algebra and statistics

### Model

- 10
- **②**2.
- 33
- (4)  $3.5 \times 10^{-3}$  (5)  $\frac{4}{9}$

2

- ①(b)
- ② (a)
- (3) (a)
- (4) (a)
- (5) (a)

3 [a]  $1 \times \frac{4}{25} \times \sqrt{\frac{25}{4}} = 1 \times \frac{4}{25} \times \frac{5}{2} = \frac{2}{5}$ [b]  $3 ab + 8 a \div (4 b)$ 

- $= 3 \times 4 \times (-2) + 8 \times 4 \div (4 \times -2)$  $= -24 + 32 \div (-8)$ 
  - = -24 4 = -28

4

- [a] (1) ::  $3 \times + 1 = 25$
- $\therefore 3 x = 24$

 $\therefore x = 8$ 

- :. The S.S. =  $\{8\}$
- (2) :: 2x + 5 < 16
- $\therefore 2 \times < 11$
- $\therefore x < \frac{11}{2}$ 
  - $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x < \frac{11}{2}\}$
- [b] The population that will be in 2 years  $= 3 (1.02)^2 \times 70^6 = 3.1212 \times 10^6$  people

5

- (1) The probability of change it before travelled 50 thousand km. =  $\frac{80}{800} = \frac{1}{10}$
- (2) The probability of change it after travelled more than 100 thousand km. =  $\frac{600}{800} = \frac{3}{4}$

### Model

1 **①**1

- @ <del>4</del>
- 3 zero
- (4) 13,21
- (5) 510 students

2

- ① (b)
- ② (d)
- 3 (a)
- (4) (b)
- (5) (c)

[3] [a] :: 5 x - 2 x = 30

- $\therefore 3 \times = 30$
- $\therefore x = 10$

.. The two numbers are: 20,50 **[b]**  $\frac{5^{-4} \times 5^7}{3} = 5^{-4+7-3} = 5^0 = 1$ 

- 4
- [a] (1) :: 3x + 7 = 13 :: 3x = 6

  - $\therefore x = 2$
- :. The S.S. =  $\{2\}$

- (2) : 2x + 15 < 19
- $\therefore 2 \times < 4$

- :. X < 2
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x < 2\}$
- [b]  $\frac{1}{9} + \frac{8}{9} 1 = 1 1 = zero$

5

- [a] (1) The probability of getting a prime even number =  $\frac{1}{6}$ 
  - (2) The probability of getting an odd number less than  $4 = \frac{2}{6} = \frac{1}{3}$
- [b] Let the width of the rectangle = x cm.
  - ... The length of the rectangle = 2 x cm.
  - .. The area = length × width
  - $\therefore 12.5 = X \times 2 X$
- $12.5 = 2 x^2$
- $6.25 = x^2$
- $\therefore x = \sqrt{6.25} = 2.5 \text{ cm}.$
- $\therefore$  The width = 2.5 cm.
- The length = 5 cm.

 $2\frac{1}{5}, \frac{1}{4}$ 

# Model

- $3\{\frac{1}{2}\}$ (4) 4/3
- ⑤-4

2

(1)

1

- ① (d)
- (c)
- (3 (b)
- (4) (b)
- (5) (b)

3

- [a] Let the number be X
  - $\therefore$  Its three times = 3  $\times$
  - $\therefore x + 3x = 28$
- $\therefore 4 \times = 28$
- x = 7
- ∴ The number = 7
- [b] : The area of the triangle =  $\frac{1}{2}$  base × height
  - $\therefore$  The area of the triangle =  $\frac{1}{2} \times 9 \times 8 = 36$  cm<sup>2</sup>. Let the side length of the square =  $\ell$
  - The area of the square = The area of the triangle
  - $36 = l^2$   $l = \sqrt{36} = 6$  cm.

[4]

- [a] (1) :: 3x + 5 = 11
- $\therefore 3 x = 6$
- $\therefore x = 2$
- $\therefore$  The S.S. =  $\{2\}$
- (2) :  $2x + 3 \le 7$
- ∴ 2 X ≤ 4
- ∴ X≤2
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \le 2\}$

68

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

[b] The time elapsed =  $\frac{d}{v} = \frac{1.44 \times 10^8 \times 1000}{3 \times 10^8}$ = 480 seconds = 8 minutes

### 5

[a] 
$$(5.4 \times 10^4) + (3.7 \times 10^5)$$

$$=10^4 (5.4 + 3.7 \times 10)$$

$$=10^4 (5.4 + 37)$$
.

$$= 10^4 \times 42.4 = 4.24 \times 10^5$$

- [b] (1) The probability of the two faces are similar  $=\frac{2}{4}=\frac{1}{2}$ 
  - (2) The probability of appearance only one tail  $=\frac{2}{4}=\frac{1}{2}$

### Model

- **2**1
- 3 {3,4}

- $4)^{\frac{-2}{5}}$
- (5)  $\frac{31}{32}$ ,  $\frac{63}{64}$

- ① (b)
- (a) (b)
- (3) (b)
- (4) (d)
- (5) (c)

$$\begin{bmatrix} \mathbf{a} \end{bmatrix} \left( \frac{x^2}{y^3} \right)^2 = \left( \left( \frac{3}{4} \right)^2 \div \left( -\frac{3}{2} \right)^3 \right)^2 \\
= \left( \frac{9}{16} \div \left( -\frac{27}{8} \right) \right)^2 \\
= \left( \frac{9}{16} \times \left( -\frac{8}{27} \right) \right)^2 = \left( -\frac{1}{6} \right)^2 = \frac{1}{36}$$

- [b] Let the great number be X
  - $\therefore$  The small number = x 5
  - $\therefore X + X 5 = 15$
- $\therefore 2 \times -5 = 15$
- $\therefore 2 x = 20$
- $\therefore x = 10$
- .. The two numbers are: 10,5

- [a] ① ::  $3 \times + 2 = 8$
- $\therefore 3x = 6$

- $\therefore x = 2$
- $\therefore$  The S.S. =  $\{2\}$
- (2) :: 4x 3 < 7
- $\therefore 4 \times < 10$
- $\therefore x < \frac{10}{4}$
- $\therefore x < \frac{5}{2}$
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x < \frac{5}{2}\}$
- [b] Let the side length of the square = l m.
  - $\therefore \frac{3}{4} l^2 = \frac{75}{64} \qquad \therefore l^2 = \frac{75 \times 4}{64 \times 3}$
- - $\therefore \ell^2 = \frac{25}{16}$
- $\ell = \sqrt{\frac{25}{16}} = \frac{5}{4} = 1\frac{1}{4}$ m.

### 5

- [a] 1 The probability of the appearance of at least one head =  $\frac{3}{4}$ 
  - (2) The probability of the appearance of at most one head =  $\frac{3}{4}$
- **[b]**  $\left(\frac{7^4 \times 7^{-2}}{7^3}\right)^{-2} = \frac{7^{-8} \times 7^4}{7^{-6}} = 7^{-8+4+6} = 7^2 = 49$

# Model

- $0^{\frac{1}{2}}$
- @1
- 3-2
- $4)\frac{3}{8}$
- (5) 4<sup>19</sup>

### 2

- (c)
  - ② (a)
- (c)
- (4) (b)
- (5) (b)

- [a]  $12 \times 4 \div 24 + 9 = 48 \div 24 + 9 = 2 + 9 = 11$
- [b]  $\left(\frac{y}{x^2}\right)^{-2} = \left(\frac{3}{4} \div \left(-\frac{1}{2}\right)^2\right)^{-2}$  $=\left(\frac{3}{4} \div \frac{1}{4}\right)^{-2}$  $=\left(\frac{3}{4}\times 4\right)^{-2}=3^{-2}=\frac{1}{9}$

### 4

- [a] (1) :: 3-4x=-5
  - $\therefore 3 + 5 = 4 \times$
- $\therefore 4x = 8$
- x=2
- $\therefore$  The S.S. =  $\{2\}$

- (2)  $\therefore 2x-1\geq 5$   $\therefore 2x\geq 6$
- :. x≥3

- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \ge 3\}$
- **[b]**  $\frac{3 n^2}{2} 3 n + 3 n = \frac{3 n^2}{2} 4 n + 3$ 
  - The value =  $\frac{3 \times 1^2}{2} 4 \times 1 + 3 = \frac{3}{2} 4 + 3 = \frac{1}{2}$

### [5]

- [a] Let the age of the eldest sister be X years
  - $\therefore$  Let the age of the middle sister = (x-3) years
  - Let the age of the youngest sister = (x 5) years
  - x + x 3 + x 5 = 25
- $\therefore 3x 8 = 25$

 $\therefore$  3 x = 33

- $\therefore x = 11$
- .. The ages of three sisters are: 6 years , 8 years and 11 years
- [b] 1 The probability the ball is red =  $\frac{5}{15} = \frac{1}{2}$ 
  - (2) The probability the ball is white or red  $=\frac{9}{15}=\frac{3}{5}$

### **Answers of school examinations** in Algebra and Statistics

# Cairo

- (1) (a)
- (2) (a)
- (3) (c)
- (4) (b)
- (5) (a)

2

- (1)  $-\frac{25}{49}$  (2) zero
- (3) 1
- (4)6
- (5) 5

- [a] ::  $5 \times + 3 > 15 + \times$
- $x \cdot 5x x > 15 3$
- $\therefore 4 \times > 12$
- $\therefore x > 3$
- $\therefore \text{ The S.S.} = \{x: x \in \mathbb{Q}, x > 3\}$
- [b]  $\frac{a^5 \times a^7}{a^8} = a^{5+7-8} = a^4$

- [a]  $a^3 \div b^2 c^2 = \left(\frac{-1}{2}\right)^3 \div \left[\left(\frac{3}{4}\right)^2 \times \left(\frac{-3}{2}\right)^2\right]$  $=\frac{-1}{8} \div \left(\frac{9}{16} \times \frac{9}{4}\right) = \frac{-1}{8} \div \frac{81}{64}$  $=\frac{-1}{8}\times\frac{64}{81}=-\frac{8}{81}$
- [b] (1) The probability of the ball is red =  $\frac{5}{20} = \frac{1}{4}$ 
  - (2) The probability of the ball is not black  $=\frac{8+5}{20}=\frac{13}{20}$

- [a] :  $3 \times + 17 = 38$
- $\therefore 3 \times = 21$
- $\therefore x = 7$
- $\therefore \text{ The S.S.} = \{7\}$
- [b]  $\frac{4}{3} \times \frac{3}{5} \times \frac{1}{4} = \frac{1}{5}$

# Cairo

1

- (1) (b)
- (2) (c)
- (3) (a)
- (4) (d)
- (5) (c)

2

- (1) zero (2)  $\frac{9}{4}$  (3) x + 5 (4) 16
- (5) {5}

- (1)  $\frac{4}{9} \times \frac{3}{2} \times 1 = \frac{2}{3}$
- (a)  $\frac{2^5 \times (-2)^4}{2^9} = \frac{2^5 \times 2^4}{2^9} = 2^{5+4-9} = 2^0 = 1$

- (1)  $:: 2 \times x + 14 = 12$   $:: 2 \times x = -2$   $:: \times x = -1$ 

  - $\therefore$  The S.S. =  $\{-1\}$
- (2) :  $3x + 1 \le 7$
- :.3 X ≤ 6
- ∴ X≤2
- $\therefore$  The S.S. =  $\{2, 1, 0, -1, \dots\}$
- [a]  $(ab)^2 c^2 = \left(\frac{-2}{3} \times \frac{3}{4}\right)^2 \left(\frac{1}{2}\right)^2 = \left(\frac{-1}{2}\right)^2 \left(\frac{1}{2}\right)^2$  $=\frac{1}{4}-\frac{1}{4}=0$
- **[b]** (1) The probability of getting red ball =  $\frac{1}{15}$ 
  - (2) The probability of getting not white ball  $=\frac{5+7}{15}=\frac{12}{15}=\frac{4}{5}$

# Cairo

1

- (1) (b)
  - (S)(C)
- (3) (b)
- (4) (c)
- (5) (a)

2

- (1)  $\frac{1}{9}$
- (2) 10<sup>-4</sup> (3) 10
- (4)3
- (5)7

[3]

- [a] : 5x + 8 = 13 2x : 5x + 2x = 13 8
  - $\therefore x = \frac{5}{7}$
  - $\therefore 7x = 5$
- [b]  $\frac{-1}{8} \div (-3) = \frac{-1}{8} \times \left(-\frac{1}{3}\right) = \frac{1}{24}$

- [a]  $a^3b^2 + b^2c 8$  abc =  $\left(-\frac{1}{2}\right)^3 \times 2^2 + 2^2 \times \frac{3}{4}$  $-8 \times \left(-\frac{1}{2}\right) \times 2 \times \frac{3}{4}$ 
  - $=\frac{-1}{9}\times4+4\times\frac{3}{4}+6=8\frac{1}{2}$
- [b] : x = 0.000625
  - $\therefore \sqrt{x} = \sqrt{0.000625} = 0.025 = 2.5 \times 10^{-2}$

- [a]  $: 3x-1 \le 2x+3$
- $\therefore 3x-2x \le 3+1$
- $\therefore x \leq 4$
- [b] The probability of getting a card with an odd number =  $\frac{20}{39}$

# Giza

- (1) (d) (2)(c)
- (3) (b)
- (4)(c)
- (5) (a)

### 2

- $(1)^{2}$
- (2)  $\frac{9}{4}$
- (3) {3,4,5,....}

- (4)  $\frac{1}{2}$
- (5)-4

- [a]  $\frac{x^3 \times x^4}{x^5} = x^{3+4-5} = x^2$ 
  - at x = -3

[b]  $\therefore 2x - 3 \le 1$ 

∴ 2 X ≤ 4

 $\therefore (-3)^2 = 9$ 

- : X≤2
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \le 2\}$

- [a]  $1 \times \frac{9}{8} \times \left(\frac{-8}{27}\right) = -\frac{1}{3}$
- **[b]** : 2x 3 = 6 : 2x = 9
- $\therefore x = \frac{9}{2}$
- $\therefore$  The S.S. =  $\left\{\frac{9}{2}\right\}$

### 5

- [a] : 5 x 3 x = 20
  - $\therefore 2 \times = 20$
- $\therefore x = 10$
- .. The two numbers are: 30 and 50
- **[b]**  $S = \{1, 2, 3, 4, 5, 6\}$ 
  - (1) The probability of rolling an even number  $=\frac{3}{6}=\frac{1}{2}$
  - (2) The probability of rolling a number greater than  $1 = \frac{5}{6}$

# Giza

- ①(c)
- (d)
- (3) (b)
- (4) (a)
- (5) (b)

### 2

- $\odot \frac{1}{2}$
- 2 zero
- ЭØ
- (4) X−5 (5) 16

### 3

- [a] (1)  $1 \times \frac{5}{2} \times \frac{4}{25} = \frac{2}{5}$  (2)  $\frac{3^4 \times 3^3}{3^6} = 3^{4+3-6} = 3$
- **[b]** Let the three numbers be:  $x \cdot x + 2 \cdot x + 4$ 
  - $\therefore x + x + 2 + x + 4 = 78$

- $\therefore 3x + 6 = 78$
- $\therefore 3 x = 72$
- $\therefore x = \frac{72}{3} = 24$
- .. The three numbers are: 24, 26, 28

- [a] :  $3 \times 4 + 5 = 26$  :  $3 \times 4 = 21$
- $\therefore x = 7$

- $\therefore$  The S.S. =  $\{7\}$
- [b] (1) The probability of the drawn ball is white
  - (2) The probability of the drawn ball is red =  $\frac{1}{16}$

### 5

- [a]  $: 4x-7 \ge 1$   $: 4x \ge 8$
- :. x≥2
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \ge 2\}$
- **[b]**  $a^2b^3 + b^2c = \left(\frac{1}{2}\right)^2 \times (2)^3 + (2)^2 \times \frac{3}{4}$  $=\frac{1}{4} \times 8 + 4 \times \frac{3}{4} = 5$

# Alexandria

### [1]

- (1) (b)
- (S)(C)
- (3) (a)
- (4) (d)
- (5) (a)

### 2

- (1) zero
- (2)1
- 3-3
- (4) 1, 10 (5)  $\frac{1}{2}$

[a] 
$$\left(\frac{x^2}{y^3}\right)^2 = \left(\frac{\left(\frac{3}{4}\right)^2}{\left(\frac{-3}{2}\right)^3}\right)^2 = \left(\frac{\frac{9}{16}}{-\frac{27}{8}}\right)^2$$

$$=\left(\frac{-1}{6}\right)^2=\frac{1}{36}$$

**[b]**  $12 \times 4 \div 24 + 9 = 48 \div 24 + 9 = 2 + 9 = 11$ 

### 4

- (1) : 4x + 3 = 11 $\therefore$  The S.S. =  $\{2\}$
- $\therefore 4 \times = 8$
- $\therefore x = 2$

- (2) :: 6x 2 < 7
- $\therefore 6x < 9$
- $\therefore x < \frac{3}{2}$
- $\therefore \text{ The S.S.} = \left\{ x : x \in \mathbb{Q}, x < \frac{3}{2} \right\}$

- (1) The probability of getting an even number greater or equal to  $6 = \frac{2}{9} = \frac{1}{4}$
- (2) The probability of getting the number  $=2^n (n \in \mathbb{Z} < 4) = \frac{3}{8}$

# Alexandria

### [1]

- (1) 8
- (2)1
- (3) 4
- (4) 3
- **⑤**9

### 2

- (1) (b)
- (2) (a)
- (3) (d)
- (4) (a)
- (5) (b)

[a] 
$$\frac{2^3 \times 2^{-4}}{2^{-2} \times 2^5} = \frac{2^{-1}}{2^3} = 2^{-1-3} = 2^{-4} = \frac{1}{16}$$

[b] : 3x-2>x+4 : 3x-x>4+2

 $\therefore 2x > 6$ 

- $\therefore x > 3$
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x > 3\}$

- [a]  $8 + [4 + (4 \div 2)] = 8 + 6 = 14$
- [b] The probability of event  $A = \frac{3}{6} = \frac{1}{2}$

### [5]

- [a]  $1 \times \frac{5}{2} \times \frac{4}{25} = \frac{2}{5}$
- **[b]**  $x^3 y^2 = \left(-\frac{1}{2}\right)^3 \times \left(\frac{3}{4}\right)^2 = -\frac{1}{8} \times \frac{9}{16} = -\frac{9}{128}$

# 8 El-Kalyoubia

### 1

- (c)
- (a) (p)
- (d)
- (4) (b)
- (5) (c)

### 2

- ① zero ② 5

- $3-\frac{16}{25}$   $4\frac{1}{2}$   $5\frac{1}{6},\frac{1}{5}$

### 3

- [a]  $\frac{7^{-3} \times 7^5}{3^2} = 7^{-3+5-2} = 7^0 = 1$
- [b] 1 The probability of getting an even number  $=\frac{3}{6}=\frac{1}{2}$ 
  - (2) The probability of getting an odd number less than  $4 = \frac{2}{6} = \frac{1}{3}$

- [a] : 3x + 9 = 11
- $\therefore 3 x = 2 \qquad \therefore x = \frac{2}{3}$
- $\therefore$  The S.S. =  $\left\{\frac{2}{3}\right\}$
- **[b]**  $\left(\frac{x}{y}\right)^2 = \left(\frac{\left(\frac{-3}{2}\right)}{\left(\frac{-4}{2}\right)}\right)^2 = \frac{81}{64}$

### 5

- [a]  $:: 2x + 3 \le 7$   $:: 2x \le 4$
- ∴ X≤2
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \le 2\}$
- [b] :  $(XY)^2 = 25$  : XY = 5 cm.

  - .. Z is the midpoint of XY
  - ∴  $XZ = \frac{5}{2} = 2.5 \text{ cm}.$

# El-Monofia

### 1

- ①(c)
- (2) (b)
- (d)
- (4) (a)
- (5) (c)

- $0\frac{1}{4},\frac{1}{3}$
- **2**1

- 41
- (5) {-2,-3,-4,....}

### 3

- [a]  $\frac{4}{25} \times \frac{5}{2} \times 1 = \frac{2}{5}$
- [b]  $\therefore 3x + 8 \le 1$   $\therefore 3x \le -7$   $\therefore x \le -\frac{7}{3}$
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \le -\frac{7}{3}\}$

### 4

- [a] : 2x + 9 = 17
- $\therefore 2 \times = 8$

- $\therefore$  The S.S. =  $\{4\}$
- [b] Let the age of the son is X years.
  - .. The age of the father is 3 x years.
  - $\therefore x + 5 + 3x + 5 = 58$   $\therefore 4x + 10 = 58$
  - $\therefore 4 \times = 48$
- $\therefore x = 12$
- .. The age of the son is 12 years
- The age of the father is 36 years.

# [a] $\left[\frac{x^3}{y^2}\right]^2 = \left[\frac{\left(\frac{-3}{2}\right)^3}{\left(\frac{3}{2}\right)^2}\right]^2 = \left[\frac{\frac{-27}{8}}{\frac{5}{16}}\right]^2 = \left(-6\right)^2 = 36$

- [b] 1 The probability the ball is red =  $\frac{5}{15} = \frac{1}{3}$ 
  - (2) The probability the ball isn't blue  $=\frac{4+5}{15}=\frac{9}{15}=\frac{3}{5}$
  - (3) The probability the ball is green =  $\frac{0}{15}$  = 0

# 10 Port Said

- 17
- ② zero \_, ③ 1
- **4** 10
- (5) 14

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

2

- (1) (b)
- (2)(c)
- (3) (b) (4) (a)
- (5) (c)

- (1) : -3 + x = 5
- $\therefore x = 8$
- $\therefore$  The S.S. =  $\{8\}$
- (2) ::  $2x 1 \ge 5$
- :.2 X≥6
- $\therefore x \ge 3$
- $\therefore$  The S.S. =  $\{3, 4, 5, \dots\}$

- [a]  $(x + y)^{-1} = \left(\frac{1}{4} + \frac{1}{8}\right)^{-1} = \left(\frac{3}{8}\right)^{-1} = \frac{8}{3}$
- [b]  $1 \times \frac{4}{25} \times \frac{5}{2} = \frac{2}{5}$

5

- [a]  $3 ab^2 \times 2 a^2b^3 = 6 a^3b^5$
- [b] (1) The probability drawing a card carries an odd number greater than  $10 = \frac{0}{10} = 0$ 
  - (2) The probability drawing a card carries an even number less than  $10 = \frac{4}{10} = \frac{2}{5}$
  - (3) The probability drawing a card carries a prime number =  $\frac{4}{10} = \frac{2}{5}$

# Kafr El-Sheikh

- (1)(c)
- (2) (d)
- (3) (a)
- (4) (a)
- (5) (d)

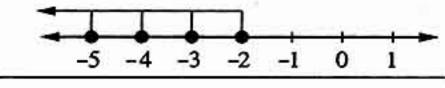
[2]

- (1)≥
- (2)  $\frac{1}{9}$
- (3) 12
- (4) 10
- (5) 15 %

3

- [a] :: 3x 5 = 4
- $\therefore 3x = 9$
- $\therefore x = 3$

- **[b]** :  $-2x-3 \ge 1$
- $\therefore -2 \times \geq 4$
- $\therefore x \leq -2$



- (1)  $\frac{16}{25} \times \frac{5}{4} \times 1 = \frac{4}{5}$
- (2)  $\frac{(-3)^6 \times (3)^{-3}}{(3)^5 \times (3)^{-4}} = \frac{(3)^6 \times (3)^{-3}}{(3)^5 \times (3)^{-4}} = \frac{3^3}{3} = 3^{3-1} = 3^2 = 9$

- [a]  $x^2yz = \left(\frac{1}{2}\right)^2 \times \frac{4}{5} \times \frac{5}{2} = \frac{1}{4} \times \frac{4}{5} \times \frac{5}{2} = \frac{1}{2}$
- [b] (1) The probability of getting a number divisible by  $7 = \frac{1}{10}$ 
  - (2) The probability of getting an even number  $=\frac{5}{10}=\frac{1}{2}$
  - (3) The probability of getting a number less than  $8 = \frac{7}{10}$

# Beni Suef

1

- (1) (b)
- (a) (d)

(2) 14

- (3) (b)
- (4)(c)
- (b) (c)

2

- (1) 4
- (3)  $\frac{6}{5}$
- (4) zero (5)  $\frac{1}{2}$

3

- (1):  $4x-1 \ge 7$
- ∴ 4 X ≥ 8
- :. x≥2
- $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \ge 2\}$
- (a) : 2(x+4) = 15
- $\therefore 2x + 8 = 15 \therefore 2x = 7$
- $\therefore x = \frac{7}{2}$
- $\therefore$  The S.S. =  $\left\{\frac{7}{2}\right\}$

[a]  $a^2b^3 + b^2c = \left(\frac{-1}{2}\right)^2 \times 2^3 + 2^2 \times \frac{3}{4}$ 

$$=\frac{1}{4}\times 8 + 4\times \frac{3}{4} = 5$$

[b]  $144 - 8 \div 8 = 144 - 1 = 143$ 

- [a]  $\frac{\mathcal{T}^2 \times 7^5}{r^3} = \mathcal{T}^{-2+5-3} = 7^0 = 1$
- [b] (1) The probability of getting an even number  $=\frac{5}{10}=\frac{1}{2}$ 
  - (2) The probability of getting a number divisible by  $5 = \frac{2}{10} = \frac{1}{5}$

# El-Menia

[1]

- (1) (d)
- (2) (a)
- (3) (c)
- (4) (a)
- (5) (b)

- (1) 0.3
- (2) 4
- 37 44
- (5) {2}

3

- [a] :: 3x 5 > 13 $\therefore 3 \times > 18$  $\therefore x > 6$  $\therefore$  The S.S. =  $\{7, 8, 9, \dots\}$
- **[b]**  $\frac{16}{9} \times \frac{9}{4} \times 1 = 4$

- [a]  $12 \times 4 + 24 + 9 = 48 + 24 + 9 = 81$
- **[b]** ::  $3 \times 13 = 26$  $\therefore 3 \times = 39$  $\therefore x = 13$  $\therefore$  The S.S. = {13}

[a] 
$$\frac{(2)^7 \times (2)^5}{(2)^6 \times (2)^3} = \frac{2^{12}}{2^9} = 2^{12-9} = 2^3 = 8$$

- [b] (1) The probability of getting a prime number  $=\frac{0}{6}=\frac{1}{2}$ 
  - (2) The probability of getting a number more than  $6 = \frac{0}{6} = 0$

# Assiut

1

(5) 13,21 (1)1 (2) 10 (3) zero (4) 14

2

(1) (b) (4) (a) (S) (C) (3) (b) (5) (b)

3

- $\therefore 3x 2x \le 3 + 1$ [a] (1) ::  $3x - 1 \le 2x + 3$ : X≤4
  - $\therefore \text{ The S.S.} = \{x : x \in \mathbb{Q}, x \le 4\}$
- $\therefore 3 \times = 6 \qquad \therefore \times = 2 \qquad \therefore \text{ The S.S.} = \{2\}$
- $[\mathbf{b}] \frac{1}{9} + \frac{8}{9} 1 = 0$

- [a] :: 5 x 2 x = 30 :: 3 x = 30
- $\therefore x = 10$
- .. The two numbers are: 20 and 50
- [b]  $\left(\frac{-4}{5}\right)^6 \div \left(\frac{4}{5}\right)^4 = \left(\frac{4}{5}\right)^6 \div \left(\frac{4}{5}\right)^4 = \left(\frac{4}{5}\right)^2 = \frac{16}{25}$

### 5

- [a]  $(5.4 \times 10^4) + (3.7 \times 10^5) = (5.4 + 3.7 \times 10) \times 10^4$  $= (5.4 + 37) \times 10^4 = 42.4 \times 10^4 = 4.24 \times 10^5$
- [b] (1) The probability that the ball is red =  $\frac{5}{15} = \frac{1}{3}$ 
  - (2) The probability that the ball is white or red  $=\frac{4+5}{15}=\frac{9}{15}=\frac{3}{5}$

# Qena

1

- (1)(c)
- (2) (c)
- (3) (c)
- (4) (a)
- (5) (d)

2

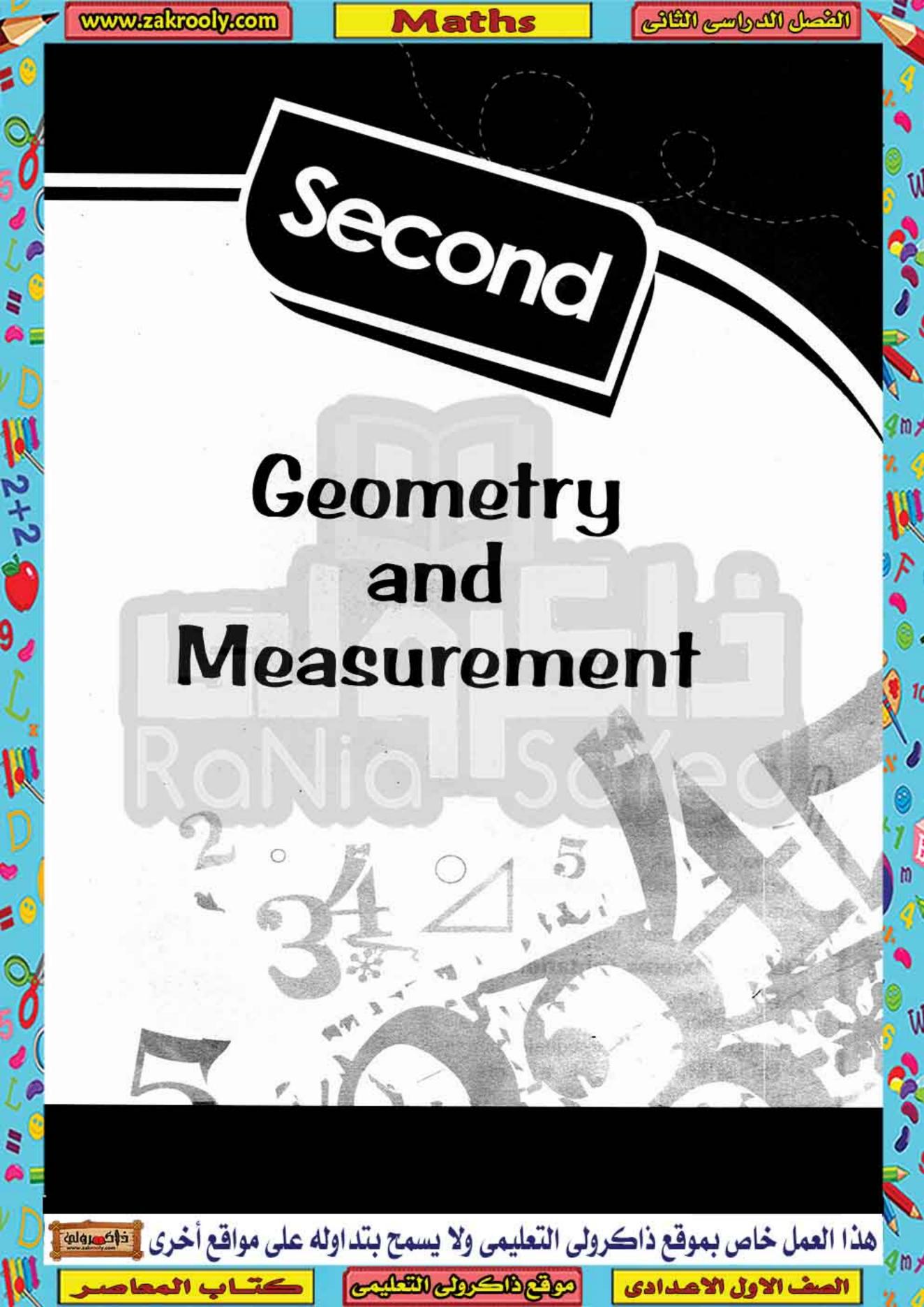
- 1)4
- (2) X + 5 (3) zero (4) 5
- (5)  $\frac{7}{2}$

3

- [a] : 5x 6 = 34
- $\therefore 5 x = 40$
- $\therefore x = 8$
- :. The S.S. =  $\{8\}$
- [b]  $\frac{16}{9} \times \frac{3}{4} \times \frac{3}{4} = 1$

- [a]  $:: 5x-2 \ge 2x+1 :: 5x-2x \ge 1+2$ 
  - :.3 X≥3
- $\therefore$  The S.S. =  $\{1, 2, 3, ....\}$
- [b]  $y \div x^2 = \frac{3}{4} \div \left(\frac{-1}{2}\right)^2 = \frac{3}{4} \div \frac{1}{4} = \frac{3}{4} \times 4 = 3$

- [a]  $\frac{7^3 \times (7)^{-4}}{(-7)^4 \times (7)^{-3}} = \frac{7^3 \times (7)^{-4}}{7^4 \times (7)^{-3}} = \frac{7^{-1}}{7} = 7^{-1-1} = 7^{-2} = \frac{1}{49}$
- [b] (1) The probability of an odd number =  $\frac{5}{10} = \frac{1}{2}$ 
  - (2) The probability of an even number =  $\frac{5}{10} = \frac{1}{2}$
  - (3) The probability of a prime number =  $\frac{4}{10} = \frac{2}{5}$





# **Geometry and Measurement**

: Deductive proof. **Lesson One** 

: The polygon. Lesson Two

**Lesson Three** : The parallelogram and its properties.

: The special cases of the parallelogram. **Lesson Four** 

**Lesson Five** : The triangle :

- Theorem (1), exterior angle of the triangle.

Lesson Six : Theorem (2), theorem (3).

**Lesson Seven** : Pythagoras' theorem.

: Geometric transformations. **Lesson Eight** 

**Lesson Nine** : Reflection in a straight line.

: Reflection in a point. Lesson Ten

Lesson Eleven: Translation. Lesson Twelve: Rotation.

# Euclid (325 B.C. - 265 B.C.)

He was a Greek mathematician. He lived in Alexandria. Euclid introduced the system of axioms. Since this time, geometry of Euclid was considered a model of logical proof.

### **Euclid's Axioms (notations):**

- Things which are equal to one thing are equal to each other.
- If equals are added to equals, then the sums are equal.
- Things which coincide with one another are equal to each other.
- The whole is greater than the part.



Euclid (325 BC - 265 BC)

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى العيف الاول الاعدادي مصطح الكري العيف المعادي

Lesson One



# Deductive proof

In the previous term, we had trained practically how to deduce some properties and theorems by measuring and using the geometric tools.

In this lesson, we will use the geometric properties that we had known before to deduce the solutions and proof for theorems and problems theoritically without going to the geometric tools in measure.

Also, in this lesson, we will give some examples to show how to use the deductive proof to prove some geometric theorems and problems.

But before that, we will give you some advices about how to write the proof in geometry.

### How to write the proof in geometry ? •

- Read the problem very good to understand all its parts. This may require to read it more than one time.
- 2 Write "The given" which are all information given in the problem.
- 3 Write "The required" which is the required to find or to prove.
- 4 Check the existence of a right mathematical figure expressing the problem. If there is no figure, draw it by yourself using the information given in the problem.
- Put on the figure all the possible information given in the problem as: side lengths angle measures signs showing the equality of side lengths signs showing the equality of angle measures signs showing the parallelism and so on.
- Think how to use the given information, the facts and the theorems you studied before to get the required.
  - Write mathematical sentences, knowing that you must write a reason to each writen sentence (if this sentence isn't one of the given information in the problem), for example: You can't write  $m (\angle A) = m (\angle B)$  without writting a mathematical reason as  $\angle A$  and  $\angle B$  are alternate angles resulted from cutting two parallel straight lines by another line.
- 7 Continue writting these sentences till getting one sentence expressing the required.

  Thus, you finish the proof.

In the following, some examples showing how to write the deductive proof:

If two straight lines intersect , then the measures of each two vertically opposite angles are equal.

61





الصف الاول الاعدادي

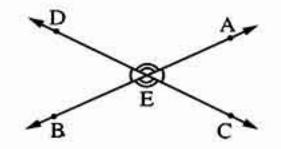
🕒 Unit 🏅

Given

AB and CD are two straight lines

the given information

intersecting at E



Required to prove (R.T.P.)

$$m (\angle AED) = m (\angle BEC)$$

what we want to find or prove

Proof

- ∴ ∠ AED and ∠ AEC are two adjacent angles where  $\overrightarrow{EC} \cup \overrightarrow{ED} = \overrightarrow{CD}$
- $\therefore$  m ( $\angle$  AED) + m ( $\angle$  AEC) = 180°
- , ∵ ∠ AEC and ∠ BEC are two adjacent angles where  $\overrightarrow{EA} \cup \overrightarrow{EB} = \overrightarrow{AB}$

The steps of proving the truth of the required.

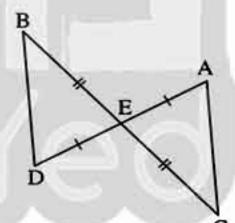
- $\therefore$  m ( $\angle$  AEC) + m ( $\angle$  BEC) = 180°
- $\therefore$  m ( $\angle$  AED) + m ( $\angle$  AEC) = m ( $\angle$  AEC) + m ( $\angle$  BEC)
- (Q.E.D.)  $\therefore$  m ( $\angle$  AED) = m ( $\angle$  BEC) Similarly, you can prove that  $m (\angle AEC) = m (\angle BED)$

### Example (1)

In the opposite figure:

 $\overline{AD} \cap \overline{BC} = \{E\}$  where AE = DE and BE = CE

Prove that :  $\triangle$  AEC  $\equiv$   $\triangle$  DEB



### Solution

Proof

 $\overline{AD} \cap \overline{BC} = \{E\}$  where  $AE = DE \cdot BE = CE$ Given

R.T.P.  $\Delta AEC \equiv \Delta DEB$ 

 $\therefore \overline{AD} \cap \overline{BC} = \{E\} \qquad \therefore m (\angle AEC) = m (\angle DEB) (V.O.A)$ 

∴ In ΔΔ AEC and DEB:

$$\begin{cases} AE = DE \text{ (given)} \\ CE = BE \text{ (given)} \\ m (\angle AEC) = m (\angle DEB) \text{ (by proof)} \end{cases}$$

 $\therefore \Delta AEC \equiv \Delta DEB$ (Q.E.D.)

\* Q.E.D. is an abbreviation for quod erat demonstrandum. It is a Latin abbreviation which means to be demonstrated

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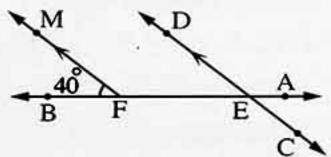
Lesson One

### Try by yourself

In the opposite figure:

 $\overrightarrow{AB} \cap \overrightarrow{CD} = \{E\}, \overrightarrow{CD} / \overrightarrow{FM}, F \in \overrightarrow{AB} \text{ and } m (\angle MFB) = 40^{\circ}$ 

Find with proof: m (∠ AEC)



### Solution

Given

Required to

find (R.T.F.)

Proof

: CD // ..... (given) and AB is a transversal.

 $\therefore$  m ( $\angle$  DEB) = m ( $\angle$  .....) = 40° (corresponding angles)

 $\therefore \overrightarrow{AB} \cap \overrightarrow{CD} = \{E\}$ 

 $\therefore$  m ( $\angle$  AEC) = m ( $\angle$  ······) (V.O.A)

∴ m (∠ AEC) = ······°

(The req.)

# The sum of the measures of the accumulative angles at a point is equal to 360°

Given

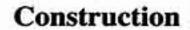
 $\overrightarrow{OA}$ ,  $\overrightarrow{OB}$ ,  $\overrightarrow{OC}$  and  $\overrightarrow{OD}$  are rays

that start at O

R.T.P. The sum of the measures of

the accumulative angles at

O is 360°



Draw DO and E € DO

Proof

 $m (\angle EOB) + m (\angle BOA) + m (\angle AOD) = 180^{\circ}$ 

 $, m (\angle EOC) + m (\angle COD) = 180^{\circ}$ 

 $\therefore$  m ( $\angle$  EOB) + m ( $\angle$  BOA) + m ( $\angle$  AOD) + m ( $\angle$  EOC)

 $+ m (\angle COD) = 180^{\circ} + 180^{\circ} = 360^{\circ}$ 

 $\therefore$  m ( $\angle$  AOB) + m ( $\angle$  BOC) + m ( $\angle$  COD) + m ( $\angle$  DOA) = 360°

(Q.E.D.)

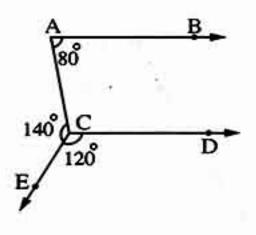
# Example (2)

In the opposite figure:

$$m (\angle BAC) = 80^{\circ} , m (\angle DCE) = 120^{\circ}$$

and m (
$$\angle$$
 ACE) = 140°

Prove that : AB // CD



### Solution

Given  $\mid m (\angle BAC) = 80^{\circ}, m (\angle DCE) = 120^{\circ},$  $m (\angle ACE) = 140^{\circ}$ 

AB // CD R.T.P.

Proof  $m (\angle DCA) + m (\angle DCE) + m (\angle ACE) = 360^{\circ}$ (accumulative angles at C)

$$\therefore$$
 m ( $\angle$  DCA) = 360° - (120° + 140°) = 100°

:. 
$$m (\angle BAC) + m (\angle DCA) = 80^{\circ} + 100^{\circ} = 180^{\circ}$$

And they are interior angles in the same side of the transversal AC

: AB // CD

(Q.E.D.)

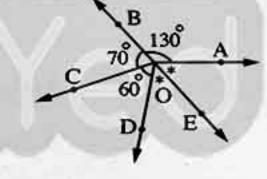
### Try by yourself

In the opposite figure:

$$m (\angle AOB) = 130^{\circ} \cdot m (\angle BOC) = 70^{\circ} \cdot$$

m (
$$\angle$$
 COD) = 60° and  $\overrightarrow{OE}$  bisects  $\angle$  AOD

Prove that OE and OB are on one straight line.



Given

R.T.P.

Proof

 $m (\angle AOB) + m (\angle BOC) + m (\angle COD) + m (\angle AOD) = \dots ^{\circ}$ (Accumulative angles at O)

$$\therefore m (\angle AOE) = \frac{1}{2} m (\angle \cdots )$$

$$\therefore$$
 m ( $\angle$  AOE) =  $\frac{1}{2} \times \dots \circ$  =  $\dots \circ$ 

(Q.E.D.)

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Lesson Two



# The polygon

### The simple line and non-simple line:

The simple line: It is the line that does not cut itself.

The non-simple line: It is the line that cuts itself once or more.

### The closed line and the open line:

The closed line: It is the line that ends where it starts at the same point.

It may be simple or non-simple.

The open line : It is the line whose starting point is not the end point.

It may be simple or non-simple.

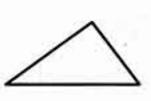
In the following, there are some figures which show simple lines and non-simple lines , closed lines or open lines :

Simple line		Non-simple line	
Closed	Open	Closed	Open
		9	2

### The polygon

It is a simple closed line that consists of three line segments, or more. The polygon is named according to the number of its sides.

### Examples for some polygons:



Triangle (3 sides)



Quadrilateral (4 sides)



Pentagon (5 sides)



Heptagon (7 sides)

الحاصد رياضيات لغات /١ إعدادي / تيرم ٢ (م : ٩)



Octagon (8 sides)

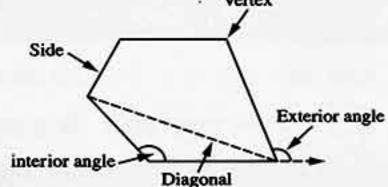
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### Remarks

- Each line segment of the line segments forming the polygon is called a side.
- 2 Each point resulted from intersecting of two adjacent sides of the polygon is called a vertex.
- 3 The sum of the side lengths of the polygon is called the perimeter of the polygon.
- 4 Each line segment joining two non-adjacent vertices of the polygon is called a diagonal of the polygon.

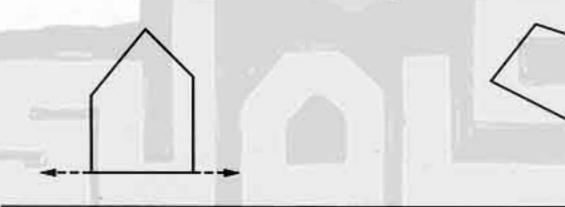


- 5 The included angle between two adjacent sides of the polygon is called an interior angle.
- 6 The included angle between a side of the polygon and the extension of its adjacent side is called an exterior angle.

### Convex polygon and concave polygon:

### In the convex polygon:

If a straight line is drawn to pass through any two consecutive vertices, then the remained vertices lie on one side of this straight line as shown in the two figures.

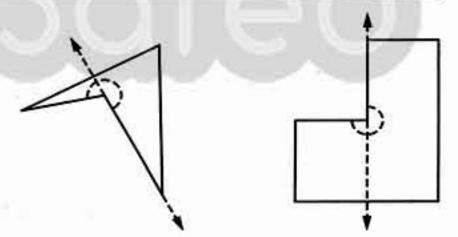


### Notice that :

Any interior angle of the convex polygon has measure less than 180°

### In the concave polygon:

There are straight lines (one at least) passing through two consecutive vertices and the remained vertices lie on two different sides of the straight line as shown in the two opposite figures.



### Notice that :

There is at least one interior angle of concave polygon of measure more than 180° (reflex angle).

### The sum of measures of the interior angles of the polygon:

We knew before that: The sum of measures of the interior angles of the triangle equals 180° We can use that to deduce a general rule to find the sum of measures of the interior angles of any polygon whose number of sides is n as follows.

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Lesson Two

If we draw from any vertex of the polygon all diagonals that pass through this point, then the surface of this polygon will be divided into a number of triangles as shown in the following table:

The polygon	The number of its sides	The number of the resulting triangles	The sum of measures of the interior angles of the polygon  2 × 180° = 360°	
quadrilateral	4	2		
2 1 pentagon	5	3	3 × 180° = 540°	
hexagon	6	4	4 × 180° = 720°	
heptagon	7	5	5 × 180° = 900°	

### From the previous , we deduce that :

The number of triangles is less than the number of the sides by 2

Generally: If the number of sides of the polygon is "n" sides,

then the number of triangles resulting from drawing all the diagonals that pass through a vertex of the polygon = (n-2) triangles.

- : The sum of measures of the interior angles of the triangle = 180°
- ∴ The sum of measures of the interior angles of a polygon of n sides equals (n 2) × 180°

# For example:

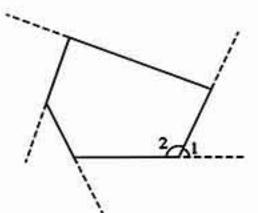
• The sum of measures of the interior angles of the octagon =  $(8-2) \times 180^{\circ} = 1080^{\circ}$ 

Unit 🏅

- The sum of measures of the interior angles of the enneagon (nonagon)  $= (9-2) \times 180^{\circ} = 1260^{\circ}$
- The sum of measures of the interior angles of the decagon = (10 − 2) × 180° = 1440°

The sum of measures of the exterior angles of the convex polygon which has n sides:

 We mentioned that the exterior angle of the polygon is the angle included between one side and the extension of its adjacent side, and although we can draw two exterior angles equal in measure at each vertex of the polygon, but the rule of the sum of measures of the exterior angles use only one exterior angle at each vertex.



• At any vertex of the polygon, we find that the sum of measures of the interior angle and the exterior angle = 180°

In the previous figure :  $m (\angle 1) + m (\angle 2) = 180^{\circ}$ 

as an example.

In the previous pentagon, we find that the sum of measures of the five exterior and five interior angles of the pentagon =  $5 \times 180^{\circ}$ 

Since the sum of measures of the interior angles equals  $3 \times 180^{\circ}$ 

 $\therefore$  The sum of measures of the five exterior angles of the pentagon =  $2 \times 180^{\circ} = 360^{\circ}$ 

We can deduce that for any convex polygon of n sides as follows:

The sum of measures of the exterior angles + the sum of measures of the interior angles =  $n \times 180^{\circ}$ 

- ... The sum of measures of the exterior angles +  $(n-2) \times 180^{\circ} = n \times 180^{\circ}$
- $\therefore$  The sum of measures of the exterior angles =  $n \times 180^{\circ} (n-2) \times 180^{\circ}$  $= 180^{\circ} \text{ n} - 180^{\circ} \text{ n} + 360^{\circ} = 360^{\circ}$

So we get : •

The sum of measures of the exterior angles of a convex polygon of n sides = 360° (taking into account one exterior angle at each vertex)

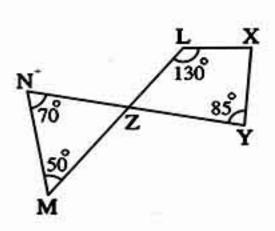


In the opposite figure:

$$\overline{LM} \cap \overline{YN} = \{Z\}, m (\angle M) = 50^{\circ},$$

$$m (\angle N) = 70^{\circ} \cdot m (\angle Y) = 85^{\circ} \text{ and }$$
  
 $m (\angle L) = 130^{\circ}$ 

Find:  $m (\angle X)$ 



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## Solution

 $|m (\angle M) = 50^{\circ}, m (\angle N) = 70^{\circ}, m (\angle Y) = 85^{\circ}, m (\angle L) = 130^{\circ}$ Given

R.T.F.  $m (\angle X)$ 

Proof In  $\triangle$  ZMN:

$$m (\angle M) = 50^{\circ}, m (\angle N) = 70^{\circ}$$

$$\therefore$$
 m ( $\angle$  NZM) = 180° - (50° + 70°) = 60°

$$:: m (\angle LZY) = m (\angle NZM)$$
 (V.O.A.)

$$\therefore$$
 m ( $\angle$  LZY) = 60°

: The figure XYZL is a quadrilateral.

... The sum of measures of its interior angles = 360°

$$\therefore$$
 m ( $\angle X$ ) = 360° - (130° + 85° + 60°) = 85° (The req.)

If the ratio among the measures of the interior angles of a quadrilateral is 2:3:3:4,

find the smallest measure of these angles of that quadrilateral.

# Solution

.. The sum of measures of the interior angles of the quadrilateral

$$= (4-2) \times 180^{\circ} = 2 \times 180^{\circ} = 360^{\circ}$$

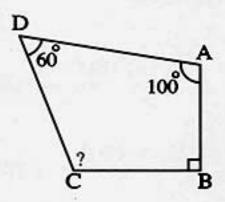
$$\therefore 2 \times + 3 \times + 3 \times + 4 \times = 360^{\circ}$$

∴ 12 
$$x = 360^{\circ}$$
 ∴  $x = \frac{360^{\circ}}{12} = 30^{\circ}$ 

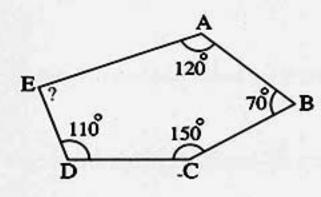
: The smallest measure = 
$$2 \times 12$$
 : The smallest measure of the angles =  $2 \times 30^{\circ} = 60^{\circ}$ 

# ny by yourself

Complete each of the following by using the given data for each figure:



- : The sum of measures of the interior angles of the figure = ······°
- ∴ m (∠ C) = ······°



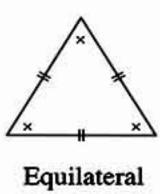
- : The sum of measures of the interior angles of the figure = ......°
- ∴ m (∠ E) = ······°

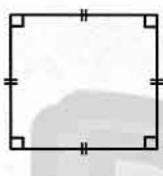
# The regular polygon :

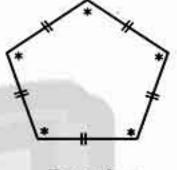
The polygon is regular if : •

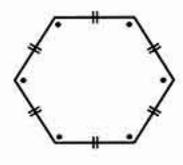
- All its sides are equal in length.
- 2 All its angles are equal in measure.

### As examples for the regular polygons:









triangle

Square

Regular pentagon

Regular hexagon

# The measure of the interior angle of a regular polygon :

We knew that the sum of measures of the interior angles of a polygon of n-sides  $=(n-2)\times180^{\circ}$ 

### Then:

If the polygon is regular, then its interior angles (whose number is n) are equal in measure.

... The measure of each interior angle of the regular polygon of n-sides =  $\frac{(n-2) \times 180^{\circ}}{}$ 

# For example:

- The measure of each interior angle of the equilateral triangle =  $\frac{(3-2) \times 180^{\circ}}{2}$  = 60°
- The measure of each interior angle of the square =  $\frac{(4-2) \times 180^{\circ}}{4}$  = 90°
- The measure of each interior angle of the regular pentagon =  $\frac{(5-2) \times 180^{\circ}}{5}$  = 108°
- The measure of each interior angle of the regular hexagon =  $\frac{(6-2) \times 180^{\circ}}{6}$  = 120°

Lesson Two



The measure of one of the interior angles of a regular polygon is 144° Find the number of its sides.

### Solution

: The measure of each interior angle of the regular polygon of n-sides =  $\frac{(n-2) \times 180^{\circ}}{}$ 

$$\therefore \frac{(n-2)\times 180^{\circ}}{n} = 144^{\circ}$$

∴ 
$$(n-2) \times 180^{\circ} = 144^{\circ} \text{ n}$$

$$180^{\circ} \text{ n} - 144^{\circ} \text{ n} = 360^{\circ}$$

$$n = 10$$

.. The number of sides = 10 sides.

# **Another solution**

: The measure of the exterior angle of the polygon = 180° - the measure of the interior angle

$$= 180^{\circ} - 144^{\circ} = 36^{\circ}$$

- : The sum of the measures of the exterior angles = 360°
- ... The number of exterior angles =  $\frac{360^{\circ}}{36^{\circ}}$  = 10 angles
- ... The number of sides = 10 sides.

### Notice that :

The number of the polygon sides

- = The number of its vertices
- = The number of its interior angles
- = The number of its exterior angles

# Remark

The number of sides of the regular polygon in which the measure of one of its interior angles is  $\chi^{\circ} = \frac{360^{\circ}}{180^{\circ} - \chi}$ 

# For example :

The number of sides of the regular polygon which the measure of one of its interior angles is  $144^{\circ} = \frac{360^{\circ}}{180^{\circ} - 144^{\circ}} = 10$  sides.

# Complete the following table:

The number of sides of the regular polygon	3	- 5	12	N	
The measure of one of its interior angles	°		°	135°	160°

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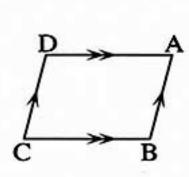
# Lesson

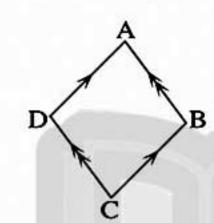
# The parallelogram and its properties

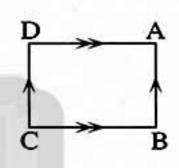


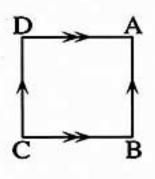
Definition:

A parallelogram is a quadrilateral, in which each two opposite sides are parallel.





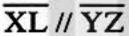


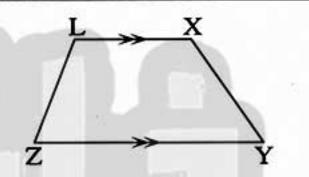


Each of the above figures is called a parallelogram for  $\overline{AB}$  //  $\overline{DC}$  and  $\overline{AD}$  //  $\overline{BC}$ 

Notice that : |

A quadrilateral in which only two sides are parallel is called a trapezium, as shown in the opposite figure in which:





## Properties of a parallelogram:

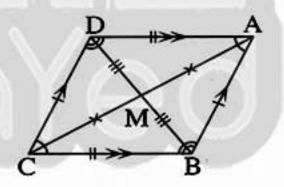
In the opposite figure:

ABCD is a parallelogram whose diagonals

AC and BD intersect at M

We can deduce

the following properties:



The sum of measures of each two consecutive angles in a parallelogram is 180°

*i.e.* • m (
$$\angle$$
 A) + m ( $\angle$  B) = 180°

• m (
$$\angle$$
 C) + m ( $\angle$  D) = 180°

• m (
$$\angle$$
 B) + m ( $\angle$  C) = 180°

• m (
$$\angle$$
 D) + m ( $\angle$  A) = 180°

In a parallelogram, each two opposite angles are equal in measure

i.e. • 
$$m (\angle A) = m (\angle C)$$

• m (
$$\angle$$
 B) = m ( $\angle$  D)

In a parallelogram, each two opposite sides are equal in length

$$i.e. \cdot AB = CD$$

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Lesson Three

# The two diagonals in a parallelogram bisect o

$$i.e. \cdot AM = CM$$

$$\bullet$$
 BM = DM

### Remark

The perimeter of the parallelogram = The sum of two consecutive sides  $\times 2$ 

### In the opposite figure:

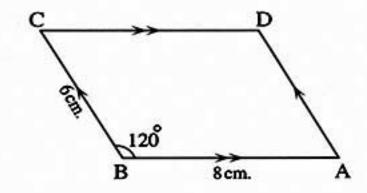
ABCD is a parallelogram in which:

AB = 8 cm. 
$$_{2}$$
BC = 6 cm. and m ( $\angle$  B) = 120°

Find: 1 The length of each of CD and DA

2 The measure of each of ∠ D , ∠ A and ∠ C

3 The perimeter of ABCD



### Solution

ABCD is a parallelogram, AB = 8 cm., BC = 6 cm.Given

and m ( $\angle$  B) = 120°

1 CD and DA R.T.F.

2 m  $(\angle D)$ , m  $(\angle A)$  and m  $(\angle C)$ 

3 The perimeter of ABCD

Proof : ABCD is a parallelogram

> $\therefore$  CD = AB = 8 cm. (Properties of a parallelogram)

and DA = CB = 6 cm. (First req.) (Properties of a parallelogram)

 $, m (\angle D) = m (\angle B) = 120^{\circ}$ (Properties of a parallelogram)

 $\rightarrow m (\angle A) + m (\angle B) = 180^{\circ}$ (Properties of a parallelogram)

 $, m (\angle B) = 120^{\circ}$ 

 $m (\angle A) = 180^{\circ} - 120^{\circ} = 60^{\circ} \text{ and } m (\angle C) = m (\angle A) = 60^{\circ}$ (Second req.)

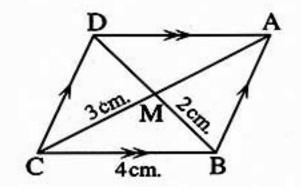
The perimeter of ABCD =  $(AB + BC) \times 2$ 

 $= (8 + 6) \times 2 = 14 \times 2 = 28$  cm. (Third req.)



### In the opposite figure:

ABCD is a parallelogram whose diagonals intersect at M If BC = 4 cm., BM = 2 cm. and MC = 3 cm., then find the perimeter of  $\triangle$  AMD



## Solution

Given

ABCD is a parallelogram whose diagonals intersect at  $M \cdot BC = 4 \text{ cm.}$ 

BM = 2 cm. and MC = 3 cm.

R.T.F.

**Proof** 

The perimeter of  $\triangle$  AMD

: ABCD is a parallelogram

 $\therefore$  BC = AD = 4 cm. (Two opposite sides in a parallelogram)

.. The two diagonals bisect each other

 $\therefore$  MD = MB = 2 cm. and AM = MC = 3 cm.

 $\therefore$  The perimeter of  $\triangle$  AMD = AD + MD + AM = 4 + 2 + 3 = 9 cm.

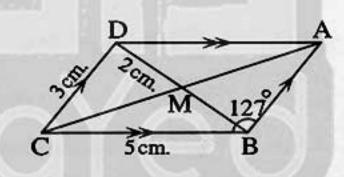
(The req.)

### In the opposite figure:

ABCD is a parallelogram whose diagonals intersect at M

If BC = 5 cm., DC = 3 cm., DM = 2 cm.

and m ( $\angle$  ABC) = 127°,



complete the following:

 $AB = \cdots cm$ , and  $AD = \cdots cm$ 

 $m (\angle ADC) = \cdots \circ m (\angle BAD) = \cdots \circ and m (\angle BCD) = \cdots \circ$ 

The perimeter of  $\square$  ABCD = ..... cm.

# When does a quadrilateral represent a parallelogram?

A quadrilateral represents a parallelogram if one of the following conditions satisfies

Each two opposite sides are parallel.

Each two opposite sides are equal in length.

Two opposite sides are parallel and equal in length.

Each two opposite angles are equal in measure

The two diagonals bisect each other.

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Lesson Three

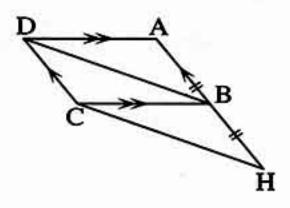


### In the opposite figure:

ABCD is a parallelogram → H ∈ AB

where AB = BH

Prove that: BHCD is a parallelogram



# Solution

Given ABCD is a parallelogram and AB = BH

R.T.P. BHCD is a parallelogram.

Proof : ABCD is a parallelogram

∴ AB = CD

 $\therefore$  AB = BH (Given)

∴ DC = BH

(1)

: AB // DC , H ∈ AB

∴ BH // DC

(2)

From (1) and (2):

.. DC = BH and DC // BH

.. BHCD is a parallelogram

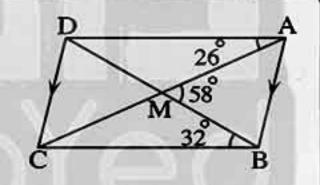
(Q.E.D.)

### In the opposite figure:

ABCD is a quadrilateral, its diagonals intersect at M,

AB // CD,  $m (\angle AMB) = 58^{\circ}$ ,  $m (\angle MBC) = 32^{\circ}$ 

and m ( $\angle$  MAD) = 26°



# Complete the following proof to prove that ABCD is a parallelogram.

Given R.T.P.

**Proof**  $: M \in \overline{AC}$ 

∴ m (∠ BMC) = 180° – ·····° = ·····°

The large interprise of the state of the state of

 $\therefore$  m ( $\angle$  MCB) = m ( $\angle$  ..........) and they are ......... angles

.....// ...... · .....// ..... -(Given)

.. ABCD is a parallelogram.

(Q.E.D.)



# Lesson

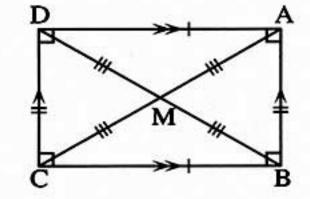
# The special cases of the parallelogram

A rectangle is a parallelogram with a right angle.

- Properties of the rectangle :
  - The rectangle has the same properties as the parallelogram in addition :
    - The four angles of a rectangle are all equal in measure and the measure of each is 90°

*i.e.* 
$$m (\angle A) = m (\angle B) = m (\angle C) = m (\angle D) = 90^{\circ}$$

2 The two diagonals of a rectangle are equal in length.



- i.e. AC = BD and as the two diagonals bisect each other, then AM = BM = CM = DM, where M is the point of intersection of the two diagonals.
- The perimeter of the rectangle = (length + width)  $\times$  2

A rhombus is a parallelogram in which two adjacent sides are equal in length.

- Properties of the rhombus:
  - The rhombus has the same properties as the parallelogram in addition :
    - The four sides of a rhombus are all equal in length.

$$i.e.$$
 AB = BC = CD = DA

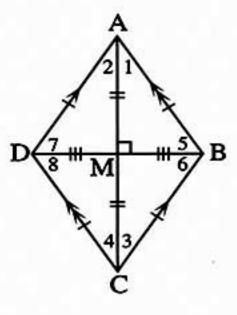
2 The two diagonals of the rhombus are perpendicular and bisect each of its interior angles.

*i.e.* 
$$\bullet \overline{AC} \perp \overline{BD}$$

• m (
$$\angle$$
 1) = m ( $\angle$  2) = m ( $\angle$  3) = m ( $\angle$  4)

• 
$$m (\angle 5) = m (\angle 6) = m (\angle 7) = m (\angle 8)$$





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هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى إلى العمف الاول الاعدادي مواقع أخرى إلى العمف الاول الاعدادي معطى العمولي العمدادي المعمدادي العمدادي ال

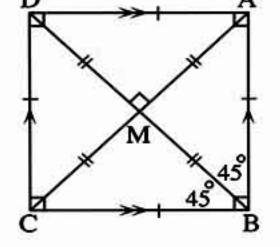


A square is a parallelogram with a right angle and two adjacent sides equal in length.

- Properties of the square :
  - The square has the same properties as the parallelogram in addition :
    - I Its four sides are all equal in length

$$i.e.$$
 AB = BC = CD = DA

2 Its four angles are all equal in measure and each of them is of measure 90°



- i.e.  $m(\angle A) = m(\angle B) = m(\angle C) = m(\angle D) = 90^{\circ}$
- 3 Its two diagonals are equal in length, perpendicular and each diagonal bisects the two vertices angles which this diagonal joins.

*i.e.* • AC = BD and hence AM = BM = CM = DM , where 
$$\overline{AC} \cap \overline{BD} = \{M\}$$

- AC ⊥ BD
- m ( $\angle$  ABD) = m ( $\angle$  CBD) = 45°
- The perimeter of the square = the length of one side  $\times$  4

# Notice that :

We can also define the square as follows:

- A square is a rectangle with two adjacent sides equal in length.
- 2 A square is a rectangle with two perpendicular diagonals.
- 3 A square is a rhombus with a right angle.
- 4 A square is a rhombus with two diagnals equal in length.

### Notice that :

To prove that the quadrilateral is a rectangle, a rhombus or a square, we must first prove that it is a parallelogram, as we see in the previous lesson, then:

Unit 3

# The parallelogram is

### a rectangle

### if:

One of its angles is a right angle

or

Its two diagonals are equal in length.

### a rhombus

### if:

Two adjacent sides are equal in length.

or

Its two diagonals are perpendicular.

### a square

### if:

One of its angles is right and two adjacent sides are equal in length.

or

One of its angles is right and its two diagonals are perpendicular.

or

Its two diagonals are perpendicular and equal in length.

or

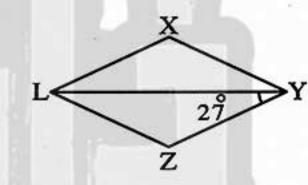
Two adjacent sides are equal in length and its two diagonals are equal in length.



### In the opposite figure:

XYZL is a rhombus in which m ( $\angle$  LYZ) = 27°

Calculate the measures of the angles of the rhombus XYZL



# Solution

### Given

XYZL is a rhombus in which m ( $\angle$  LYZ) = 27°

R.T.F.

 $m (\angle XYZ), m (\angle XLZ), m (\angle X) \text{ and } m (\angle Z)$ 

Proof

- ∵ YL is a diagonal in the rhombus XYZL
- ∴ YL bisects ∠ XYZ

- $\therefore$  m ( $\angle$  XYZ) = 2 × 27° = 54°
- , : Each two opposite angles in the rhombus are equal in measure.
- $\therefore m (\angle XLZ) = 54^{\circ}$
- : The rhombus is a special case of the parallelogram
- $\therefore m (\angle X) + m (\angle XYZ) = 180^{\circ}$
- $\therefore m (\angle X) + 54^{\circ} = 180^{\circ}$

 $\therefore$  m ( $\angle X$ ) = 126°

 $\therefore$  m ( $\angle$  Z) = 126°

(The req.)

Try to solve this example by another method using the properties of the rhombus

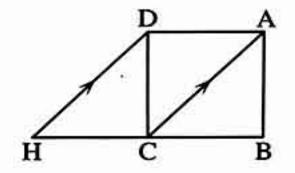
Lesson Four

### In the opposite figure:

ABCD is a square. Draw DH // AC to intersect BC at H

Prove that : CH = BC

2 Find:  $m (\angle ADH)$ 



# Solution

ABCD is a square and DH // AC Given

R.T.P. CH = BC

R.T.F.  $m (\angle ADH)$ 

Proof : AD // BC (Two opposite sides in the square) and H∈BC

∴ AD // CH

: DH // AC (Given)

.. ACHD is a parallelogram

:. CH = AD

But AD = BC (Two opposite sides in the square)

:. CH = BC : AC is a diagonal in the square

∴ CA bisects ∠ BCD

: m (∠ BCD) = 90°

 $\therefore$  m ( $\angle$  ACD) = 45°

: DH // AC and CD is their transversal

 $\therefore$  m ( $\angle$  CDH) = m ( $\angle$  ACD) = 45° (Two alternate angles)

• :  $m (\angle ADC) = 90^{\circ} (Property of the square)$ 

 $\therefore m (\angle ADH) = m (\angle ADC) + m (\angle CDH)$ 

 $=90^{\circ} + 45^{\circ} = 135^{\circ}$ 

(Second req.)

(First req.)

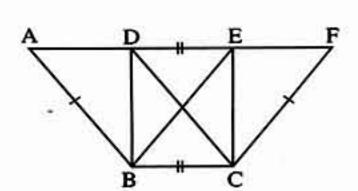


### In the opposite figure:

ABCD, EBCF are two parallelograms,

D and E belong to  $\overrightarrow{AF}$ ,  $\overrightarrow{AB} = FC$ ,  $\overrightarrow{BC} = \overrightarrow{DE}$ 

Prove that: The figure DBCE is a rectangle.



## Solution

Given

ABCD and EBCF are two parallelograms AB = FC BC = DE

R.T.P.

The figure DBCE is a rectangle.

Proof

:. AD // BC : ABCD is a parallelogram.

, ∵ D and E belong to AF

∴ DE // BC , :: DE = BC.. DBCE is a parallelogram.

, : ABCD is a parallelogram.

 : EBCF is a parallelogram.  $\therefore$  FC = EB but : AB = FC

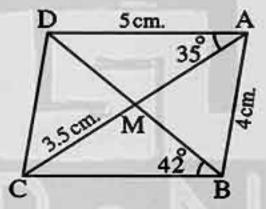
 $\therefore$  DC = EB

.. DBCE is a parallelogram and its diagonals are equal in length.

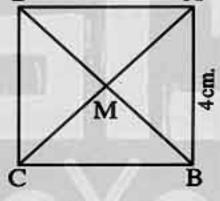
.. DBCE is a rectangle.

(Q.E.D.)

Using the given in each figure, complete where M is the intersection point of the diagonals:



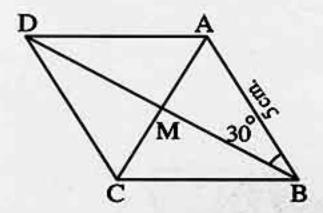
- ABCD is a parallelogram :
  - The perimeter of  $\triangle$  ABC = ......... cm.
  - m (∠ AMB) = ······°



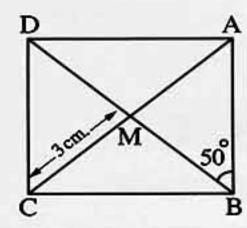
ABCD is a square :

 $\therefore AB = DC$ 

- The perimeter of the square = ..... cm.
- m (∠ BAC) = .....°



- ABCD is a rhombus :
  - AD = ..... cm.
  - m (∠ BAM) = ······°



- ABCD is a rectangle :
  - BD = ..... cm.
  - m (∠ MCD) = ······°

Lesson Five



# The triangle

### Theorem (1):

The sum of the measures of the interior angles of a triangle is 180°

Given

ABC is a triangle

Draw CX // AB

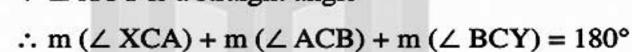
R.T.P.

$$m (\angle A) + m (\angle B) + m (\angle ACB) = 180^{\circ}$$

Construction

∵ ∠ XCY is a straight angle

**Proof** 



$$\therefore \overrightarrow{XY} // \overrightarrow{AB}$$

$$\therefore$$
 m ( $\angle$  XCA) = m ( $\angle$  A) (alternate angles)

$$, m (\angle YCB) = m (\angle B)$$

(alternate angles)

$$\therefore m (\angle A) + m (\angle ACB) + m (\angle B) = 180^{\circ}$$

(Q.E.D.)



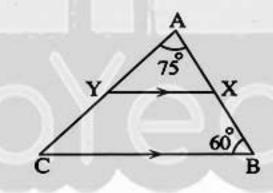
# In the opposite figure:

ABC is a triangle in which  $m (\angle A) = 75^{\circ}$ ,

m (
$$\angle$$
 B) = 60°,  $X \in \overline{AB}$  and  $Y \in \overline{AC}$ 

such that  $\overline{XY} /\!/ \overline{BC}$ 

Find: m (∠ AYX)



# Solution

Given

$$\overline{XY} // \overline{BC}$$
, m ( $\angle A$ ) = 75° and m ( $\angle B$ ) = 60°

R.T.F.

 $m (\angle AYX)$ 

**Proof** 

$$\therefore$$
 m ( $\angle$  A) = 75° and m ( $\angle$  B) = 60° (given)

, The sum of measures of the interior angles of  $\Delta$  ABC = 180°

$$\therefore$$
 m ( $\angle$  C) = 180° - (75° + 60°) = 180° - 135° = 45°

.. XY // BC and AC is a transversal.

$$\therefore$$
 m ( $\angle$  AYX) = m ( $\angle$  C) = 45° (corresponding angles)

(The req.)

(Try to solve the example by another method.)

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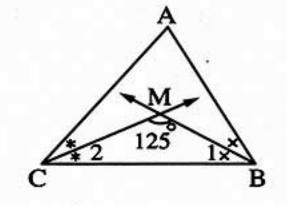


In the opposite figure:

BM bisects ∠ ABC, CM bisects ∠ ACB

and m ( $\angle$  BMC) = 125°

Find:  $m (\angle A)$ 



# Solution

**Proof** 

 $\overrightarrow{BM}$  bisects  $\angle$  ABC  $\rightarrow$   $\overrightarrow{CM}$  bisects  $\angle$  ACB and m ( $\angle$  BMC) = 125° Given

R.T.F.  $m (\angle A)$ 

> : The sum of measures of the interior angles of  $\Delta$  MBC = 180° and m ( $\angle$  BMC) = 125°

 $m (\angle 1) + m (\angle 2) = 180^{\circ} - 125^{\circ} = 55^{\circ}$ 

But m ( $\angle$  ABC) = 2 m ( $\angle$  1) and m ( $\angle$  ACB) = 2 m ( $\angle$  2)

 $\therefore$  m ( $\angle$  ABC) + m ( $\angle$  ACB) = 2 × 55° = 110°

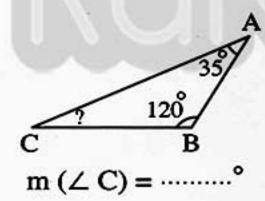
: The sum of measures of the interior angles of  $\triangle$  ABC = 180°

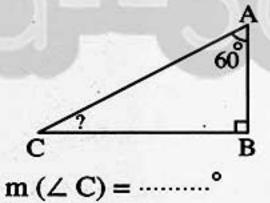
 $m (\angle A) = 180^{\circ} - 110^{\circ} = 70^{\circ}$ 

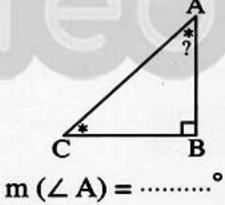
(The req.)

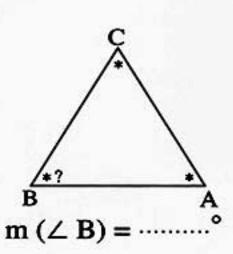
# Try by yourself

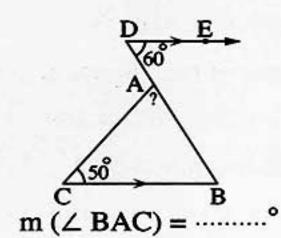
In each of the following figures , find the measure of the angle marked by (?):

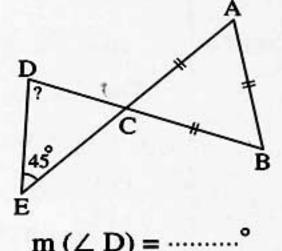












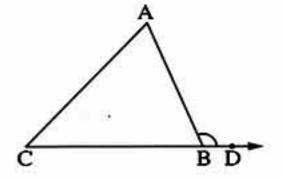
m (∠ D) = ······

Lesson Five

# The exterior angle of the triangle

### In the opposite figure:

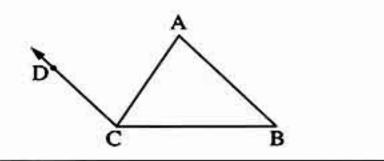
If ABC is a triangle,  $D \in \overline{CB}$  and  $D \notin \overline{CB}$ , then  $\angle ABD$ is called an exterior angle of  $\Delta$  ABC



### Notice that : |

# In the opposite figure:

 $\angle$  ACD is not an exterior angle of  $\triangle$  ABC because D∉BC



# The measure of the exterior angle of a triangle : \_

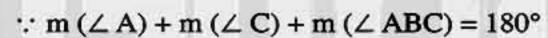
The measure of the exterior angle of a triangle is equal to the sum of the measures of its non adjacent interior angles.

### In the opposite figure:

If ABC is a triangle,  $D \in \overline{CB}$  and  $D \notin \overline{CB}$ ,

then m ( $\angle$  ABD) = m ( $\angle$  A) + m ( $\angle$  C)

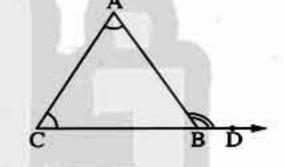
We can prove that as follows:



 $m (\angle ABD) + m (\angle ABC) = 180^{\circ}$ 

 $\therefore m (\angle ABD) + m (\angle ABC) = m (\angle A) + m (\angle C) + m (\angle ABC)$ 

 $\therefore m (\angle ABD) = m (\angle A) + m (\angle C)$ 



### (Q.E.D.)

# Notice that:

The measure of the exterior angle of a triangle is greater than the measure of any interior angle of the triangle except its adjacent angle.

*i.e.* In the previous figure:  $m (\angle ABD) > m (\angle A)$  and  $m (\angle ABD) > m (\angle C)$ 



# In the opposite figure:

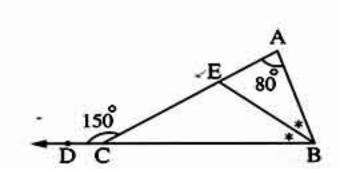
ABC is a triangle  $D \in BC$  and  $E \in AC$ 

where  $\overrightarrow{BE}$  bisects  $\angle ABC$ , m ( $\angle A$ ) = 80° and

 $m (\angle ACD) = 150^{\circ}$ 

Find:  $1 \text{ m} (\angle ABC)$ 

2 m (∠ BEC)



Unit 3

### Solution

Given

BE bisects  $\angle$  ABC  $\Rightarrow$  m ( $\angle$  A) = 80° and m ( $\angle$  ACD) = 150°

R.T.F.

1 m (∠ ABC)

2 m (∠ BEC)

**Proof** 

 $\therefore$   $\angle$  ACD is an exterior angle of  $\triangle$  ABC

 $\therefore$  m ( $\angle$  ACD) = m ( $\angle$  A) + m ( $\angle$  ABC)

 $\therefore 150^{\circ} = 80^{\circ} + m (\angle ABC)$ 

∴ m ( $\angle$  ABC) = 150° - 80° = 70°

(First req.)

∴ BE bisects ∠ ABC (given)

 $\therefore m (\angle ABE) = \frac{1}{2} m (\angle ABC) = \frac{70^{\circ}}{2} = 35^{\circ}$ 

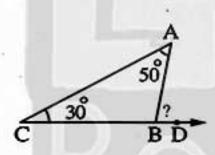
 $\therefore$   $\angle$  BEC is an exterior angle of  $\triangle$  ABE

:.  $m (\angle BEC) = m (\angle A) + m (\angle ABE) = 80^{\circ} + 35^{\circ} = 115^{\circ}$ (Second req.)

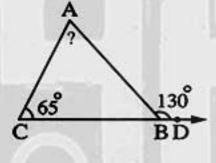
(Try to solve this example by another method.)

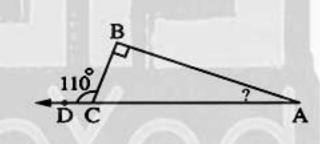
# Try by yourself

In each of the following figures, find the measure of each angle marked by (?)

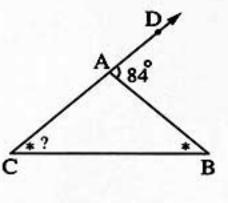


 $m (\angle ABD) = \cdots m (\angle A) = \cdots m$ 

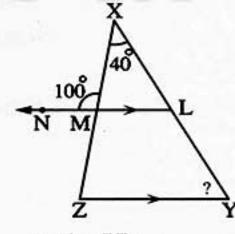




m (∠ A) = ······°



m (∠ C) = ······°



m (∠ Y) = ······°

### Remark (1)

If two angles of one triangle equal two angles of another triangle in measure, then the third angle of the first triangle is equal in measure to the third angle of the other triangle.

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

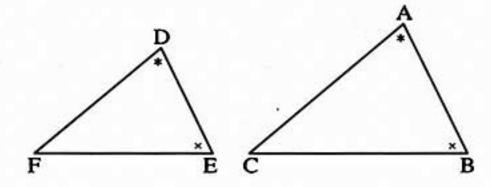
Lesson Five

In  $\Delta\Delta$  ABC and DEF,

if 
$$m (\angle A) = m (\angle D)$$
 and  $m (\angle B) = m (\angle E)$ ,

then m ( $\angle$  C) = m ( $\angle$  F)

"You can check the truth of the previous by measuring"



# Example (4)

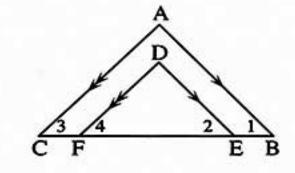
### In the opposite figure:

ABC and DEF are two triangles,

 $E \in \overline{BC}$ ,  $F \in \overline{BC}$ ,  $\overline{DE} // \overline{AB}$  and

DF // AC

**Prove that:**  $m (\angle A) = m (\angle D)$ 



### Solution

DE // AB and DF // AC Given

R.T.P.  $m (\angle A) = m (\angle D)$ 

: DE // AB and BC is a transversal to them. **Proof** 

 $\therefore$  m ( $\angle$  1) = m ( $\angle$  2) (corresponding angles)

.. DF // AC and BC is a transversal to them.

 $m (\angle 3) = m (\angle 4)$  (corresponding angles)

In  $\Delta \Delta$  ABC and DEF:

 $m (\angle 1) = m (\angle 2)$  and  $m (\angle 3) = m (\angle 4)$ 

 $\therefore$  m ( $\angle$  A) = m ( $\angle$  D) (Q.E.D.)

## Remark (2)

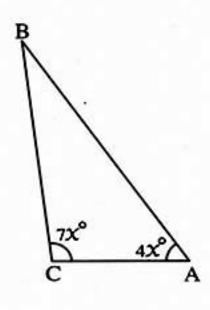
- If the sum of measures of two angles in a triangle equals 90°, then the third angle is right.
- If the sum of measures of two angles in a triangle is less than 90°, then the third angle is obtuse.
- If the sum of measures of two angles in a triangle is more than 90°, then the third angle is acute.

# Example (5)

### In the opposite figure:

ABC is a triangle in which m ( $\angle A$ ) = 2 m ( $\angle B$ ) = 4  $\mathcal{X}^{\circ}$  and  $m (\angle C) = 7 X^{\circ}$ 

**Prove that:**  $\angle$  C is an obtuse angle.



## Solution

Given 
$$| m(\angle A) = 2 m(\angle B) = 4 \mathcal{X}^{\circ}$$
 and  $m(\angle C) = 7 \mathcal{X}^{\circ}$ 

R.T.P. ∠ C is an obtuse angle.

$$\therefore m (\angle A) + m (\angle B) = 4 \mathcal{X}^{\circ} + 2 \mathcal{X}^{\circ} = 6 \mathcal{X}^{\circ}$$

$$:: m (\angle C) = 7 X^{\circ} :: m (\angle A) + m (\angle B) < m (\angle C)$$

∴ ∠ C is an obtuse angle.

(Q.E.D.)

### Remark (3)

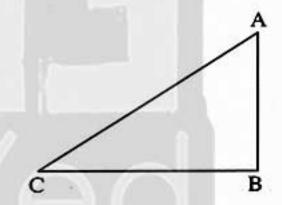
If the measure of an angle in a triangle equals the sum of measures of the other two angles, then the triangle is right-angled.

### In the opposite figure:

If ABC is a triangle in which:  $m (\angle A) + m (\angle C) = m (\angle B)$ 

, then m (∠ B) = 
$$\frac{180^{\circ}}{2}$$
 = 90°

i.e.  $\triangle$  ABC is right-angled at B



ABC is a triangle in which  $m (\angle A) : m (\angle B) : m (\angle C) = 2 : 3 : 5$ 

Prove without finding the measures of the angles of the triangle that the triangle is right-angled, then mention the right angle.

### Solution

Given ABC is a triangle in which  $m(\angle A) : m(\angle B) : m(\angle C) = 2 : 3 : 5$ 

R.T.P.  $\triangle$  ABC is right-angled and mention the right angle.

Proof  $m (\angle A) + m (\angle B)$  is equivalent to 5 parts and  $m (\angle C)$ is equivalent to 5 parts

$$\therefore m (\angle A) + m (\angle B) = m (\angle C)$$

∴ ∆ ABC is right-angled at C (Q.E.D.)

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

Lesson Six



# Follow : The triangle

### Theorem (2):

The ray drawn from the midpoint of a side of a triangle parallel to another side bisects the third side.

Given

D is the midpoint of AB, DE // BC

R.T.P.

E is the midpoint of AC

Construction

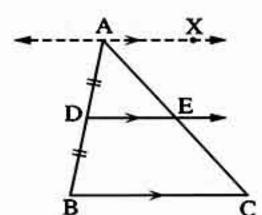
Draw AX // BC ·· AX // DE // BC

Proof

- , AB and AC are two transversals to them at D and E respectively.
- , :: AD = DB

 $\therefore AE = EC$ 

.. E is the midpoint of AC



(Q.E.D.)

# Example (1

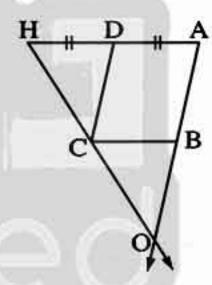
In the opposite figure:

ABCD is a parallelogram  $H \in \overline{AD}$  such that AD = DH,

 $\overrightarrow{HC} \cap \overrightarrow{AB} = \{0\}$ 

Prove that: I HC = CO

2 AB = BO



# Solution

ABCD is a parallelogram, AD = DH and  $HC \cap AB = \{0\}$ Given

R.T.P.

II HC = CO

In A HAO:

2 AB = BO

Proof

: D is the midpoint of HA (Given),

DC // AO (Definition of the parallelogram)

.. C is the midpoint of HO

i.e. HC = CO (Theorem)

(Q.E.D. 1)

: C is the midpoint of OH (Proved)

, CB // HA (Definition of the parallelogram)

.. B is the midpoint of AO

i.e. AB = BO (Theorem)

(Q.E.D. 2)

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى في المعلومين العمل العمامين المعاميرين المعاميرين العماميرين المعاميرين ا

### Corollary

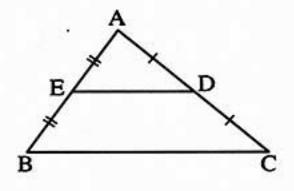
The line segment joining the midpoints of two sides of a triangle is parallel to the third side.

### In the opposite figure:

If ABC is a triangle in which D

is the midpoint of AC,

E is the midpoint of  $\overline{AB}$ , then :  $\overline{ED} // \overline{BC}$ 



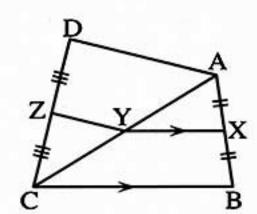
# Example (2)

# In the opposite figure:

X is the midpoint of AB,

XY // BC and Z is the midpoint of DC

Prove that :  $\overline{YZ} // \overline{AD}$ 



# Solution

X is the midpoint of AB, Z is the midpoint of CD and XY // BC Given

R.T.P.

YZ // AD

In A ABC:

∴ YZ // AD

Proof

 $:: AX = XB , \overline{XY} // \overline{BC}$ 

 $\therefore AY = YC$ (Theorem)

In  $\triangle$  ACD:  $\therefore$  AY = YC

(Corollary)

(Proved)

DZ = ZC

(Given)

(Q.E.D.)

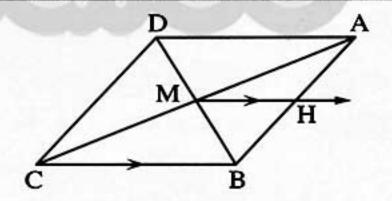
# Try by yourself.

### In the opposite figure:

ABCD is a parallelogram and M is the point of intersection of its two diagonals.

Draw MH // BC to cut AB at H

Complete the solution to prove that AH = HB



Given

R.T.P.

Proof

: ABCD is a parallelogram

.. M is the midpoint of .....

In A ABC:

: M is the midpoint of ..... and ..... // .....

····· (Theorem)

(Q.E.D.)

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هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى

# Theorem (3):

The length of the line segment joining the midpoints of two sides of a triangle is equal to half the length of the third side.

Given

ABC is a triangle, D is the midpoint of AB, H is the midpoint of AC

R.T.P.

 $DH = \frac{1}{2}BC$ 

Construction

Draw HO // AB to cut BC at O

**Proof** 

- : D is the midpoint of AB, H is the midpoint of AC
- :. DH // BC (Corollary)
- , : HO // AB (Construction), H is the midpoint of AC
- .. O is the midpoint of BC
- $\therefore$  BO =  $\frac{1}{2}$  BC
- , : The figure DHOB is a parallelogram.

$$\therefore DH = BO = \frac{1}{2} BC$$

(Q.E.D.)

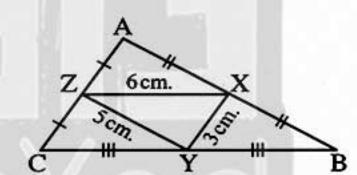


### In the opposite figure:

ABC is a triangle in which X , Y and Z are the midpoints of AB, BC and CA respectively.

If XY = 3 cm., YZ = 5 cm. and ZX = 6 cm.,

then find the perimeter of  $\triangle$  ABC



# Solution

Given

ABC is a triangle in which X , Y and Z are the midpoints of AB ,

BC and CA respectively, XY = 3 cm., YZ = 5 cm. and ZX = 6 cm.

R.T.F.

The perimeter of  $\triangle$  ABC

Proof

In  $\triangle$  ABC:

- : X is the midpoint of AB and Z is the midpoint of AC
- $\therefore$  XZ =  $\frac{1}{2}$  BC (Theorem)
- $\therefore$  BC = 6 × 2 = 12 cm.

Similarly : X is the midpoint of AB and Y is the midpoint of BC

 $\therefore XY = \frac{1}{2}AC$ 

 $\therefore$  AC = 3 × 2 = 6 cm.

Similarly : Y is the midpoint of BC and Z is the midpoint of AC

 $\therefore$  YZ =  $\frac{1}{2}$  AB

 $\therefore$  AB = 5 × 2 = 10 cm.

 $\therefore$  The perimeter of  $\triangle$  ABC = AB + BC + CA = 10 + 12 + 6 = 28 cm.

(The req.)

# Example (4)

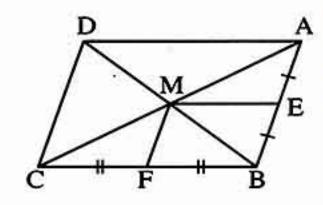
### In the opposite figure:

ABCD is a parallelogram in which:

 $\overline{AC} \cap \overline{BD} = \{M\}$ , E is the midpoint of  $\overline{AB}$ 

F is the midpoint of BC

**Prove that:** The figure EBFM is a parallelogram.



### Solution

Proof

Given ABCD is a parallelogram, E is the midpoint of AB

, F is the midpoint of BC

R.T.P. The figure EBFM is a parallelogram.

: ABCD is a parallelogram whose diagonals intersect at M

.. M is the midpoint of each of AC and BD

∴ In ∆ ABC:

: E is the midpoint of AB, M is the midpoint of AC

∴ EM // BC

∴ EM // BF

 $, EM = \frac{1}{2} BC \text{ (Theorem)}$ 

 $\therefore EM = BF$ 

.. The figure EBFM is a parallelogram.

(Q.E.D.)

# fry by yours

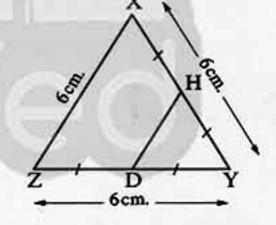
### In the opposite figure:

XYZ is an equilateral triangle whose side is of length 6 cm. ,

D is the midpoint of YZ and H is the midpoint of XY

Complete the following solution to prove that:

Δ HYD is an equilateral triangle and find its perimeter.



Given

R.T.P.

Proof

 $\therefore$  D is the midpoint of  $\cdots$   $\therefore$  YD =  $\cdots$  cm. (1)

: H is the midpoint of ..... : YH = ..... cm. (2)

In A XYZ:

: D is the midpoint of ...... and H is the midpoint of ......

 $\therefore$  DH =  $\frac{1}{2}$  ..... cm. (3)

From (1), (2) and (3):

 $\therefore$   $\triangle$  HYD is ..... and its perimeter = ..... cm. (The req.)

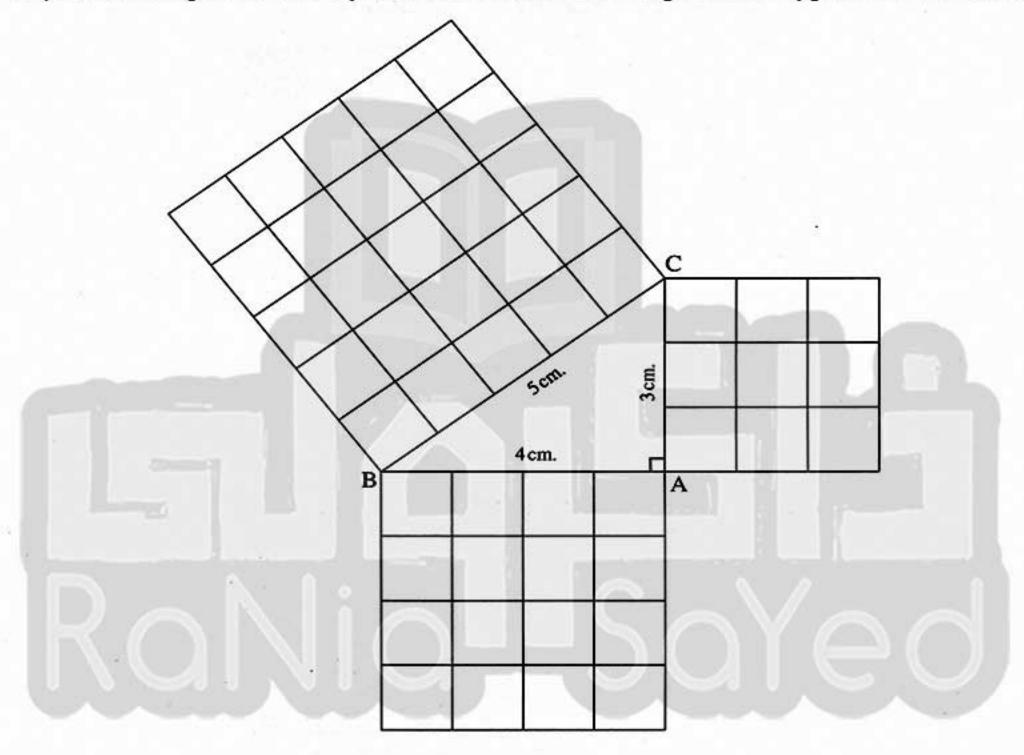
Lesson Seven



# Pythagoras' theorem

### Prelude drill:

 Draw the right-angled triangle ABC at A in which AB = 4 cm., AC = 3 cm. If your drawing is accurate, you will find that: The length of the hypotenuse BC is 5 cm.



 Draw a square on each side of the triangle as in the opposite figure From the opposite figure, we find that: The area of the square drawn on  $\overline{AB} = (AB)^2 = 16 \text{ cm}^2$ .

The area of the square drawn on  $\overline{AC} = (AC)^2 = 9 \text{ cm}^2$ 

The area of the square drawn on  $\overline{BC} = (BC)^2 = 25 \text{ cm}^2$ .

The area of the square drawn on BC is i.e.: equal to the sum of the areas of the two squares drawn on AB and AC

In other words : \_  $(BC)^2 = (AB)^2 + (AC)^2$ 

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى العمف الاول الاعدادي مصطح الكري العمد العمد

The verbal formula of this relation is defined by Pythagoras' theorem.

### Pythagoras' theorem:

The sum of areas of the squares on the sides of the right angle of a right-angled triangle is the same as the area of the square on the hypotenuse.



Pythagoras (582-501 B.C.)

We can also write the previous theorem as follows : • ......

In a right-angled triangle, the square of the length of the hypotenuse is equal to the sum of the squares of the lengths of the other two sides. i.e.

If ABC is a right-angled triangle at A, then:

$$(BC)^2 = (AB)^2 + (AC)^2$$

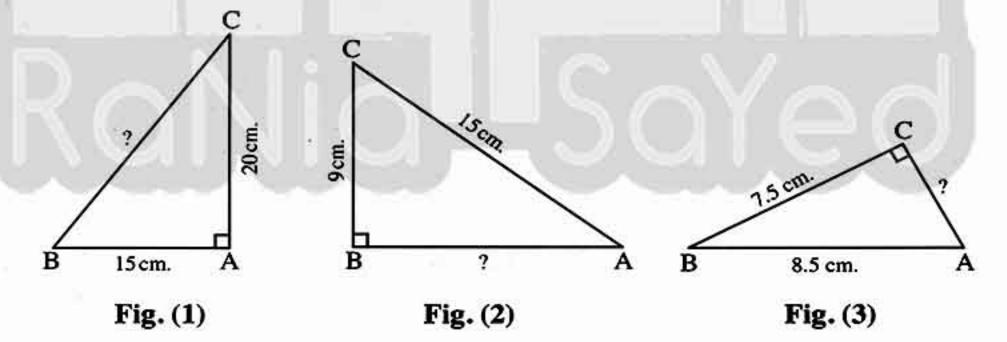
From the previous relation, we can deduce the following two relations:

$$(AB)^2 = (BC)^2 - (AC)^2$$

$$(AC)^2 = (BC)^2 - (AB)^2$$

# Example (1

In each of the following figures, find the side length which is denoted by sign (?):



# Solution

In fig. (1):

- .: Δ ABC is right-angled at A
- $\therefore (BC)^2 = (AB)^2 + (AC)^2 = (15)^2 + (20)^2 = 225 + 400 = 625$
- ∴ BC =  $\sqrt{625}$  = 25 cm.

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

Lesson Seven

### In fig. (2):

- ∴ ∆ ABC is right-angled at B
- :  $(AB)^2 = (AC)^2 (BC)^2 = (15)^2 (9)^2 = 225 81 = 144$
- ∴ AB =  $\sqrt{144}$  = 12 cm.

### In fig. (3):

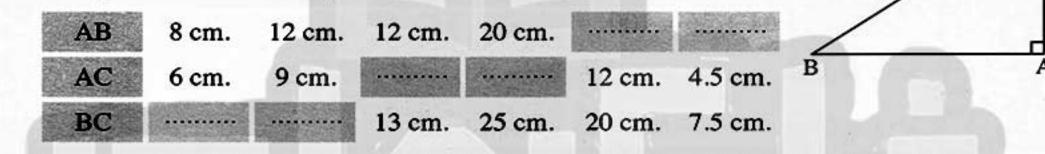
- .: Δ ABC is right-angled at C
- $\therefore (AC)^2 = (AB)^2 (BC)^2 = (8.5)^2 (7.5)^2 = 72.25 56.25 = 16$
- $\therefore AC = \sqrt{16} = 4 \text{ cm}.$

### Try by yourself

### In the opposite figure:

Δ ABC is right-angled at A

### Complete the following table:

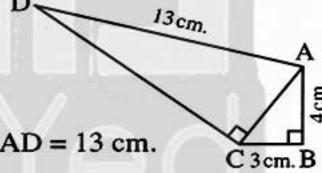


### In the opposite figure:

ABCD is a quadrilateral in which:

 $m (\angle B) = m (\angle ACD) = 90^{\circ}$ , AB = 4 cm., BC = 3 cm. and AD = 13 cm.

Find: The length of each of AC and CD



### Solution

Given

 $m (\angle B) = m (\angle ACD) = 90^{\circ}$ , AB = 4 cm., BC = 3 cm. and AD = 13 cm.

R.T.F.

The length of each of AC and CD

Proof

- ∴ ∆ ABC is a right-angled triangle at B
- $\therefore$  (AC)<sup>2</sup> = (AB)<sup>2</sup> + (BC)<sup>2</sup> (Pythagoras' theorem)
- $\therefore$  (AC)<sup>2</sup> = (4)<sup>2</sup> + (3)<sup>2</sup> = 16 + 9 = 25
- $\therefore$  AC =  $\sqrt{25}$  = 5 cm.

(First req.)

- .: Δ ACD is a right-angled triangle at C
- $\therefore (CD)^2 = (AD)^2 (AC)^2$
- $\therefore$  (CD)<sup>2</sup> =  $(13)^2 (5)^2 = 169 25 = 144$  (Pythagoras' theorem)
- $\therefore$  CD =  $\sqrt{144}$  = 12 cm. (Second req.)

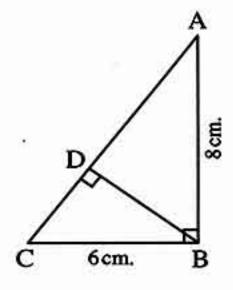


### In the opposite figure:

ABC is a right-angled triangle at B,  $D \in \overline{AC}$ 

such that  $\overline{BD} \perp \overline{AC}$ , AB = 8 cm. and CB = 6 cm.

Find: The length of BD



### Solution

 $\triangle$  ABC is right-angled at B,  $\overline{BD} \perp \overline{AC}$ Given

AB = 8 cm. and CB = 6 cm.

R.T.F. The length of BD

: A ABC is right-angled at B Proof

:  $(AC)^2 = (AB)^2 + (BC)^2$ 

(Pythagoras' theorem)

 $\therefore (AC)^2 = 64 + 36 = 100$ 

:. AC =  $\sqrt{100}$  = 10 cm.

• The area of  $\triangle$  ABC =  $\frac{1}{2}$  BC  $\times$  AB =  $\frac{1}{2}$   $\times$  6  $\times$  8 = 24 cm<sup>2</sup>.

• : The area of  $\triangle$  ABC =  $\frac{1}{2}$  AC × BD

 $\therefore 24 = \frac{1}{2} \times 10 \times BD$ 

 $\therefore 24 = 5 BD$ 

:. BD =  $\frac{24}{5}$  = 4.8 cm.

(The req.)

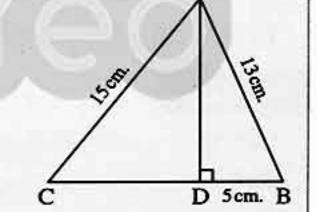
# Try by yourse

# In the opposite figure:

ABC is a triangle in which AB = 13 cm.

AC = 15 cm.,  $D \in \overline{BC}$  such that

 $\overline{AD} \perp \overline{BC}$  and BD = 5 cm.



## Complete the following proof to find the length of DC

.: Δ ABD is right-angled at D

:. 
$$(AD)^2 = (AB)^2 - (\cdots)^2 = (\cdots)^2 - (\cdots)^2 = \cdots$$

 $\therefore$  AD =  $\sqrt{\cdots}$  =  $\cdots$  cm.

, ∵ ∆ ADC is right-angled at D

: 
$$(DC)^2 = (\cdots)^2 - (AD)^2 = (\cdots)^2 - (\cdots)^2 = \cdots$$

$$\therefore$$
 DC =  $\sqrt{\cdots}$  =  $\cdots$  cm.

(The req.)

Lesson Seven

# Can you prove Pethagoras' theorem theoretically?

- We can prove Pethagoras' theorem which has been explained theoretically as follows:

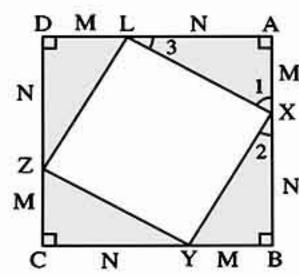
### In the opposite figure:

If ABCD is a square and the points

X, Y, Z and L divide its sides AB, BC

CD and DA respectively into two parts,

one part is M length unit and the other is N length unit



In 
$$\triangle \triangle AXL$$
 and BYX: 
$$\begin{cases} AL = BX = N \text{ length unit} & C & N \\ AX = BY = M \text{ length unit} \\ m (\angle A) = m (\angle B) = 90^{\circ} \text{ (properties of the square)} \end{cases}$$

i.e.  $\triangle AXL \equiv \triangle BYX$  (two sides and the included angle)

Similarly we can prove that:

$$\Delta BYX \equiv \Delta CZY$$
,  $\Delta CZY \equiv \Delta DLZ$ ,  $\Delta DLZ \equiv \Delta AXL$ 

i.e. 
$$\triangle AXL \equiv \triangle BYX \equiv \triangle CZY \equiv \triangle DLZ$$

, then we deduce that : XY = YZ = ZL = LX

i.e. The figure XYZL is a rhombous

$$\mathbf{m} (\angle 1) + \mathbf{m} (\angle 3) = 90^{\circ}$$

$$m (\angle 2) = m (\angle 3)$$

(from congruence)

$$\therefore m (\angle 1) + m (\angle 2) = 90^{\circ} \quad \therefore m (\angle LXY) = 90^{\circ}$$

$$\therefore$$
 m ( $\angle$  LXY) = 90°

.. The figure XYZL is a square

, then the area of the squure XYZL

= The area of the square ABCD – 4 the area of  $\triangle$  AXL

$$\therefore (XY)^2 = (M+N)^2 - 4 \times \frac{1}{2} \times MN$$

$$(XY)^2 = M^2 + 2 MN + N^2 - 2 MN$$

$$\therefore (XY)^2 = M^2 + N^2$$

$$(XY)^2 = M^2 + N^2$$
  $(XY)^2 = (BY)^2 + (BX)^2$ 

i.e. In  $\triangle$  XBY which is right-angled at B:

The square of the length of the hypotenuse = The sum of the squares of the lengths of the other two sides.

Unit 3

### Enrichment information (for reading only)

You can get three numbers representing the lengths of sides of a right-angled triangle as follows:

If M is an even number bigger than 2, then the numbers  $M_1 \left(\frac{M}{2}\right)^2 - 1_2 \left(\frac{M}{2}\right)^2 + 1_2$  represent three lengths of sides of a right-angled triangle as shown in the following table:

M	$\left(\frac{M}{2}\right)^2 - 1$	$\left(\frac{M}{2}\right)^2 + 1$
4	$\frac{16}{4} - 1 = 3$	$\frac{16}{4} + 1 = 5$
6	$\frac{36}{4} - 1 = 8$	$\frac{36}{4} + 1 = 10$
8	$\frac{64}{4} - 1 = 15$	$\frac{64}{4} + 1 = 17$

If M is an odd number bigger than 2, then the numbers M,  $\frac{M^2-1}{2}$ ,  $\frac{M^2+1}{2}$  represent three lengths of sides of a right-angled triangle as shown in the following table:

M	$\frac{M^2-1}{2}$	$\frac{M^2+1}{2}$		
5	$\frac{25-1}{2}=12$	$\frac{25+1}{2}=13$		
7	$\frac{49-1}{2} = 24$	$\frac{49+1}{2} = 25$		
9	$\frac{81-1}{2} = 40$	$\frac{81+1}{2} = 41$		

# Enrichment Activity

You can prove Pethagoras' theorem by using computer through the Paint programme as shown in the computer activities at the end of that book.

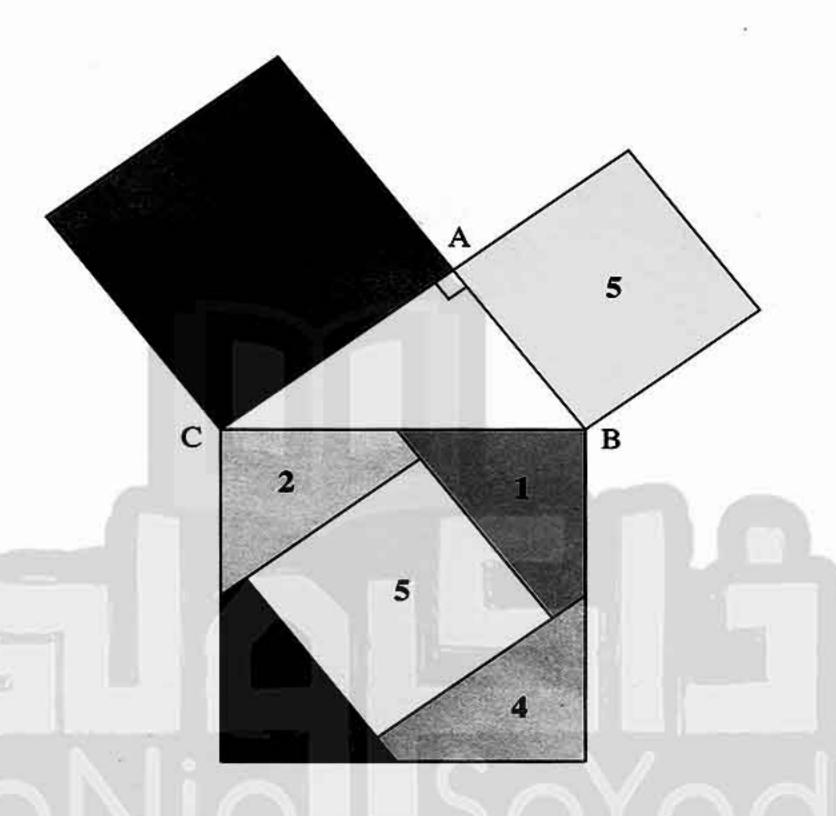
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Enrichment Activity (2)

# A practical activity to prove Pethagoras' theorem





- Cut the square drawn on AB and the square drawn on AC
- Cut the numbered areas by numbers 10, 29, 30 and 40
- Try to stick the areas you cut on the areas with their corresponding numbers on the square drawn on the chord  $\overline{BC}$
- If you are accurate in your work, you will find that they are completely congruent, so we prove Pethagoras' theorem practically which says:

The area of the square drawn on the hypotenuse  $\overline{BC}$  is equal to the sum of areas of the two squares drawn on the sides of the right angle  $\overline{AB}$  and  $\overline{AC}$ 



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Lesson Eight



# Lesson

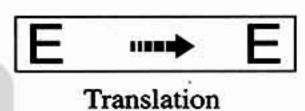
# Geometric transformations

Bassim and Ayman play with a set of plastic letters. In each time, they notice the change which occurs to a certain letter as ( ) if they:

Reflect its position.

Reflection

2 Move it straight a certain distance.



3 Rotate it with a certain angle.



Rotation anticlockwise

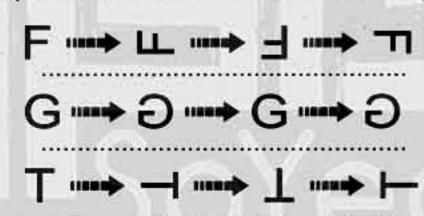
Rotation clockwise

## Try by yourself

By noticing the change that occurs to every letter compared with the figure preceding it, write down each figure the suitable word (reflection, translation, rotation):

$$B \longrightarrow B \longrightarrow B \longrightarrow B$$

$$P \longrightarrow Q \longrightarrow Q \longrightarrow Q$$



In each of the following figures, notice the image of  $\triangle$  ABC and deduce what happened to it:

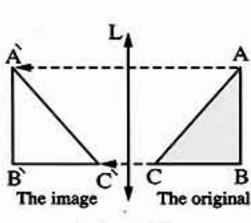


Fig. (1)

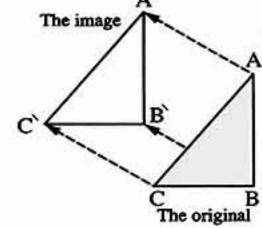


Fig. (2)

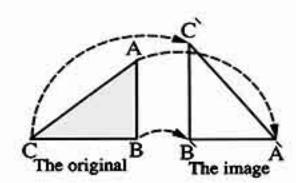


Fig. (3)

- Fig. (1): Δ ABC has been reflected.
- Fig. (2) : ∆ ABC has been translated.
- Fig. (3): Δ ABC has been rotated.

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Unit 3

### In each of the previous figures, notice that:

- The point A has been transferred to  $\hat{A}$  i.e.  $A \longrightarrow \hat{A}$
- The point B has been transferred to  $\hat{B}$  i.e. B  $\longrightarrow$   $\hat{B}$
- The point C has been transferred to C i.e. C → C

Thus , all the points of  $\Delta$  ABC have been transferred to another position , then we say that  $\Delta$  ABC has been transformed from position to another position.

### From the previous, we deduce that:

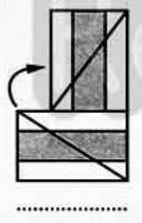
If all the points of a geometrical figure have moved according to a certain system, then we will obtain an image in a new position to the same figure, then we say that this figure has been under the effect of a geometric transformation.

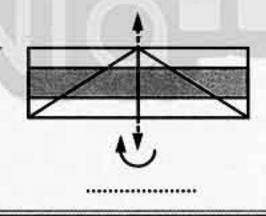
i.e. The geometric transformation maps each point P in the plane onto an image point P in the same plane.

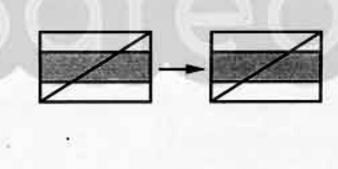
Geometric transformations are many types as reflection, translation and rotation which we will study each of them in detail in the following lessons.

# Try by yourself

Describe the type of the geometric transformation (reflection , translation or rotation) in each of the following figures :







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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق



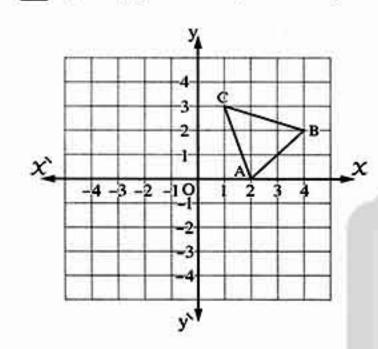


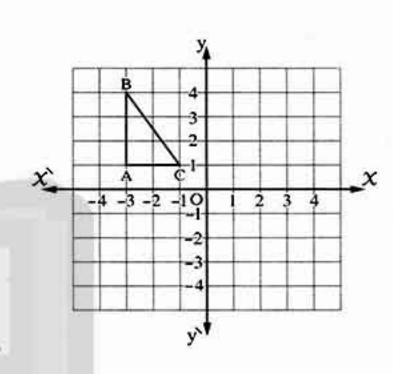
الصف الاول الاعدادي

Lesson Eight

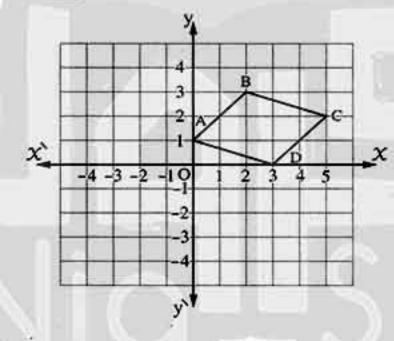
# Example (1)

Draw the image of each of the following figures according to the illustrated geometric transformation, then describe its type:





$$3(x,y) \longrightarrow (x,-y)$$



# Solution

$$1 (x,y) \longrightarrow (x-4,y+1)$$

i.e. x transferred to x-4 and

y transferred to y + 1, therefore we get:

$$A(2,0) \longrightarrow \hat{A}(2-4,0+1)$$

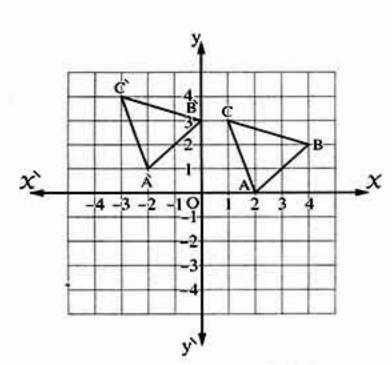
$$B(4,2) \longrightarrow \vec{B}(4-4,2+1)$$

i.e. B (0,3)

$$C(1,3) \longrightarrow \hat{C}(1-4,3+1)$$

i.e. C (-3,4)





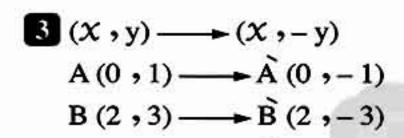
 $(x,y) \longrightarrow (-x,-y)$ i.e.

$$A(-3,1) \longrightarrow \hat{A}(3,-1)$$
 [Note: -(-3) = 3]

$$B(-3,4) \longrightarrow B(3,-4)$$

$$C(-1,1) \longrightarrow \hat{C}(1,-1)$$

From the graph, it is shown that  $\triangle$  ABC has been rotated to become  $\triangle$  ABC

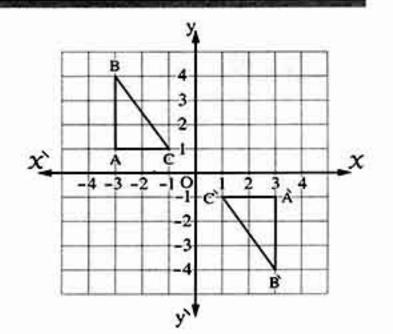


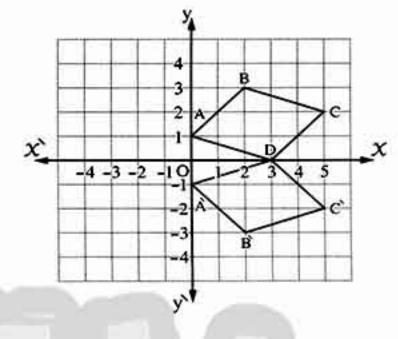
$$C(5,2) \longrightarrow \hat{C}(5,-2)$$

$$D(3,0) \longrightarrow D(3,0)$$

From the graph, it is shown that the shape

ABCD has been reflected to become ABCD





Draw the image of the quadrilateral ABCD where A (1,1), B (4,1), C (4,3)

, D (1,5) according to each of the following transformations, then describe its type:

# Solution

$$1 (x,y) \longrightarrow (-x,y)$$
i.e.

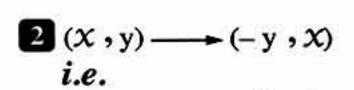
$$A(1,1) \longrightarrow \hat{A}(-1,1)$$

$$B(4,1) \longrightarrow B(-4,1)$$

$$C(4,3) \longrightarrow \hat{C}(-4,3)$$

$$D(1,5) \longrightarrow \hat{D}(-1,5)$$

The transformation is reflection



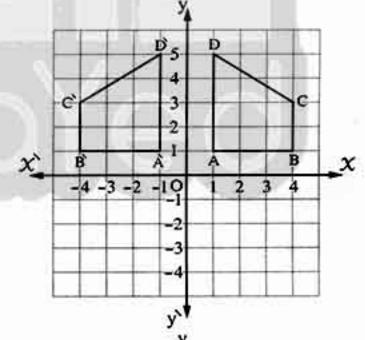
$$A(1,1) \longrightarrow A(-1,1)$$

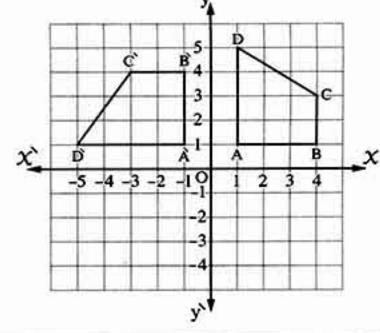
$$B(4,1) \longrightarrow \overrightarrow{B}(-1,4)$$

$$C(4,3) \longrightarrow \hat{C}(-3,4)$$

$$D(1,5) \longrightarrow \hat{D}(-5,1)$$

The transformation is rotation.





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Lesson Eight

$$3(x,y) \longrightarrow (x,y-5)$$

i.e.

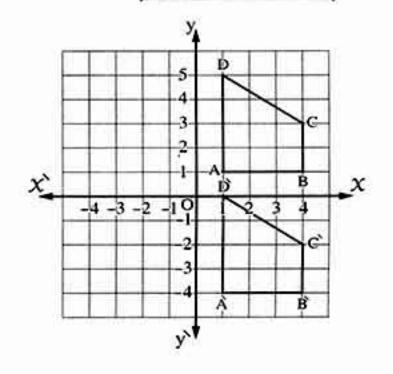
$$A(1,1) \longrightarrow \hat{A}(1,-4)$$

$$B(4,1) \longrightarrow B(4,-4)$$

$$C(4,3) \longrightarrow \hat{C}(4,-2)$$

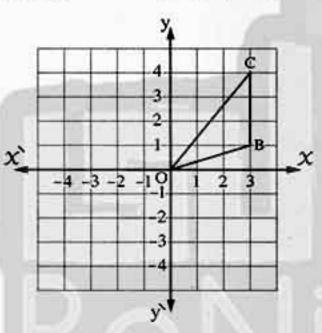
$$D(1,5) \longrightarrow \vec{D}(1,0)$$

The transformation is translation.

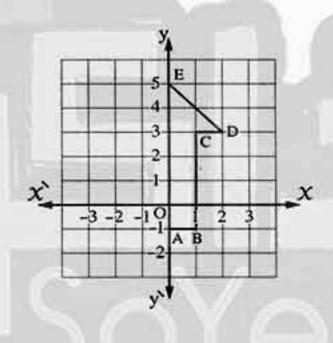


Map each of the following shapes due to the geometric transformation above it , then describe its type:

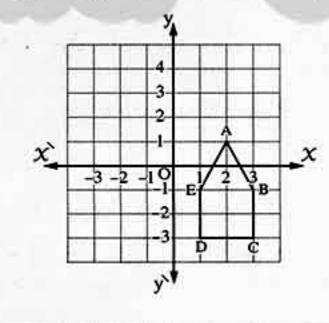
 $(x,y) \longrightarrow (-x,-y)$ 



 $2(x,y) \longrightarrow (-x,y)$ 



 $3(x,y) \longrightarrow (x,y+2)$ 





# Reflection (Reflection in a straight line)

#### Prelude

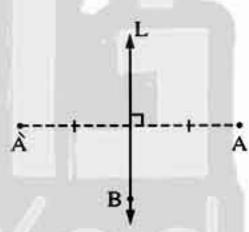
If you stand in front of a plane mirror, then you will see your picture (image) reflected in the mirror in the same size and details and you will notice also that the distance between the image and the mirror equals the real distance between you and the mirror. If you approach the mirror, then you will find that your image approaches also the mirror.



#### Reflection in a straight line

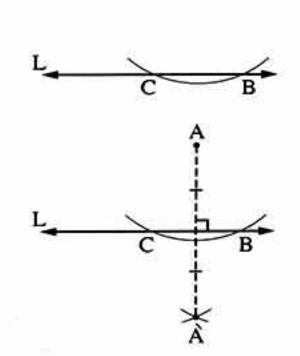
Reflection in the straight line L maps each point A to the point A in the same plane such that :

- If A∉L, then the straight line L is the perpendicular bisector to the line segment AA
- 2 If B∈L, then B is reflected onto itself i.e. B coincides B



# Finding the image of a point by reflection in a given straight line

- To find  $\hat{\mathbf{A}}$  which is the image of  $\mathbf{A}$  by reflection in the straight line  $\mathbf{L}$  , we do as follows :
  - Draw an arc of a circle with centre A to cut L at B and C
  - With the same radius length taking B and C as centres, draw two arcs in the other side of the straight line L to intersect at A, then A is the image of A by reflection in L



#### Check by measuring that:

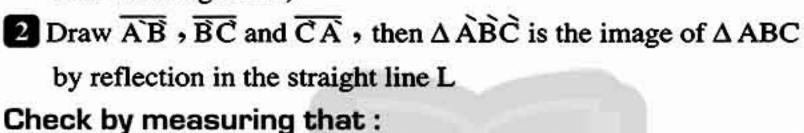
 $\overline{AA} \perp L$  and L bisects  $\overline{AA}$ 

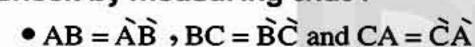
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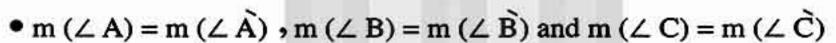
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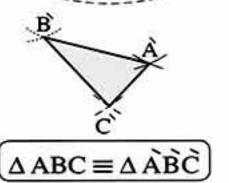
# Finding the image of a polygon by reflection in a given straight line

- To find the image of a polygon as  $\triangle$  ABC by reflection in the straight line L , we do as follows :
  - Find the image of each vertex of Δ ABC by reflection in the straight line L as we did before (A is the image of A, B is the image of B and C is the image of C)









## From the previous, we deduce that:

Reflection is a geometrical transformation which transforms the geometrical shape into another one congruent to it (equal to it in its side lengths and angle measures), but the direction of reading the shape is the opposite direction of reading the image.

Notice that:

The reading of  $\triangle$  ABC is clockwise while the reading of  $\triangle$   $\stackrel{>}{A}\stackrel{>}{B}\stackrel{>}{C}$  is anticlockwise.

# Properties of reflection in a straight line

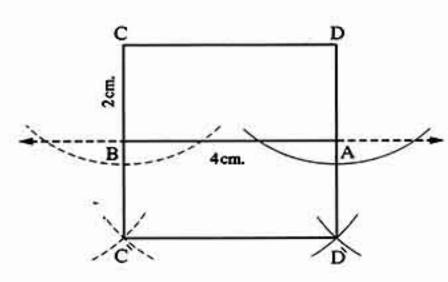
# Illustrated example

Draw the image of the rectangle ABCD in which  $\overrightarrow{AB}=4$  cm. ,  $\overrightarrow{BC}=2$  cm. by reflection in  $\overrightarrow{AB}$ 

#### Solution

First: We draw the rectangle ABCD in which AB = 4 cm. and BC = 2 cm.

Second: To find the image of the rectangle ABCD by reflection in  $\overrightarrow{AB}$  we do as follows:



11 The images of A and B by reflection in  $\overrightarrow{AB}$  are the same because they belong to  $\overrightarrow{AB}$ 

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2 We find the image of D by reflection in  $\overrightarrow{AB}$ , let it be  $\overrightarrow{D}$ , the image of C by reflection in AB let it be C, then we get the rectangle ABCD to be the image of the rectangle ABCD by reflection in AB

Notice that :

- $\mathbf{I} \quad \mathbf{AD} = \mathbf{AD} \cdot \mathbf{DC} = \mathbf{DC} \cdot \mathbf{CB} = \mathbf{CB} \text{ and } \mathbf{AB} \text{ is a common side.}$ 
  - i.e. Reflection in a straight line reserves the lengths of the line segments.
- $2 m (\angle BAD) = m (\angle BAD), m (\angle ABC) = m (\angle ABC)$ 
  - $, m (\angle C) = m (\angle \hat{C}) \text{ and } m (\angle D) = m (\angle \hat{D})$
  - i.e. Reflection in a straight line reserves the measures of angles.
- 3 From the rectangle ABCD: AD // BC , from the rectangle ABCD: AD // BC
  - .. The images of the two parallel line segments are also two parallel line segments.
  - i.e. Reflection in a straight line reserves parallelism.
- 4 The reading of the rectangle ABCD is in the clockwise direction while the reading of the rectangle ABCD is in anticlockwise direction.
  - i.e. Reflection in a straight line doesn't reserve the orientation of the vertices of the figure.
- 5 If a point lies on DC and we find its image by reflection in AB, we find its image lie on DC
  - i.e. Reflection in a straight line reserves the betweenness.

Example

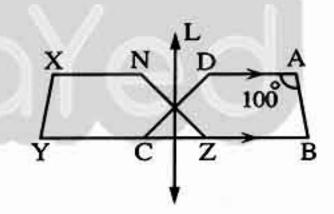
In the opposite figure:

ABCD is a quadrilateral in which  $m (\angle A) = 100^{\circ}$  and

AD // BC If the figure XYZN is the image of the figure

ABCD by reflection in the straight line L

Find:  $m (\angle Y)$ 



## Solution

- : The figure XYZN is the image of the figure ABCD by reflection in L
- .. X is the image of A by reflection in L
- $\therefore$  m ( $\angle$  X) = m ( $\angle$  A) = 100°
- (Because the reflection in the straight line reserves the measures of angles)
- $\therefore$  XN is the image of AD and YZ is the image of BC by reflection in L and  $\therefore$  AD // BC
- .. XN // YZ (Because the reflection in a straight line reserves parallelism)
- $\therefore$  m ( $\angle$  X) + m ( $\angle$  Y) = 180° (Two interior angles in the same side of the transversal)
- $m (\angle Y) = 180^{\circ} 100^{\circ} = 80^{\circ}$

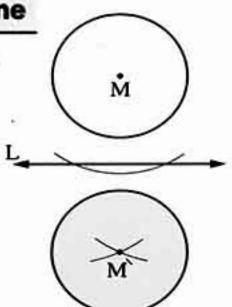
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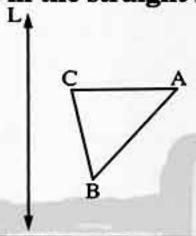
# Finding the image of a circle by reflection in a given straight line

- To find the image of a circle M by reflection in the straight line L, we do as follows:
  - I Find the image of the centre M by reflection in L as we did before, say M
  - 2 Use the compasses with radius length equal to the radius length of the circle M to draw a circle with centre M that will be the image of the circle M by reflection in L



#### Try by yourself

Draw the image of the triangle by reflection in the straight line L:



#### Optical illusion

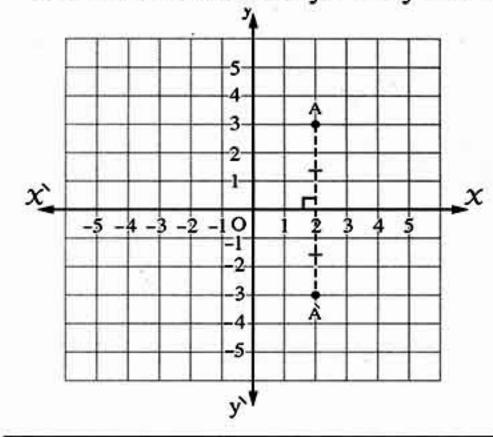
Look at the picture. What do you see?



#### Reflection in the Cartesian coordinates plane

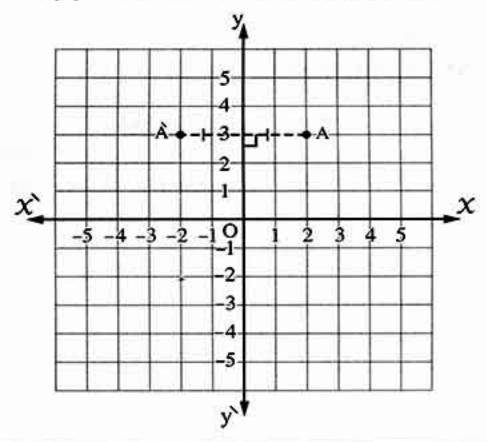
#### Reflection in the x-axis

• If A (2, 3) is a point in the Cartesian coordinate plane and the required is finding its image by reflection in XX (the X-axis), then draw  $\overline{AA}$  such that  $\overrightarrow{x} \stackrel{\checkmark}{\cancel{x}}$  is the line of symmetry of it:



#### Reflection in the y-axis

 If A (2,3) is a point in the Cartesian coordinate plane and the required is finding its image by reflection in yy (the y-axis), then draw AA such that y y is the line of symmetry of it:



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#### Then we find that:

$$A(2,3) \longrightarrow \hat{A}(2,-3)$$

*i.e.* The reflection in the x-axis changes the sign of the 2<sup>nd</sup> projection (y-coordinates)

$$A(X,y) \xrightarrow{\text{by reflection in}} \widehat{A}(X,-y)$$

#### For example:

- (2,4) (2,-4)
- $\bullet$  (-3,1)  $\longrightarrow$  (-3,-1)
- $(5, -6) \longrightarrow (5, 6)$
- $\bullet$  (-2,-1)  $\longrightarrow$  (-2,1)

#### Then we find that:

$$A(2,3) \longrightarrow \hat{A}(-2,3)$$

i.e. The reflection in the y-axis changes the sign of the 1st projection (X-coordinates)

$$A(x,y) \xrightarrow{\text{by reflection in}} \widehat{A}(-x,y)$$

#### For example:

- $\bullet$  (2,4)  $\longrightarrow$  (-2,4)
- $\bullet$  (-3,1)  $\longrightarrow$  (3,1)
- $(5, -6) \longrightarrow (-5, -6)$
- $\bullet$  (-2,-1)  $\longrightarrow$  (2,-1)

#### Remarks

II The image of the point (x, 0) by reflection in the x-axis is itself because it lies on the X-axis

For example: (5,0) by reflection in the x-axis (5,0)

2 The image of the point (0, y) by reflection in the y-axis is itself because it lies on the y-axis

For example: (0,-3) by reflection in the y-axis (0,-3)

3 The image of the point (0,0) by reflection in the X-axis or the y-axis is itself because it lies on both two axes.

## Try by yourself

## Complete the following table:

The point	(5,1)	(2,-3)	(-1,4)	(-2,-6)	(0 ,-1)	(3,0)	(0,0)
Its image by reflection in the $X$ -axis							
Its image by reflection in the y-axis							

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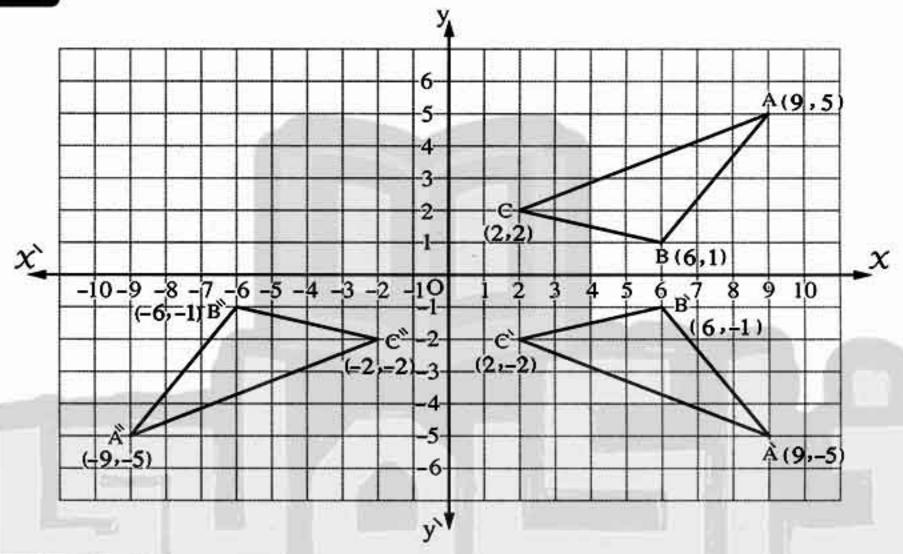
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# Example (2)

Draw on a square lattice the triangle ABC where A (9,5), B (6,1) and C (2,2):

- II Draw  $\triangle ABC$  which is the image of  $\triangle ABC$  by reflection in the X-axis
- 2 Draw  $\triangle \overrightarrow{ABC}$  which is the image of  $\triangle \overrightarrow{ABC}$  by reflection in the y-axis

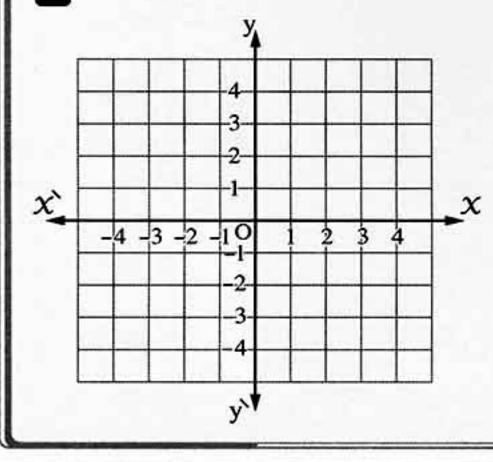
#### Solution



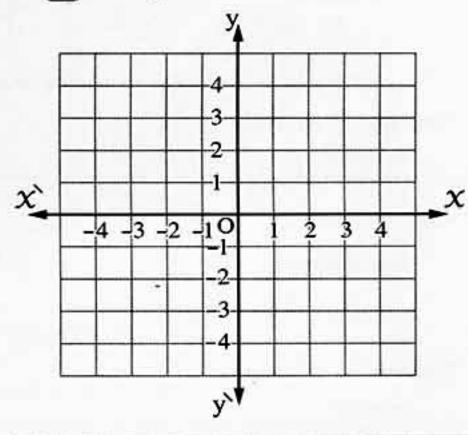
#### Try by yourself

Draw  $\triangle$  ABC where A (1,1), B (4,1) and C (3,3), then draw its image by reflection in:

The X-axis



The y-axis



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Unit 3

## Symmetry

• In the opposite figure:

ABC is a triangle,  $\overrightarrow{AD} \perp \overrightarrow{BC}$ , D is the midpoint of  $\overrightarrow{BC}$ , we find that:

- The image of A by reflection in L is itself (A)
- The image of B by reflection in L is C
- The image of C by reflection in L is B

i.e. The image of  $\triangle$  ABC by reflection in L is  $\triangle$  ACB

We can say that  $\triangle$  ABC is transformed to itself by reflection in the straight line L ,

Therefore the straight line L is called the axis of symmetry of  $\Delta$  ABC



If the reflection in a line transforms the figure to itself, then this line is called an axis of symmetry of the figure.

#### Remark

The axis of symmetry divides the figure into two congruent figures.

## The axes of symmetry of some geometric figures

The figure			
	An isosceles triangle	An equilateral triangle	Scalene
Number of axes of symmetry	1	3	Zero (does not exist)
The figure	Parallelogram	Rectangle	Rhombus
Number of axes of symmetry	Zero (does not exist)	2	2

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The figure	Square	Trapezium	An isosceles trapezium
Number of axes of symmetry	4	Zero (does not exist)	1
The figure	The circle	The regular pentagon	The regular hexagon
Number of axes of symmetry	An infinite number	5	6

# Example (3)

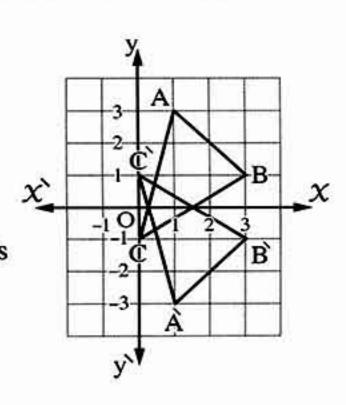
On a square lattice, determine the point A, B and C in each case, then find the image of  $\triangle$  ABC by reflection in  $\overrightarrow{XX}$  (X-axis).

Mention if  $\overrightarrow{xx}$  is an axis of symmetry of  $\triangle$  ABC or not :

- IA(1,3),B(3,1),C(0,-1)
- 2 A(1,2), B(4,0), C(1,-2)

#### Solution

- $\mathbf{II} \bullet \mathbf{A} (1,3) \longrightarrow \hat{\mathbf{A}} (1,-3)$ 
  - $B(3,1) \longrightarrow B(3,-1)$
  - $C(0,-1) \longrightarrow \hat{C}(0,1)$
  - $\therefore \Delta \overrightarrow{ABC}$  is the image of  $\Delta ABC$  by reflection in X-axis
  - $\overrightarrow{x}\overrightarrow{x}$  is not an axis of symmetry of  $\triangle$  ABC because it does not transform the figure ABC to itself by reflection.



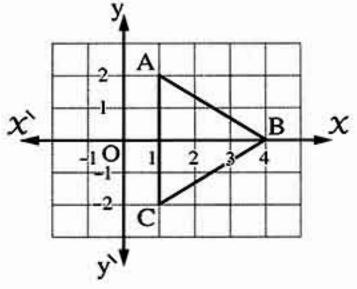
Unit 3



$$B(4,0) \longrightarrow B(4,0)$$
 itself

$$C(1,-2) \longrightarrow A(1,2)$$

- $\therefore$   $\triangle$  CBA is the image of  $\triangle$  ABC by reflection in  $\overrightarrow{XX}$  (X-axis)
- XX is the axis of symmetry of Δ ABC
   because it transforms Δ ABC by reflection in it to itself.



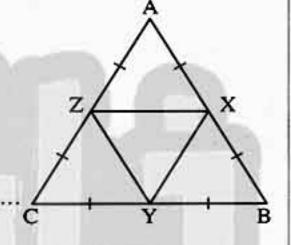
# Try by yourself

In the opposite figure:

ABC is an equilateral triangle. X , Y and Z are the midpoints of its sides.

Complete the following:

- II The image of  $\triangle$  AXZ by reflection in  $\overrightarrow{XZ}$  is .......
- The image of the figure AZYX by reflection in  $\overrightarrow{AY}$  is ......
- $3 \Delta ABC$  is the image of  $\Delta ACB$  by reflection in .......
- 4 The number of axes of symmetry of the figure ABYZ is .........
- 5 The number of axes of symmetry of Δ ABC is .........



Lesson Ten



# Lesson

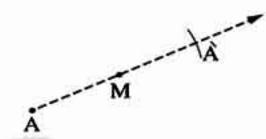
# Follow: Reflection (Reflection in a point)

Reflection in a point M maps each point A in the plane to the point  $\widehat{A}$  in the same plane where M is the midpoint of the line segment  $\overline{A}\widehat{A}$ , the point M is called the centre of reflection and the image of M by reflection in M is itself.



## Finding the image of a point by reflection in a given point

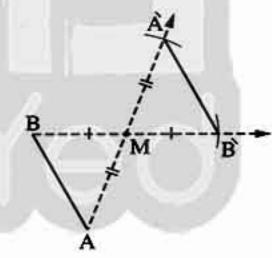
- To find the image of a point as A by reflection in M, we do as follows:
  - Draw AM
  - Using the compasses with open length equals MA, then use M as a centre and draw an arc to intersect AM at a point as A, then A is the image of the point A by reflection in the point M



3 From the previous, we found that: MA = MA

# Finding the image of a line segment by reflection in a given point

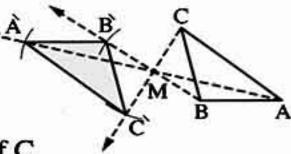
- To find the image of a line segment as  $\overline{AB}$  by reflection in M, we do as follows:
  - I Find the image of A by reflection in M to be A as we mentioned before.
  - 2 Similarly find the image of B by reflection in M to be B
  - 3 Draw  $\overrightarrow{AB}$  to be the image of  $\overrightarrow{AB}$  by reflection in the point M Notice that :  $\overrightarrow{AB} = \overrightarrow{AB}$  and  $\overrightarrow{AB} / / \overrightarrow{AB}$



i.e.: The image of a line segment by reflection in a point is a line segment parallel to the original one and its length equals the length of the original line segment.

## Finding the image of a polygon by reflection in a given point

- ullet To find the image of a polygon as the triangle ABC by reflection in M  $\,_2$  we do as follows :
  - I Find the image of each vertex of the vertices of the triangle ABC by reflection in the point M as we mentioned before to be:



A is the image of A, B is the image of B and C is the image of C

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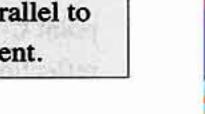
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2 Draw  $\overrightarrow{AB}$ ,  $\overrightarrow{BC}$  and  $\overrightarrow{CA}$  to get  $\overrightarrow{ABC}$  which is the image of  $\overrightarrow{ABC}$  by reflection in the point M

Notice that:

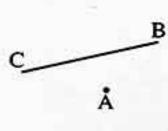
 $\triangle ABC \equiv \triangle ABC$ , therefore it is said that the reflection in a point is **isometric**.

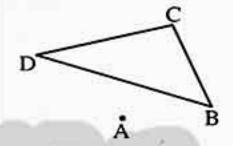
# From the previous, we deduce that:

Reflection in a point is a geometric transformation that maps the geometric figure to another geometric figure congruent to it and has the same orientation of its vertices.

## Try by yourself

In each of the following, map the image of each figure by reflection in the point A:





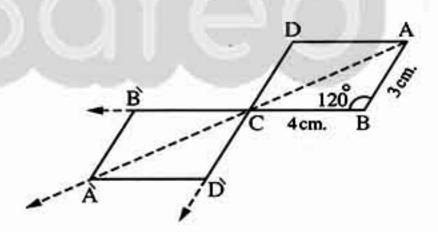
# Properties of reflection in a point

# Illustrated example

Draw the parallelogram ABCD in which AB = 3 cm.  $_{2}$  BC = 4 cm. and m ( $\angle$  B) = 120°, then draw its image by reflection in the point C and show what you observe.

## Solution

Finding the image of each vertex of the vertices of ABCD by reflection in the point C, we find the image of ABCD by reflection in the point C is ABCD



## Notice that :

- $\overrightarrow{AB} = \overrightarrow{AB} \cdot \overrightarrow{BC} = \overrightarrow{BC} \cdot \overrightarrow{CD} = \overrightarrow{CD} \text{ and } \overrightarrow{DA} = \overrightarrow{DA}$ i.e. Reflection in a point reserves the lengths of the line segments.
- $2 m (\angle A) = m (\angle A) \cdot m (\angle B) = m (\angle B),$  $m (\angle BCD) = m (\angle BCD)$  and  $m (\angle D) = m (\angle D)$

i.e. Reflection in a point reserves the measures of angles.

Lesson Ten

3 From the parallelogram ABCD : AB // DC ,

From the parallelogram ABCD: AB // DC

- ... The images of the two parallel line segments are also two parallel line segments.
- i.e. Reflection in a point reserves parallelism.
- 4 The reading of the parallelogram ABCD is in the clockwise direction and the reading of the parallelogram ABCD is in the clockwise direction also.
  - i.e. Reflection in a point reserves the orientation of vertices of the figure.
- 5 Putting a point belongs to AB, we find its image by reflection in C belongs to AB
  - i.e. Reflection in a point reserves the betweenness.

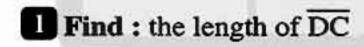
# Example (1

#### In the opposite figure:

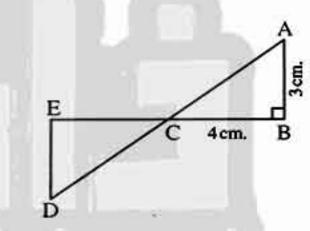
ABC is a triangle in which  $m (\angle B) = 90^{\circ}$ ,

AB = 3 cm.  $\Rightarrow$  BC = 4 cm. and  $\triangle$  DEC

is the image of  $\triangle$  ABC by reflection in C



2 Prove that : AB // DE



# Solution

In  $\triangle$  ABC:  $\therefore$  m ( $\angle$  B) = 90°

:. 
$$(AC)^2 = (AB)^2 + (BC)^2 = (3)^2 + (4)^2 = 25$$
 (Pythagoras' theorem)

- $\therefore$  AC = 5 cm.
- , ... Δ DEC is the image of Δ ABC by reflection in C
- .. DC = AC = 5 cm. (The reflection reserves the lengths of the line segments) (First req.)
- $\cdot$  m ( $\angle$  E) = m ( $\angle$  B) = 90° (Properties of reflection in a point) and they are alternate angles
- ∴ AB // DE (Second req.)

# = Unit 🏅

#### Using reflection in a point to prove that a quadrilateral is a parallelogram

 We mentioned before that the image of a line segment by reflection in a point is a line segment parallel to it and has the same length of the main line segment.

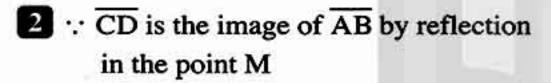
If CD is the image of AB by reflection in the point M, then  $\overline{AB} // \overline{DC}$ , AB = DC

We can prove that the quadrilateral is a parallelogram

by several methods as follows:



.. The quadrilateral ABCD is a parallelogram.



∴ MA = MC and MB = MD

.. The quadrilateral ABCD is a parallelogram.

MA = MC and MB = MD

:. AD is the image of CB by reflection in the point M

.: CD is the image of AB by reflection in the point M

.. AB // DC and AD // BC

.. The quadrilateral ABCD is a parallelogram.

: AD is the image of CB and CD is the image of AB by reflection in the point M

 $\therefore AD = CB \cdot CD = AB$ 

.. The quadrilateral ABCD is a parallelogram.

#### Remember that :

The quadrilateral in which two opposite sides are parallel and equal in length is a parallelogram.

#### Remember that : [

The quadrilateral whose diagonals bisect each other is a parallelogram.

#### Remember that : [

The quadrilateral in which each two opposite sides are parallel is a parallelogram.

## Remember that : [

The quadrilateral in which each two opposite sides are equal in length is a parallelogram.



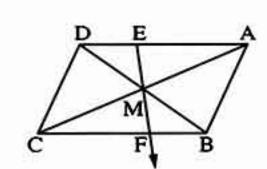
#### In the opposite figure:

ABCD is a parallelogram, M is the point of intersection of its diagonals,  $E \in \overline{AD}$  and  $\overline{EM} \cap \overline{BC} = \{F\}$ 

#### Prove that:

F is the image of E by reflection in M

2 The quadrilateral AFCE is a parallelogram.



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Lesson Ten

#### Solution

- : ABCD is a parallelogram.
- ∴ AD // BC

∴ In ΔΔ AME and CMF:

$$m (\angle DAC) = m (\angle BCA)$$
 (alternate angles)

 $m (\angle AME) = m (\angle FMC) (V.O.A.)$ 

AM = MC (properties of parallelogram)

- $\therefore \triangle AME \equiv \triangle CMF$ , then we deduce that EM = FM
- ,∵F∈<del>EM</del>
- .. F is the image of E by reflection in the point M
- $\cdots$  AM = CM and A  $\in$  CM
- .. A is the image of C by reflection in the point M
- .. AF is the image of CE by reflection in the point M
- $\therefore$  AF = CE and  $\overline{AF} //\overline{CE}$
- .. The quadrilateral AFCE is a parallelogram.



(Q.E.D. 1)



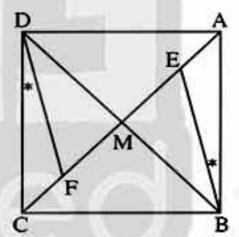
#### In the opposite figure:

ABCD is a square whose diagonals intersect at M,

 $E \in \overline{AC}$  and  $F \in \overline{AC}$  where m ( $\angle ABE$ ) = m ( $\angle CDF$ )

Prove that:

- 1  $\triangle$  ABE is the image of  $\triangle$  CDF by reflection in M
- 2 The quadrilateral EBFD is a rhombus.



## Solution

#### In $\Delta\Delta$ ABE and CDF:

AB = CD (properties of the square)

 $m (\angle BAE) = m (\angle DCF) = 45^{\circ}$  (properties of the square)

 $l m (\angle ABE) = m (\angle CDF) (given)$ 

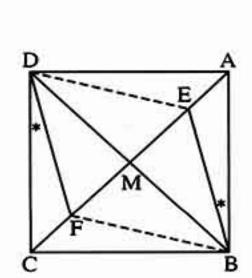
 $\therefore \triangle ABE \equiv \triangle CDF$ , then we deduce that : AE = CF

 $\rightarrow$ : AM = CM (properties of the square) : AM - AE = CM - CF

 $\therefore EM = FM, E \in FM$ .. E is the image of F by reflection in M

 $AM = CM A \in \overline{CM}$ .. A is the image of C by reflection in M

 $,BM = DM ,B \in \overline{DM}$ .. B is the image of D by reflection in M (2)



∴ ∆ ABE is the image of ∆ CDF by reflection in M

(Q.E.D. 1)

From (1) and (2):

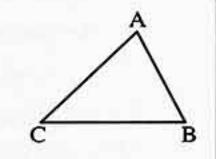
- .: EB is the image of FD by reflection in M
- $\therefore \overline{EB} // \overline{FD}$  and EB = FD
- .. The quadrilateral EBFD is a parallelogram.
- $\cdots$   $\overline{DB} \perp \overline{EF}$  (properties of the square ABCD)
- .. The quadrilateral EBFD is a rhombus.

(Q.E.D. 2)

#### Try by yourself

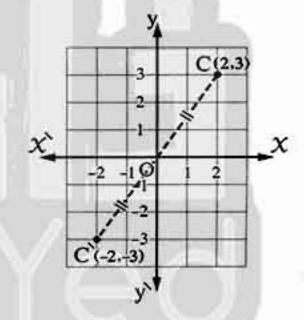
#### In the following figure:

Draw A ABC as the image of  $\triangle$  ABC by reflection in C, then prove that the quadrilateral ABAB is a parallelogram.



# Reflection in the origin point

- If the point C is a point in the Cartesian coordinates plane where C (2,3)
- To find the image of the point C by reflection in the origin point O using the same previous method, we will find it  $\hat{C}$  (-2, -3)



#### Notice that:

The signs of the two projections of the ordered pair (2,3) have been changed, hence we can define the reflection in the origin point as follows:



#### Definition :

If A (X, y) is a point in the Cartesian coordinates plane, then the image of the point A by reflection in the origin point O is  $\hat{A}(-x, -y)$ 

i.e. Reflection in the origin point converts the signs of each of the coordinates of the point.

... The image of the point 
$$(x, y)$$
 by reflection in the origin point  $(-x, -y)$ 

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هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى في المعاصر المعاصر المعاصر المعاصر

Lesson Ten

#### For example:

- The image of the point (2,3) by reflection in the origin point (-2,-3)
- by reflection in the origin point  $\rightarrow$  (4, -1) • The image of the point (-4,1)-
- The image of the point (3, -5) by reflection in the origin point (-3, 5)
- The image of the point (-1, -3) by reflection in the origin point (1, 3)

#### Remark

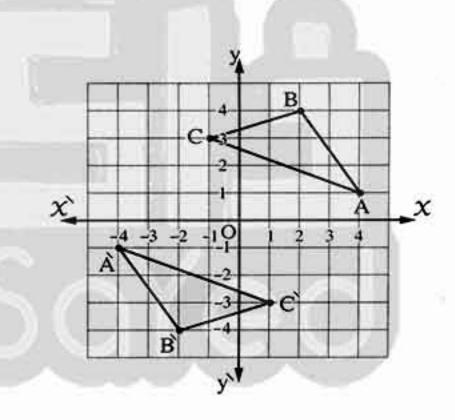
The image of the point (0,0) by reflection in the origin point is itself.

# Example (4

Draw  $\triangle$  ABC where A (4, 1), B (2, 4) and C (-1, 3), then map its image by reflection in the origin point.

#### Solution

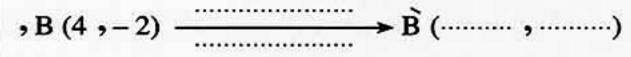
- $\therefore (x,y) \xrightarrow{\text{by reflection in}} (-x,-y)$
- $\therefore A (4, 1) \xrightarrow{\text{by reflection in}} \widehat{A} (-4, -1)$ 
  - B (2,4) by reflection in the origin point  $\overrightarrow{B}$  (-2,-4)
  - C (-1,3) by reflection in the origin point  $\stackrel{>}{\sim}$   $\stackrel{>}{\sim}$   $\stackrel{>}{\sim}$   $\stackrel{>}{\sim}$   $\stackrel{>}{\sim}$   $\stackrel{>}{\sim}$   $\stackrel{>}{\sim}$   $\stackrel{>}{\sim}$

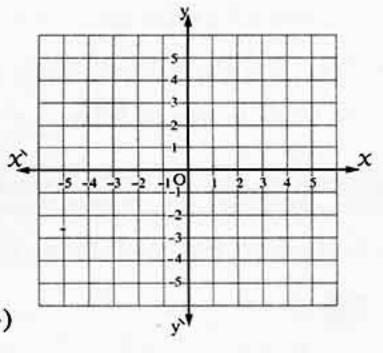


## Try by yourself

Draw on a square lattice  $\triangle$  ABC, where A (-2,1),

B (4, -2) and C (2, 3), then draw its image by reflection in the origin point





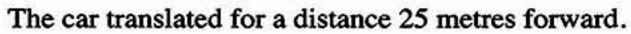
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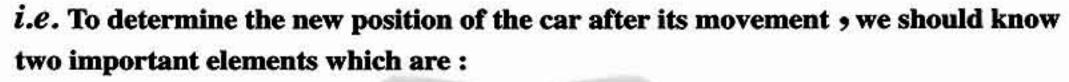


# Translation

#### Prelude

If a car moved a distance 25 metres in a straight line forward, then we say that:





- The magnitude of the translation (25 metres).
- 2 The direction of the translation (forward in a straight line).

#### According to this, we can say that : •

Translation is a geometrical transformation which maps each point A in the plane to another point A in the same plane with a constant distance in a certain direction.

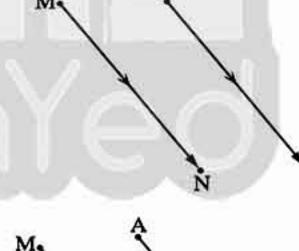
#### Translation in the plane

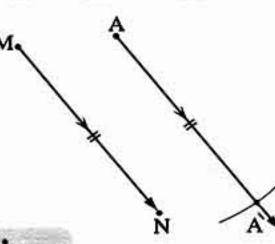
# Finding the image of a point by a given translation

- To find A which is the image of A by translation MN in the direction of MN , we do as follows:
  - I Draw from A a ray parallel to MN and in the same direction.
  - 2 By the compasses in A as a centre with radius = MN , draw an arc to intersect the ray drawn from A at the point  $\hat{A}$  ( $A\hat{A} = MN$  and  $\overline{A\hat{A}}//\overline{MN}$ )
- Then A is the image of A by translation of magnitude MN in the direction of MN

# Finding the image of a line segment by a given translation

- To find the image of  $\overline{AB}$  by translation MN in the direction of  $\overline{MN}$ , we do as follows:
  - I Find the image of the point A by translation MN in the direction of MN as we mentioned before, say A



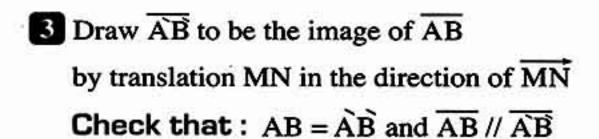


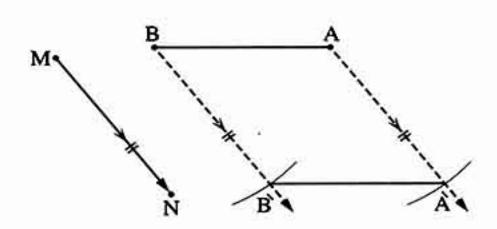
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هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى والعربية العمل خاص بموقع أخرى والعملينية العمل العماصي

Lesson Eleven

2 Similarly, we find the image of the point B by translation MN in the direction of MN, say B

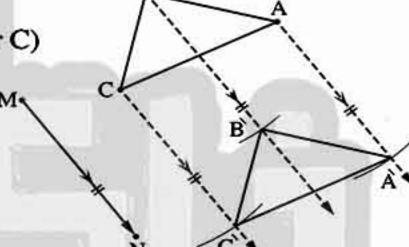




# Finding the image of a polygon by a given translation

To find the image of a polygon as  $\triangle$  ABC by translation MN in the direction of MN , we do as follows:

I Find the image of each vertex of the vertices of  $\triangle$  ABC by translation MN in the direction of MN as we mentioned before (say A for A, B for B and C for C)



2 Draw AB, BC and CA then ΔABC is the image of  $\triangle$  ABC by translation MN in the direction of MN

#### Check that:

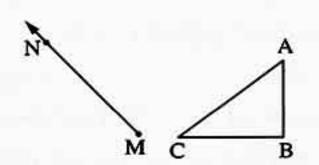
•  $AB = \overrightarrow{AB}$ ,  $BC = \overrightarrow{BC}$  and  $CA = \overrightarrow{CA}$ 

•  $m(\angle A) = m(\angle \hat{A}), m(\angle B) = m(\angle \hat{B}), m(\angle C) = m(\angle \hat{C})$ 

From the previous, we deduce that translation is a geometrical transformation which maps the geometrical figure to another geometrical figure congruent to it.

## Try by yourself

Using the geometrical tools, draw the image of  $\Delta$  ABC by translation MN in the direction of MN as shown:



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Unit 3

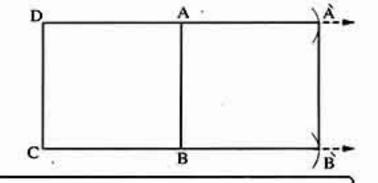
#### Properties of translation

#### Illustrated example

Draw the square ABCD whose side length is 4 cm., then draw its image by translation AB in the direction  $\overrightarrow{DA}$ 

#### Solution

The square ABBA is the image of the square ABCD by translation AB in the direction DA



Notice that :

- $\mathbf{1} \hat{A} \hat{B} = AB , AB = DC$ 
  - i.e. Translation reserves the lengths of the line segments.
- 2 m  $(\angle \hat{A}) = m (\angle BAD)$ , m  $(\angle \hat{B}) = m (\angle CBA)$ 
  - i.e. Translation reserves the measures of angles.
- 3 From the square ABCD :  $\overline{AB}$  //  $\overline{DC}$ , from the square  $\overrightarrow{AB}BA$  :  $\overline{\overrightarrow{AB}}$  //  $\overline{AB}$ 
  - .. The images of the two parallel line segments are also two parallel line segment.
  - i.e. Translation reserves the parallelism.
- The reading of the square ABCD is in the clockwise direction and the reading of the square ABBA is in the clockwise direction also.
  - i.e. Translation reserves the orientation of vertices of the figure.
- If you take a point lies on  $\overline{AB}$  and find its image by the previous translation, you will find its image lies on  $\overline{AB}$ 
  - i.e. Translation reserves the betweenness.

# Example (1)

#### In the opposite figure:

ABC is a triangle, X is the image of B by translation of a distance CA in the direction of  $\overrightarrow{CA}$ ,

Y A 2 2 2 2 B

Y is the image of C by translation of a distance BA in the direction of  $\overrightarrow{BA}$ 

- 2 Determine the translation which makes  $\triangle$  AYC the image of  $\triangle$  XAB

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#### Solution

- : X is the image of B by translation of a distance CA in the direction CA
- .: BX = CA and BX // CA
- (1)  $m (\angle 1) = m (\angle 2)$  (alternate angles)
- , : Y is the image of C by translation of a distance BA in the direction BA
- $\therefore$  CY = BA,  $\overline{CY} // \overline{BA}$
- (2)  $\therefore$  m ( $\angle$  2) = m ( $\angle$  3) (alternate angles) From (1) and (2): We deduce that:  $m (\angle 1) = m (\angle 3)$
- ∴ In ∆ ∆ XAB , AYC :

BX = CA (properties of translation) BA = CY (properties of translation)

 $m (\angle 1) = m (\angle 3)$  (proved)

 $\therefore \Delta XAB \equiv \Delta AYC$ (First req.)

The translation which makes  $\triangle$  AYC is the image of  $\triangle$  XAB is the translation of a distance BC in the direction of BC (Second req.)

## Using the properties of translation to prove that the figure is a parallelogram:

#### We noticed that:

The image of a line segment by a translation is another line segment parallel to it and has the same length of the original line segment.

#### For example:

## In the opposite figure:

If AB is the image of DC by a translation,

then:  $\overline{AB} // \overline{DC}$  and  $\overline{AB} = \overline{DC}$ 

i.e. The figure ABCD is a parallelogram.

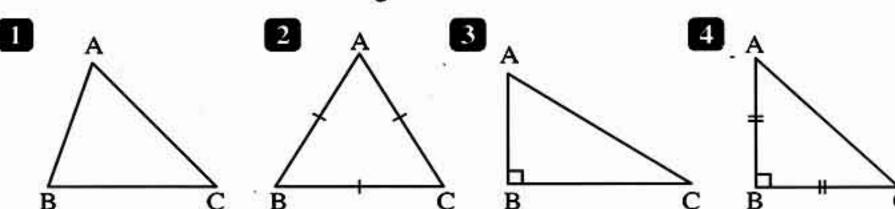
#### Remember that : [

The parallelogram is a quadrilateral in which two opposite sides are parallel and equal in length.

# Example (2

#### In each of the following figures:

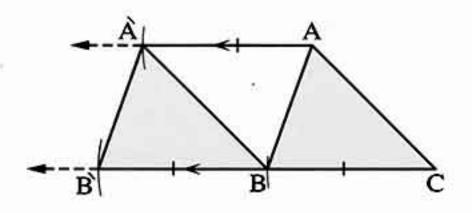
Draw  $\triangle ABB$  as the image of  $\triangle ABC$  by translation of a distance CB in the direction of CB then show the kind of the figure ABBA in each case :

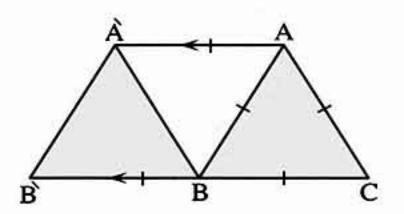


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## Solution

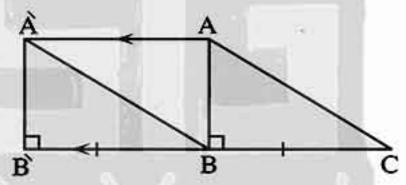
- $\mathbf{I} : \Delta \widehat{ABB}$  is the image of  $\Delta ABC$ 
  - $\therefore \overrightarrow{AB}$  is the image of  $\overrightarrow{AB}$
  - $\therefore \overrightarrow{AB} / / \overrightarrow{AB} \cdot \overrightarrow{AB} = AB$
  - .. The figure ABBA is a parallelogram.
- $2 : \Delta \overrightarrow{ABB}$  is the image of  $\Delta \overrightarrow{ABC}$ 
  - $\therefore$   $\overrightarrow{AB}$  is the image of  $\overline{AB}$
  - $\therefore \overrightarrow{AB} / / \overrightarrow{AB} \cdot \overrightarrow{AB} = AB$
  - .. The figure ABBA is a parallelogram.
  - $, :: \Delta ABC \equiv \Delta \stackrel{\sim}{ABB}B$
  - ∴ ∆ ABB is an equilateral triangle
  - $\therefore \hat{A}\hat{B} = \hat{B}B$
  - .. The figure ABBA is a rhombus.
- $3 :: \Delta \stackrel{\frown}{ABB}$  is the image of  $\Delta \stackrel{\frown}{ABC}$ 
  - : AB is the image of AB
  - $\therefore \overrightarrow{AB} / / \overrightarrow{AB}, \overrightarrow{AB} = \overrightarrow{AB}$
  - .. The figure ABBA is a parallelogram.
  - $m (\angle B) = m (\angle B) = 90^{\circ}$
  - .. The figure ABBA is a rectangle.
- $4 : \Delta \stackrel{>}{ABB} = 1$  is the image of  $\Delta \stackrel{>}{ABC}$ 
  - $\therefore$   $\overrightarrow{AB}$  is the image of  $\overrightarrow{AB}$
  - $\therefore \overrightarrow{AB} / / \overrightarrow{AB}, \overrightarrow{AB} = AB$
  - .. The figure ABBA is a parallelogram.
  - $m (\angle B) = m (\angle B) = 90^{\circ}$ 
    - $\rightarrow AB = BB$
  - .. The figure ABBA is a square.





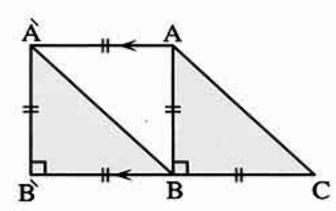
## Remember that :

The rhombus is a parallelogram in which two adjacent sides are equal in length.



#### Remember that :

The rectangle is a parallelogram one of its angles is right.



## Remember that : [

The square is a parallelogram in which one of its angles is right and two adjacent sides are equal in length.

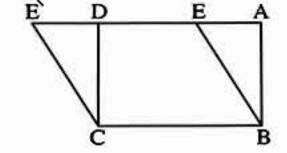
Lesson Eleven

# Example (3)

Draw the rectangle ABCD. Take the point  $E \in \overline{AD}$ , then find the image of E by translation DA in the direction of  $\overrightarrow{AD}$ . Then prove that the figure EBCÈ is a parallelogram.

#### Solution

• We take  $\hat{E} \in \overrightarrow{AD}$  such that  $\hat{E}E = AD$ , then  $\hat{E}$ is the image of E by translation DA in the direction of AD



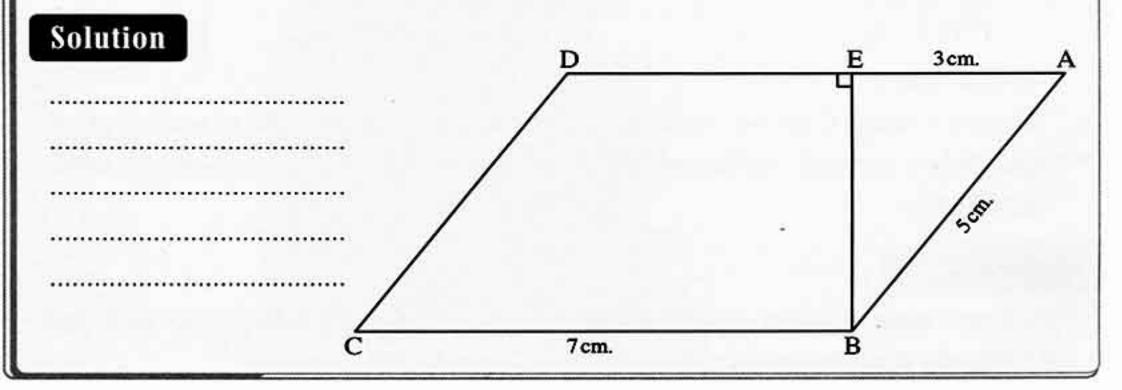
- : ABCD is a rectangle.
- $\therefore \overline{AD} // \overline{BC}$  and  $\overline{AD} = \overline{BC}$
- .. C is the image of B by translation AD in the direction of AD
- , : È is the image of E by the same translation.
- .: EC is the image of EB by translation AD in the direction of AD
- $\therefore$  EB =  $\stackrel{.}{E}$ C and  $\stackrel{.}{E}$ B //  $\stackrel{.}{E}$ C
- .. The figure EBCE is a parallelogram.

#### In the following figure:

ABCD is a parallelogram in which AB = 5 cm.  $_{2}$  BC = 7 cm. and E  $\in$  AD where AE = 3 cm.

If  $\overline{BE} \perp \overline{AD}$ , draw  $\triangle DCE$  as the image of  $\triangle ABE$  by translation of a distance 7 cm. in the direction of AD:

- Prove that the figure EBCE is a rectangle.
- 2 Determine the distance and the direction of the translation which transforms BC to EE



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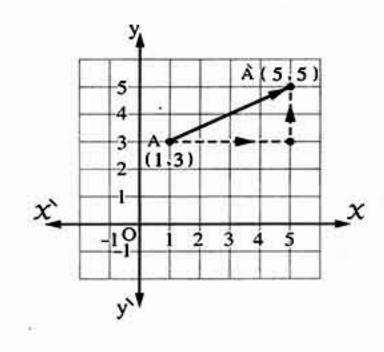
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## Translation in the Cartesian plane

If A (1,3) is a point in the orthogonal coordinates plane and to find its image A by translation with magnitude 4 length units in the direction of  $\overrightarrow{OX}$ followed by a translation with magnitude 2 length units in the direction of OY

From the graph, we get  $\hat{A}$  to be the point (5,5)

*i.e.* 
$$\overrightarrow{A}$$
 (1 + 4 , 3 + 2)



#### According to this : •

Translation in the orthogonal Cartesian coordinates plane transforms each point by a displacement a in the direction of the X-axis followed by a displacement b in the direction of the y-axis

i.e. The image of the point A (x, y) — the point A (x + a, y + b)

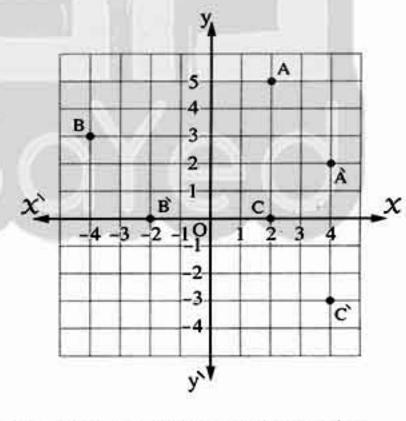
# Example (4

Find the images of the points A (2,5), B (-4,3) and C (2,0)by translation  $(x, y) \longrightarrow (x+2, y-3)$ 

## Solution

$$(x,y) \longrightarrow (x+2,y-3)$$
, then:

- The image of A (2,5) is  $\hat{A}$  (2+2,5-3) i.e. A (4,2)
- The image of B (-4,3) is  $\hat{B}(-4+2,3-3)$ i.e. B (-2,0)
- The image of C (2,0) is  $\hat{C}$  (2+2,0-3) i.e. C (4, -3)



#### Notice that :

The translation  $(x, y) \longrightarrow (x + 2, y - 3)$  transforms each point to another point by a right horizontal displacement of 2 units and a vertical displacement of 3 units downwards.

# Example (5

Draw on a square lattice  $\triangle$  ABC where A (4,4), B (0,2), C (6,-2), then find its image by translation  $(x, y) \longrightarrow (x-4, y+1)$ 

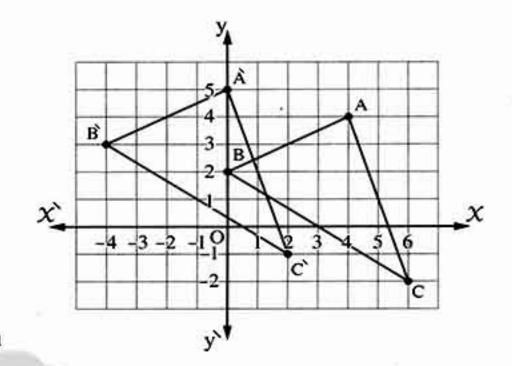
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#### Solution

The point	Its image by the translation		
(x,y)	(x-4,y+1)		
A (4,4)	À (0,5)		
B (0,2)	B (-4,3)		
C (6,-2)	Č(2,-1)		

 $\therefore \triangle ABC$  is the image of  $\triangle ABC$  by translation  $(x,y) \longrightarrow (x-4,y+1)$ 



#### Remark

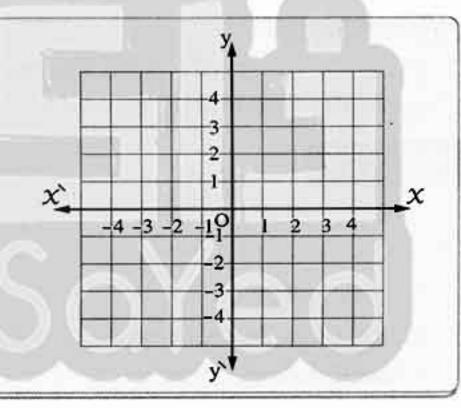
The translation  $(X, y) \longrightarrow (X + a, y + b)$  can be written as the translation (a, b) for example: The translation  $(x, y) \longrightarrow (x + 2, y - 1)$  can be written as the translation (2, -1)

#### Try by yourself

On a square lattice, draw ABC where A (-3,2), B (-1,1), C (-2,0), then find its image by translation :

$$(x,y) \longrightarrow (x+2,y+1)$$
  
 $\hat{A} = (\dots,y)$ 

$$\vec{\mathbf{B}} = (\cdots, \cdots)$$

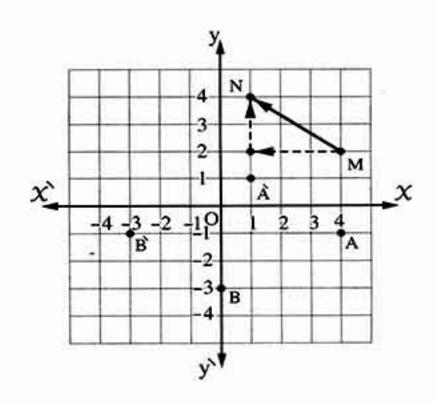


# Example (6

Find the image of each of the two points A (4, -1) and B (0, -3) by translation with magnitude MN in the direction of MN where M (4,2) and N (1,4)

## Solution

By noticing the opposite graph, we find that the translation with magnitude MN in the direction of  $\overline{MN}$  where M (4, 2) and N (1,4) is equivalent to:



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- Horizontal displacement from 4 to 1 *i.e.* a displacement = 3 units to the left (-3)
- Vertical displacement from 2 to 4

*i.e.* a displacement = 2 units upwards (2)

i.e.  $(x, y) \longrightarrow (x-3, y+2)$ , thus we get:

$$A(4,-1) \longrightarrow A(4-3,-1+2)$$

i.e. A (1,1)

$$B(0,-3) \longrightarrow B(0-3,-3+2)$$

*i.e.*  $\vec{B}$  (-3,-1)

Notice that :

The translation with magnitude MN in the direction of MN where M (4,2) and N (1,4) is equivalent to:

- A horizontal displacement (in the X-axis direction) from 4 to 1 = 1 4 = -3
- A vertical displacement (in the y-axis direction) from 2 to 4 = 4 2 = 2*i.e.* The rule of translation is  $(x, y) \longrightarrow (x-3, y+2)$

Draw the image of  $\triangle$  ABC where A (5,2), B (4,5) and C (2,2) by translation BC in the direction of BC and write the rule of the translation.

#### Selution

- : B (4,5), C (2,2)
- .. The translation BC in the direction of BC is equivalent to:
- Horizontal displacement = 2 4 = -2
- Vertical displacement = 2 5 = -3

Thus the rule of translation

is 
$$(x, y) \longrightarrow (x-2, y-3)$$

Thus:

$$A(5,2) \longrightarrow \hat{A}(5-2,2-3)$$

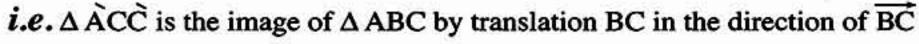
i.e. A (3 ,-1)

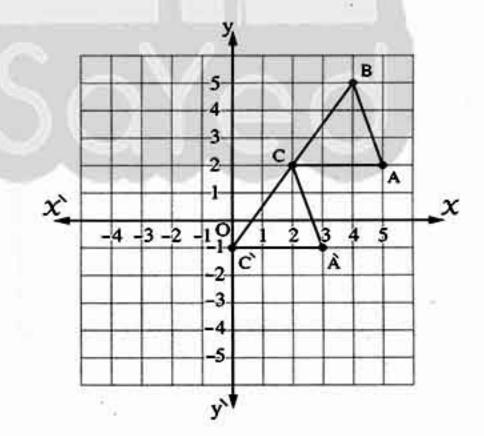
$$B(4,5) \longrightarrow B(4-2,5-3)$$

i.e. B (2,2)

$$C(2,2) \longrightarrow \hat{C}(2-2,2-3)$$

i.e. C (0,-1)





Notice that :

B coincides C

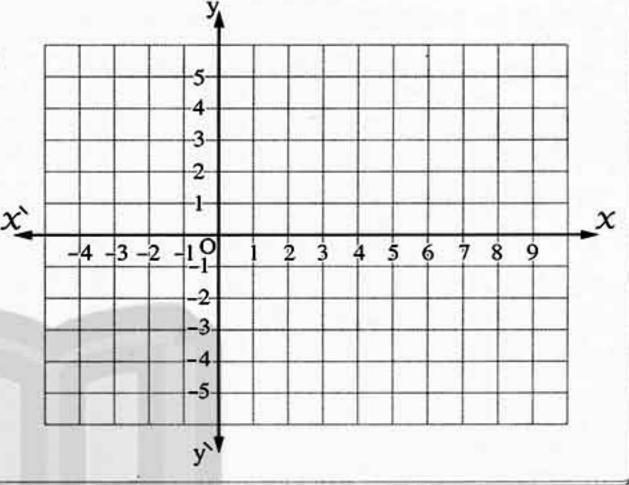
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Lesson Eleven

## Try by yourself

Draw the square ABCD where A(4,-2), B(4,-5), C(1,-5)and D (1, -2), then find its image by translation CA in the direction of CA



# Example 8

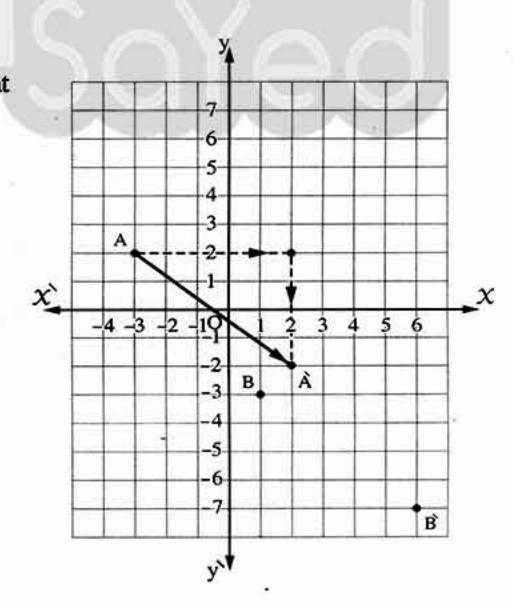
If the image of the point A (-3, 2) by translation in the Cartesian coordinates plane is  $\hat{A}(2,-2)$ :

- I Find the rule of translation.
- 2 Find the image of B (1, -3) by the same translation.

#### Solution

- By noticing the opposite graph, we find that the translation which makes  $\hat{A}$  (2, -2) the image of A (-3, 2) is equivalent to:
  - Horizontal displacement of 5 units to the right side (5)
  - Vertcial displacement of 4 units downwards (-4) .. The rule of translation is
  - $(X,y) \longrightarrow (X+5,y-4)$

2 B (1,-3) 
$$\rightarrow$$
 B (1+5,-3-4)  
*i.e.* B (6,-7)



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Unit  $oldsymbol{3}$ 

# Example 9

If  $\hat{A}$  (7 > -2) is the image of A by the translation whose rule

is  $(x, y) \longrightarrow (x-3, y+1)$ , find A

#### Solution

Let A be (X, y)

$$\therefore A(x,y) \longrightarrow \hat{A}(x-3,y+1)$$

 $\cdot : \stackrel{\sim}{A} (7 \cdot -2)$ 

$$\therefore (X-3,y+1)=(7,-2)$$

$$\therefore x-3=7$$

$$\therefore x = 10$$

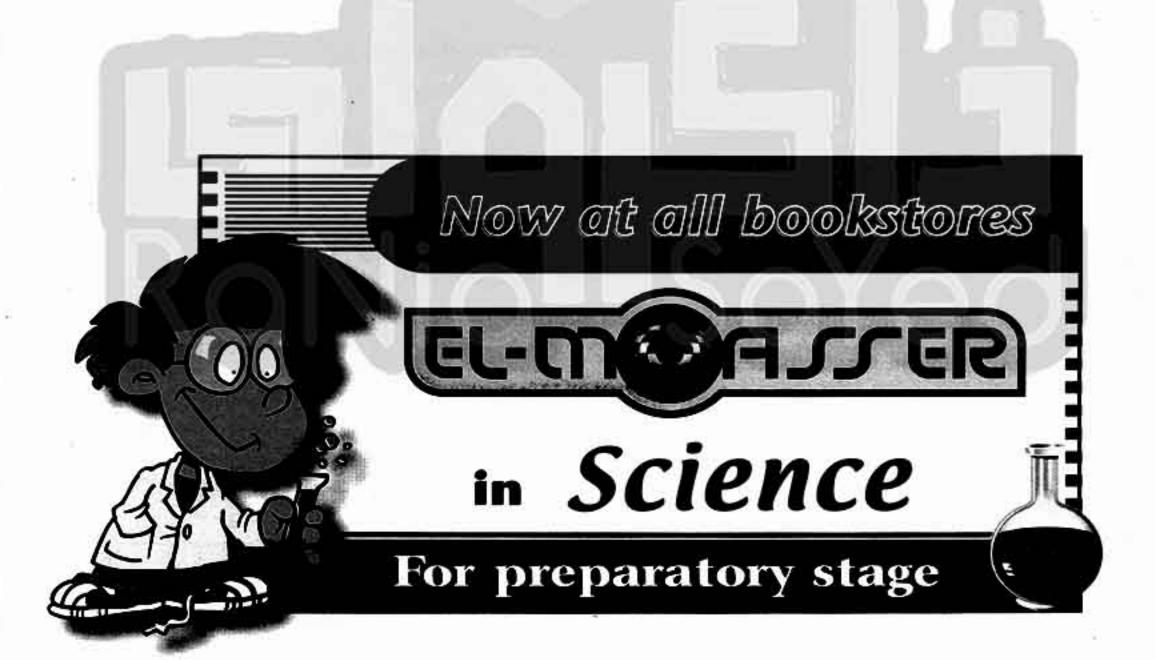
$$y + 1 = -2$$

$$\therefore A(10,-3)$$

# Notice that :

If 
$$(X, y) = (a, b)$$
, then  $X = a, y = b$ 

$$\therefore y = -3$$



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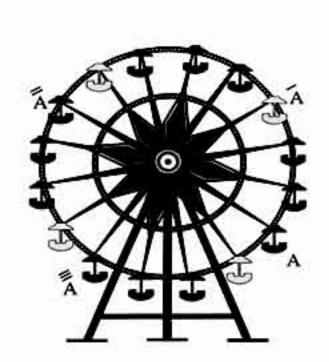
Lesson Twelve



## Rotation

#### Prelude

If you stand in front of the spinning wheel play in the funfair , you will find that the carriage moves in a circular motion around a fixed point in a certain direction with a certain angle. It will take different positions as shown in the opposite picture. The carriage moves from position A to position A, then to position A, then to position A, then it returns back to its original position to complete the perfect circulation and so on.

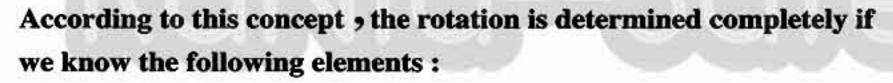


#### The concept of rotation

If M is a fixed point in the plane, then the rotation around M with an angle of measure  $\theta$ is a geometric transformation transforming each point A in the plane to another point A in the same plane such that  $m (\angle AMA) = \theta , MA = MA$ 

It is denoted by R  $(M, \theta)$  where:

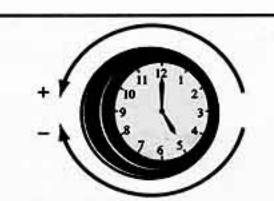
- M is the centre of rotation.
- θ is the measure of the angle of rotation.



- The centre of rotation.
- 2 The measure of the angle of rotation  $(\theta)$
- 3 The direction of rotation.

#### Remark

The measure of rotation angle is positive if the rotation is anticlockwise and it is negative if the rotation is clockwise.



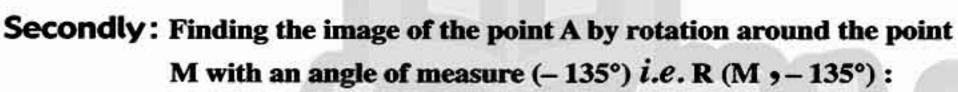
هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى المعنف الاول الاحدادي معنى التعليمي المعنف الاول الاحدادي معنى المعنف الاول الاحدادي المعنف المعنف الاحدادي المعنف الاحدادي المعنف المعنف الاحدادي المعنف المعنف الاحدادي المعنف المعنف

## Rotation in the plane

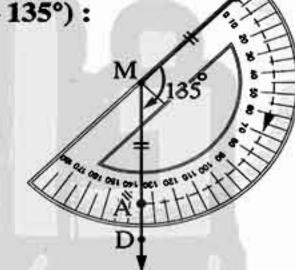
Finding the image of a given point by a given rotation

Firstly: Finding the image of the point A by rotation around the point M with an angle of measure 45° i.e. R (M , 45°):

- Draw the ray MA
- Put the protractor with its straight edge on MA and in the anticlockwise direction , then draw  $\overline{MC}$  such that m ( $\angle$  AMC) = 45°
- Use the compasses at the point M as a centre with radius = MA, draw an arc to cut MC at A then A is the image of the point A by rotation around M with an angle of measure 45°



• Repeat the same previous steps, then draw MD in the clockwise direction such that  $m (\angle AMD) = 135^{\circ}$ , then determine on it the point A such that MA = MA, then A is the image of A by rotation around M with an angle of measure (- 135°)

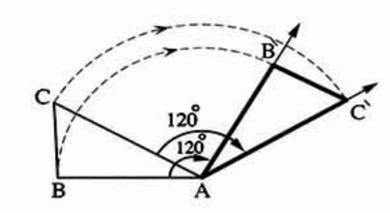


#### Remark

If A is the image of A by rotation around M with an angle θ, then A is the image of A by rotation around M with an angle of measure  $(-\theta)$ 

## Finding the image of a polygon

The opposite figure shows how to find the image of  $\triangle$  ABC by the rotation R (A<sub>2</sub> – 120°) by finding the image of each vertex of its vertices , then Δ ABC is the image of  $\triangle$  ABC by rotation R (A  $\rightarrow$  120°)



Notice that :  $\triangle ABC \equiv \triangle ABC$ 

#### Remark

From the previous figure, the image of the point A by rotation R  $(A, -120^\circ)$  is itself because it is the centre of rotation.

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Lesson Twelve

#### **Properties of rotation**

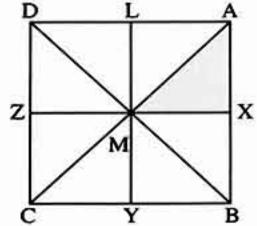
Through our study of rotation, we found that the rotation is a geometric transformation that maps the figure to another congruent figure to it.

Therefore it is said that the rotation in the plane is isometric, thus we can deduce some of properties and add other properties through our study of the following illustrated example.

#### lllustrated example

#### In the opposite figure:

ABCD is a square whose diagonals intersect at M, X, Y, Z and L are the midpoints of its sides AB, BC, CD and DA respectively.



#### Find:

- The image of  $\triangle$  AXM by rotation R (M , 90°), then mention what you observe.
- The image of each of  $\overline{AB}$  and  $\overline{DC}$  by rotation R (M  $_{2}$ -90°), then mention what you observe.
- 3 The image of each of B, Y and C by rotation R (M, 180°), then mention what you observe.

#### Solution

- ... D is the image of A by rotation R (M, 90°), L is the image of X by rotation R (M, 90°) and M is the image of itself (The centre of rotation).
  - ∴ ∆ DLM is the image of ∆ AXM by rotation R (M, 90°) Notice that :
    - DL = AX , LM = XM and DM = AM
      - Rotation in the plane reserves the lengths of the line segments.
    - m ( $\angle$  DLM) = m ( $\angle$  AXM), m ( $\angle$  LDM) = m ( $\angle$  XAM) and  $m (\angle DML) = m (\angle AMX)$ 
      - Rotation in the plane reserves the measures of angles.
    - Reading A AXM is in the clockwise direction and reading its image  $\Delta$  DLM is in the clockwise direction also.
      - Rotation in the plane reserves the orientation of vertices of the figure.
- 2 : B is the image of A by rotation R (M > -90°) C is the image of B by rotation  $R(M, -90^{\circ})$ 
  - $\therefore$  BC is the image of AB by rotation R (M  $\rightarrow$  90°)
  - : A is the image of D by rotation R (M > 90°) D is the image of C by rotation R (M  $\rightarrow$  – 90°)
  - $\therefore$  AD is the image of DC by rotation R (M  $\Rightarrow$  90°)

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#### We notice that:

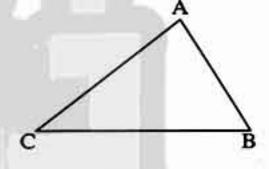
- AB // DC and BC // AD
  - i.e.: Rotation in the plane reserves parallelism.
- D is the image of B, L is the image of Y and A is the image of C by rotation (M, 180°)
  - We notice that:
  - $Y \in \overline{BC}$  and L (The image of Y)  $\in \overline{AD}$ 
    - Rotation in the plane reserves the betweenness.
  - B, Y, C are collinear, D, L, A are also collinear.
    - Rotation in the plane reserves the collinearity.

#### In the opposite figure:

ABC is a triangle Find:

- The point D as the image of B by rotation R  $(A \cdot m (\angle B))$
- The point E as the image of C by rotation R  $(A \rightarrow m (\angle C))$

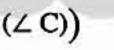
Then prove that: The points D, A and E are collinear.

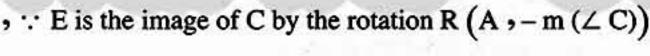


#### Solution

 $\therefore$  D is the image of B by the rotation R (A, m ( $\angle$  B))

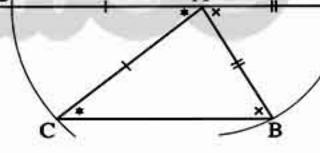
$$\therefore$$
 m ( $\angle$  DAB) = m ( $\angle$  B)





$$\therefore m (\angle EAC) = m (\angle C)$$

(2)



Adding (1) and (2), we deduce that:

$$m (\angle DAB) + m (\angle EAC) = m (\angle B) + m (\angle C)$$

Adding m ( $\angle$  BAC) to both sides,

- $\therefore m (\angle DAB) + m (\angle EAC) + m (\angle BAC) = m (\angle B) + m (\angle C) + m (\angle BAC)$
- : The sum of measure of the interior angles of the triangle = 180°
- $\therefore$  m ( $\angle$  B) + m ( $\angle$  C) + m ( $\angle$  BAC) = 180°
- $\therefore$  m ( $\angle$  DAB) + m ( $\angle$  EAC) + m ( $\angle$  BAC) = 180°
- .. D , A and E are collinear.

(Q.E.D.)

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Lesson Twelve

# Example (2)

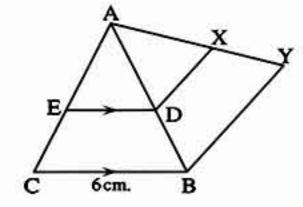
#### In the opposite figure:

If the figure XYBD is the image of the figure DBCE by the rotation R (A, 50°),

 $BC = 6 \text{ cm.}, \overline{DE} // \overline{BC}$ 

Find the length of: BY

Prove that : DX // BY



# Solution

- ☐ ∵ The figure XYBD is the image of the figure DBCE by the rotation R (A , 50°).
  - .. B is the image of C and Y is the image of B by this rotation.
  - .. BY is the image of CB by this rotation.

$$\therefore$$
 BY = CB = 6 cm.

(First req.)

- 2 : The figure XYBD is the image of the figure DBCE by rotation R (A, 50°)
  - .. XD and YB are the images of DE and BC by this rotation respectively.
  - , ∵ DE // BC

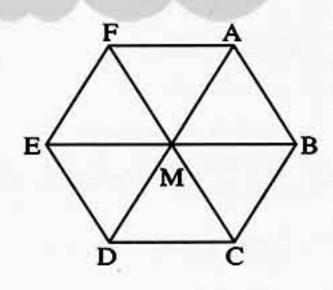
∴ XD // BY

(Second req.)

## In the opposite figure:

ABCDEF is a regular hexagon. Complete the following:

- The image of the point A by rotation around M with an angle of measure 180° is .....
- 2 The image of AB by rotation around M with an angle of measure (-60°) is ......
- The image of Δ CMD by rotation around M with an angle of measure 120° is .....



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## Rotation in the Cartesian plane

#### First

Rotation about the origin point (O) with an angle of measure 90°:

#### The opposite figure:

shows the two images of the two points

A 
$$(3, 1)$$
 and B  $(-2, 1)$ 

by rotation R (O, 90°)

# By noticing the figure, we find that:

- The image of the point A (3, 1) by rotation the point  $\hat{A}$  (-1, 3) R (O, 90°)
- The image of the point B (-2, 1)  $\xrightarrow{\text{by rotation}}$  the point B (-1, -2)

# From the previous, we deduce the following rule:

The image of the point (x, y) by rotation the point (-y, x)R (O, 90°)

#### Remark

• The image of the point (x, y)  $\xrightarrow{\text{by rotation}}$  the point (y, -x)

For example:

- The image of the point (2, -3) by rotation the point (-3, -2)
- Rotation about the origin point with an angle of measure 270° is equivalent to rotation about the origin point with an angle of measure (- 90°)

#### For example :

• The image of the point (2, -3) by rotation the point (-3, -2)R (O, 270°)

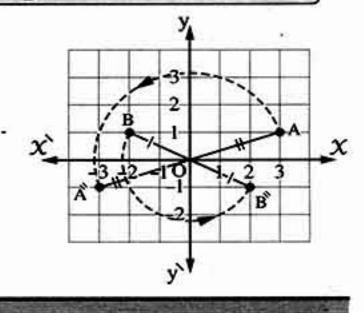
#### Second Rotation about the origin point (O) with an angle of measure 180°:

#### The opposite figure:

shows the two images of the

two points A (3, 1) and B (-2, 1)

by rotation R (O, 180°)



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Lesson Twelve

#### By noticing the figure, we find that:

- The image of the point A (3, 1)  $\xrightarrow{\text{by rotation}}$  the point A (-3, -1) R (O, 180°)
- The image of the point B (-2, 1) by rotation the point B (2, -1)

## From the previous, we deduce the following rule:

The image of the point (x, y) by rotation the point (-x, -y)R (O, 180°)

#### Remarks

- The image of the point A (x, y) by rotation R  $(0, 180^\circ)$  is the same image of the point A by rotation R (O , - 180°)
- The image of the point A (x, y) about the origin point with an angle of measure  $\pm$  360° is the same point A ( $\chi$ , y)
- 3 Rotation with an angle of measure 90° is called a  $\frac{1}{4}$  turn.
- 4 Rotation with an angle of measure 180° is called a  $\frac{1}{2}$  turn.
- 5 Rotation with an angle of measure 360° is called the identity rotation because it returns the figure to its original position.

## Complete the following table:

The point	Its image by rotation R (O , ± 180°)	Its image by rotation R (O, 90°)		
(3,2)		3444444444444		
2 (-3,4)	***************************************	***************************************		
(-2,-1)		******************		
<b>3</b>	(5, -2)			
5		(6,0)		

# Solution

$$1 (-3,-2), (-2,3)$$

$$3(2,1),(1,-2)$$

$$5(0,-6),(0,6)$$

$$2(3,-4),(-4,-3)$$

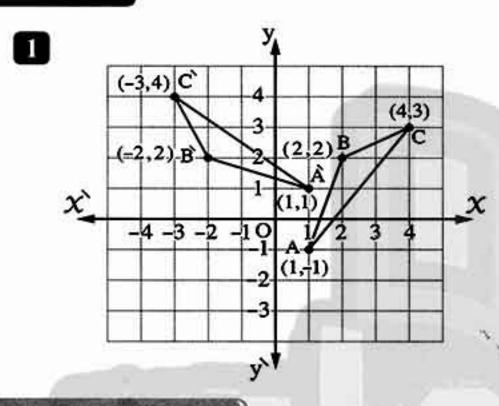
$$4(-5,2),(-2,-5)$$

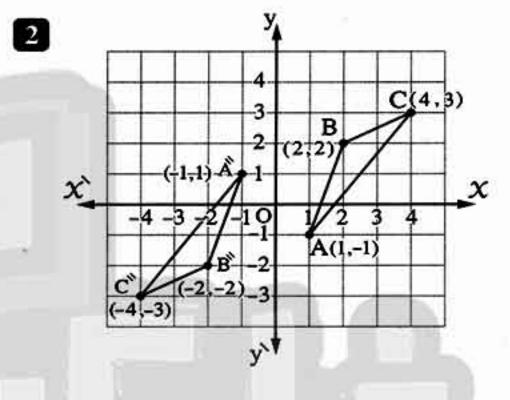
# Example (4)

On a square lattice, draw  $\triangle$  ABC where A (1, -1), B (2, 2) and C (4, 3):

- Draw Δ ÀBC which is the image of Δ ABC by rotation R (O , 90°)
- 2 Draw Δ ABC which is the image of Δ ABC by rotation R (O , 180°)

# Solution





#### Try by yourself

In the opposite figure:

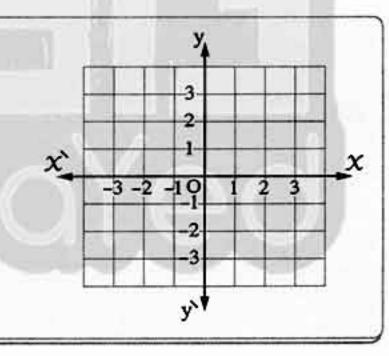
on the square lattice,

draw AB where A (2, 1) and B (1, 3),

then draw its image by rotation:

R (O, 90°)

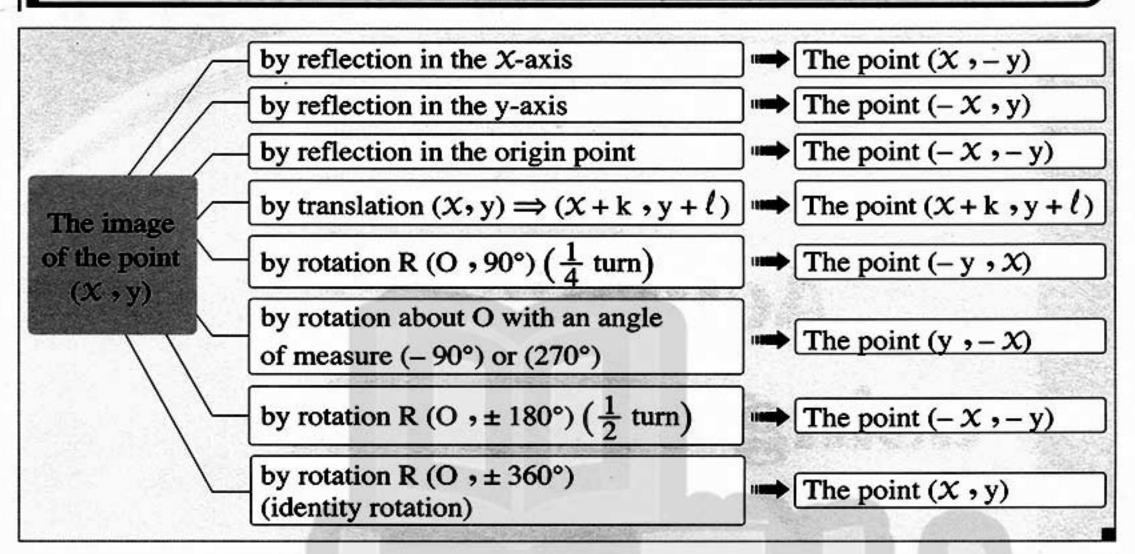
2 R (O, 180°)



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Lesson Twelve

## Summary for geometrical transformations (reflection, translation, rotation) in the Cartesian plane:



#### Try by yourself

2+2-8

The image _	by reflection in the X-axis	,	The point ()
	by reflection in the y-axis	11000	The point ()
	by reflection in the origin point	11000	The point ()
	by translation $(x, y) \Rightarrow (x-3, y+4)$	11000	The point ()
of the point _	by rotation R (O , 90°)	-	The point ()
(2,-1)	by rotation R (O , – 90°)	-	The point ()
	by rotation R (O , ± 180°)	-	The point ()
_	by rotation R (O > ± 360°)	-	The point ()

#### Optical illusion

Look at the picture.

Turn the book with an angle of measure 180° and look at it again.

What do you notice?





# HODING FRY 8

Lesson One : Deductive proof.

Lesson Two: The polygon.

Lesson Three: The parallelogram and its properties.

Lesson Four: The special cases of the parallelogram.

Lesson Five : The triangle :

Theorem (1), the measure of the

exterior angle of a triangle.

**Lesson Six** : Theorem (2), theorem (3).

Lesson Seven: Pythagoras' theorem.

Lesson Eight: Geometric transformations.

**Lesson Nine**: Reflection in a straight line.

**Lesson Ten**: Reflection in a point.

Lesson Eleven: Translation.

Lesson Twelve: Rotation.

General exercises at the end of the unit.

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☐ From the school book

# Exercise 1

# On deductive proof

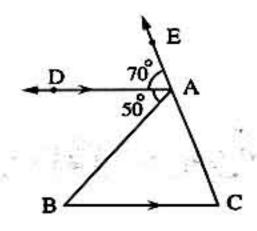
1 In the opposite figure:

$$\overrightarrow{AD} / / \overrightarrow{BC}$$
,

$$m (\angle DAB) = 50^{\circ}$$

and m (
$$\angle$$
 DAE) = 70°

Find the measures of the angles of  $\Delta$  ABC



Complete the following table by writting the reason of each step of the solution steps:

Mathematical Statement	The reason
$m (\angle DAB) = 50^{\circ} \cdot m (\angle DAE) = 70^{\circ}$	Given
$m (\angle CAB) = 180^{\circ} - (50^{\circ} + 70^{\circ}) = 60^{\circ}$	<b>(1)</b>
AD // BC	<b>②</b>
$m (\angle C) = m (\angle DAE) = 70^{\circ}$	(3) ····
$m (\angle B) = m (\angle DAB) = 50^{\circ}$	

2 In the opposite figure:

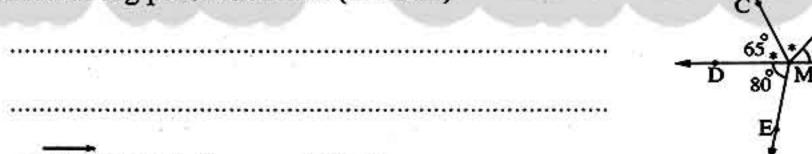
$$m (\angle AMB) = 50^{\circ}$$
,  $m (\angle EMD) = 80^{\circ}$ ,  $\overrightarrow{MC}$  bisects  $\angle BMD$  and  $m (\angle CMD) = 65^{\circ}$ 

Complete the following proof to find m (∠ AME)

Given

R.T.F.

**Proof** 



∴ MC bisects ∠ ..... (given)

∴ m (∠ BMC) = m (∠ ·······) = ······°

$$m (\angle AMB) + m (\angle BMC) + m (\angle CMD) + m (\angle DME) + m (\angle AME) = \dots$$

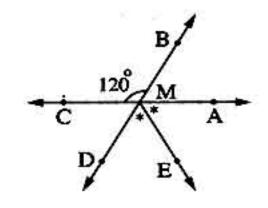
$$\therefore m (\angle AME) = \dots \circ - \dots \circ = \dots \circ$$
 (The req.)

Lesson One

#### 3 In the opposite figure:

$$\overrightarrow{AC} \cap \overrightarrow{BD} = \{M\}$$
, m ( $\angle BMC$ ) = 120°  
and  $\overrightarrow{ME}$  bisects  $\angle AMD$ 

Complete the following solution steps to find m ( $\angle$  EMC)



Given

R.T.F.

Proof

$$\therefore \overrightarrow{AC} \cap \overrightarrow{BD} = \{M\}$$

$$\therefore$$
 m ( $\angle$  BMC) = m ( $\angle$  ·······) (V.O.A.)

$$\therefore$$
 m ( $\angle$  BMC) + m ( $\angle$  ·······) = 180°

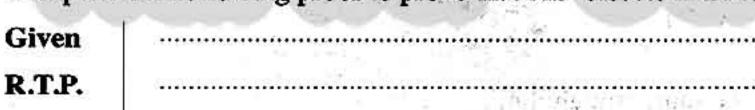
$$m (\angle EMC) = m (\angle \dots + m (\angle \dots))$$

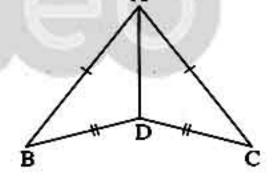
(The req.)

#### 4 In the opposite figure:

$$AB = AC \cdot BD = CD$$

Complete the following proof to prove that AD bisects ∠ BAC





Proof

$$\therefore$$
 In  $\triangle \triangle$  ADB, .....:

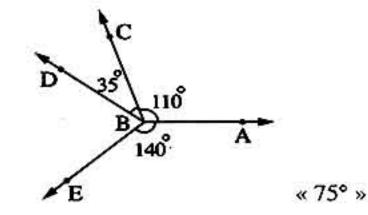
$$\therefore \Delta ADB \equiv \Delta \cdots$$
 then we deduce that :

$$m (\angle \cdots ) = m (\angle \cdots )$$

#### 5 🕮 In the opposite figure :

m (
$$\angle$$
 ABC) = 110°, m ( $\angle$  CBD) = 35° and m ( $\angle$  ABE) = 140°

Find:  $m (\angle EBD)$ 



« 32° »

« 100° »

« 110° »

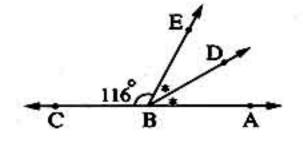
« 105° »

#### 6 🕮 In the opposite figure :

$$B \in \overrightarrow{AC}$$
, m ( $\angle$  CBE) = 116° and

BD bisects ∠ ABE

Find: m (∠ ABD)

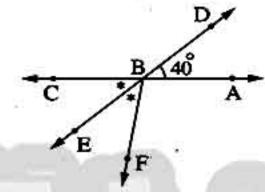


#### 7 u In the opposite figure :

$$\overrightarrow{AC} \cap \overrightarrow{DE} = \{B\}$$
, m ( $\angle ABD$ ) = 40° and

BE bisects ∠ CBF

Find: m (∠ ABF)

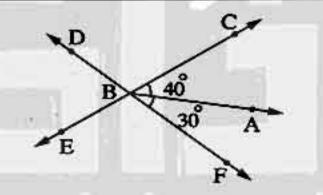


#### 8 In the opposite figure :

$$\overrightarrow{CE} \cap \overrightarrow{FD} = \{B\}$$
,

 $m (\angle ABC) = 40^{\circ} \text{ and } m (\angle ABF) = 30^{\circ}$ 

Find:  $m (\angle DBC)$ 



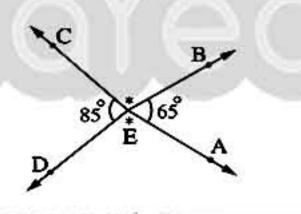
#### 9 In the opposite figure:

 $EA \cap EB \cap EC \cap ED = \{E\}$ 

If  $m (\angle BEC) = m (\angle AED)$ 

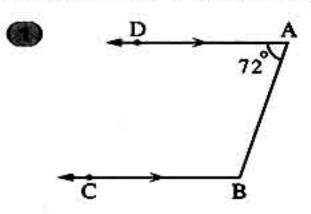
Find: m (∠ BEC)

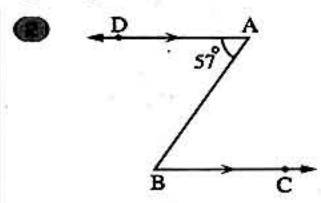
Are A, E, and C on the same straight line? Why?

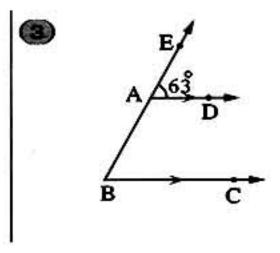


#### 10 In each of the following figures >

If  $\overrightarrow{AD} // \overrightarrow{BC}$ , Find: m ( $\angle ABC$ ), giving reason.







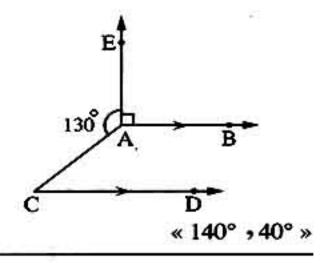
Lesson One

# 11 In the opposite figure:

$$\overrightarrow{AB} / \overrightarrow{CD}$$
,

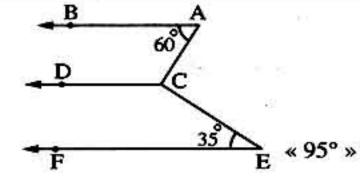
, m (
$$\angle$$
 EAC) = 130° and

$$m (\angle EAB) = 90^{\circ}$$



#### 12 In the opposite figure:

• m (
$$\angle$$
 A) = 60° and m ( $\angle$  E) = 35°

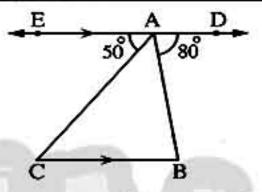


#### 13 In the opposite figure:

$$\overrightarrow{DE} // \overrightarrow{BC} \cdot A \subset \overrightarrow{DE} \cdot m (\angle DAB) = 80^{\circ} \text{ and}$$

$$m (\angle EAC) = 50^{\circ}$$

Find the measures of the angles of  $\triangle$  ABC

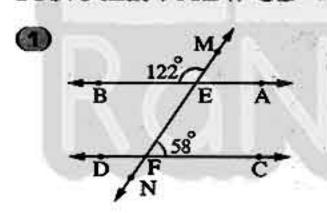


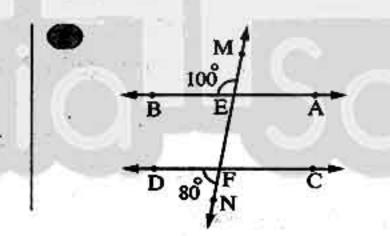
$$\ll$$
 m ( $\angle$  BAC) = 50°  $\Rightarrow$  m ( $\angle$  B) = 80°  $\Rightarrow$  m ( $\angle$  C) = 50°  $\Rightarrow$ 

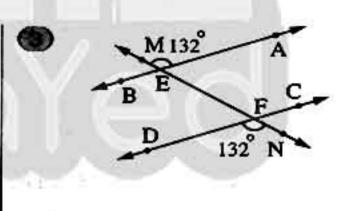
# 14 In each of the following figures,

If MN intersects AB, CD at E and F respectively,

Prove that : AB // CD





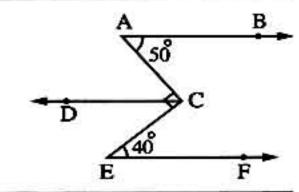


#### 15 🛄 In the opposite figure :

$$\overrightarrow{AB} // \overrightarrow{CD}$$
, m ( $\angle A$ ) = 50°,

$$\angle$$
 ACE is right and m ( $\angle$  E) = 40°

Prove that : AB // EF

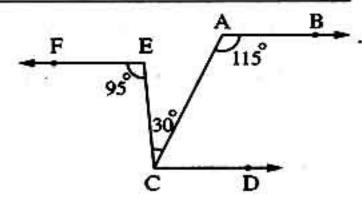


#### 16 In the opposite figure:

$$\overrightarrow{EF} // \overrightarrow{CD}$$
, m ( $\angle CEF$ ) = 95°,

$$m (\angle ACE) = 30^{\circ}, m (BAC) = 115^{\circ}$$

Prove that : AB // EF



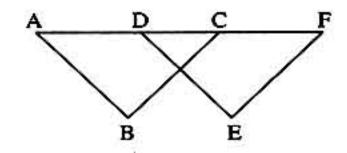
هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى

Unit 3

17 In the opposite figure:

The two triangles are congruent

Prove that : BC // EF



18 In the opposite figure:

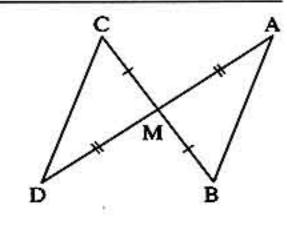
$$\overline{AD} \cap \overline{BC} = \{M\}$$
,

MA = MD and MB = MC

Prove that:

$$(1) AB = CD$$

② AB // CD



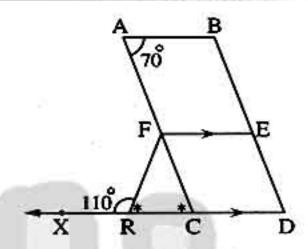
19 In the opposite figure :

 $\overline{FE} // \overline{CD}$ , m ( $\angle FRC$ ) = m (FCR),

 $m (\angle A) = 70^{\circ} \text{ and } m (\angle FRX) = 110^{\circ}$ 

(1) Prove that : CD // AB

(2) Find: m ( $\angle$  AFE) in three ways.



« 110° »

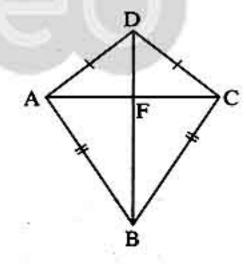
- 20 Prove that :
  - A straight line which is perpendicular to one of two parallel lines is also perpendicular to the other.
  - (2) A straight line that is parallel to one of two parallel lines is also parallel to the other.
- 21 In the opposite figure:

AD = CD and AB = BC

Use the properties of congruent triangles to show that :

① DB bisects ∠ ADC

(2)  $\overline{AC}$  and  $\overline{DB}$  are perpendicular to each other.



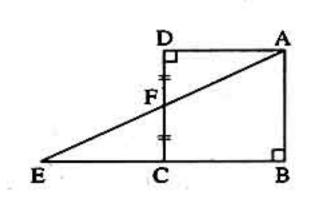
22 In the opposite figure:

ABCD is a square in which F

is the midpoint of  $\overline{CD}$  and

 $\overrightarrow{AF} \cap \overrightarrow{BC} = \{E\}$ 

Prove that : CE = CB



54

مذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

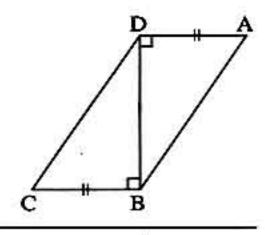
Lesson One

#### 23 In the opposite figure :

AD = BC and  $m (\angle ADB) = m (\angle DBC) = 90^{\circ}$ 

Prove that:

- $\bigcirc$  AB = CD
- (2) AB // CD

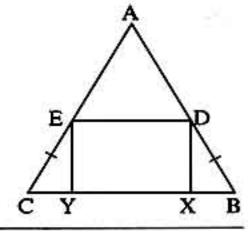


#### 24 In the opposite figure:

EC = DB and

DXYE is a rectangle.

**Prove that:**  $m (\angle ADE) = m (\angle AED)$ 

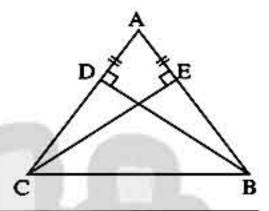


#### 25 In the opposite figure:

 $\overline{BD} \perp \overline{AC}$ ,  $\overline{CE} \perp \overline{AB}$  and

AD = AE

Prove that : BD = CE



#### 26 In the opposite figure:

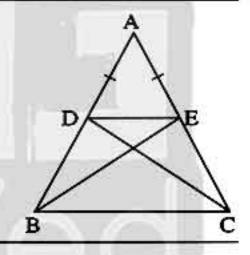
AD = AE and

 $m (\angle ADC) = m (\angle AEB)$ 

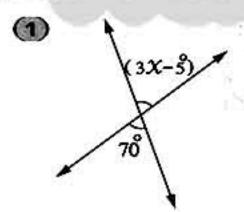
Show that:

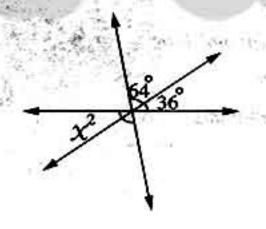
 $\bigcirc$  BE = CD



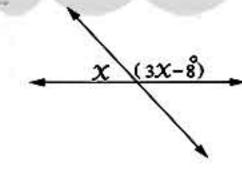


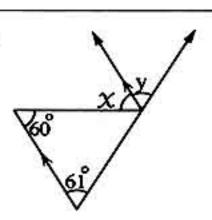
#### 27 Pind the values of X and y in each of the following:



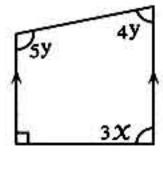


3

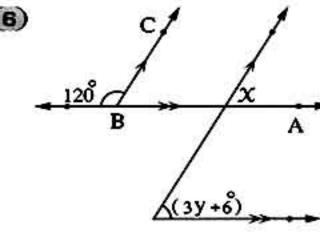




(5)



**(6)** 

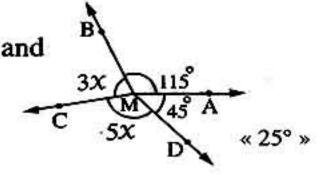


#### [28] In the opposite figure:

 $m (\angle AMB) = 115^{\circ}$ ,  $m (\angle AMD) = 45^{\circ}$ ,  $m (\angle BMC) = 3 \%$  and

 $m (\angle CMD) = 5 x$  What is the value of x?

Are A, M and C collinear? Why?



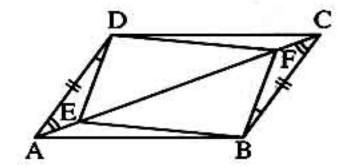


#### For excellent pupils

#### [29] [In the opposite figure:

- (a) Is  $\triangle$  ADE congruent to  $\triangle$  CBF? Give your reason(s).
- (2) Prove that:

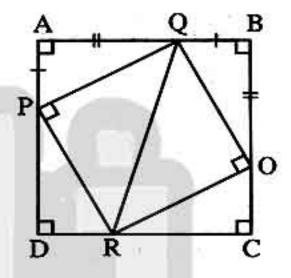
First:  $\triangle DEF \equiv \triangle BFE$  Second:  $\triangle ABE \equiv \triangle CDF$ 



#### 30 In the opposite figure :

- (a) Is  $\triangle$  PAQ congruent to  $\triangle$  QBO? Give your reason (s).
- Show that :

First:  $\triangle PQR \equiv \triangle OQR$  Second:  $\triangle PDR \equiv \triangle RCO$ 





هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلقة

Lesson Two

From the school book

	2000
	-
Exercise	
LACI DISC	

#### On the polygon

LACITISE	4	On me polygon	
Complete the follo	owing:		36.7
The regular pol	ygon is the one in which	n :	
(a) ······		(b) ······	
The sum of mea	asures of the interior ang	gles of the quadrilatera	1 = ······· °
The sum of mea	asures of the interior ang	gles of the pentagon =	°
The sum of mea	asures of the interior ang	gles of the hexagon = .	o
The sum of mea	asures of the interior ang	gles of the heptagon =	
The measure of	the interior angle of the	e regular pentagon = ···	., •
and the measure	of the interior angle of	the regular heptagon =	=°
The sum of mea	asures of the exterior an	gles of the hexagon eq	uals ········ °
If the perimeter	of a regular hexagon is	30 cm., then its side	length = ······ cm.
an the measure	of each interior angle in	it =	-07
If the perimeter	of a regular polygon =	80 cm. and its side len	gth = 10 cm.
then the measur	e of each interior angle	in it = °	
	(b) $(n-2) \times 180^{\circ}$ the interior angle of a r		
(a) $\frac{(n-2)\times 90}{n}$	(b) $\frac{(n-2) \times 180^{\circ}}{2}$	(c) $\frac{(n-2)\times 100}{n}$	(d) $180^{\circ} \times (n-1)$
The measure of	the interior angle of the	e regular polygon of 10	sides equals
(a) 72°	(b) 108°	(c) 144°	(d) 150°
The measure of	the interior angle of a r	egular polygon of 18 s	ides equals
(a) 130°	(b) 140°	(c) 150°	(d) 160°
If the measure of its sides is	of an interior angle of a	regular polygon is 135	o, then the number
(a) 6	(b) 4	(c) 7	(d) 8
The sum of mea	asures of the exterior an	gles of the triangle equ	als ·····
(a) 90°	(b) 180°	(c) 360°	(d) 720°
In the quadrilat	eral ABCD, if m (∠A)	$= 2 \text{ m } (\angle B) = \text{ m } (\angle C)$	C) = 96° ,
then m $(\angle D) =$	**********		

المحاصد ریاضیات لفات اتمارین ۱ (عدادی / تیری ۱۲:۲۱ ا





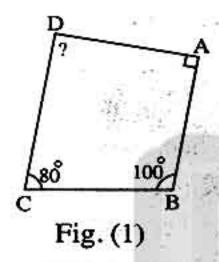
الصف الأول الأعدادي

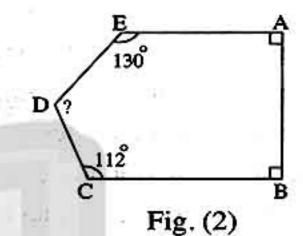
Unit  $oldsymbol{3}$ 

- 3 Find the number of the diagonals of each of the following figures:
  - 1 Triangle.
  - 2 Quadrilateral.
  - (3) Pentagon.

Hint: The number of diagonals of the polygon of n sides =  $\frac{n(n-3)}{2}$ 

4 In each of the following, find the measure of the angle marked by (?):



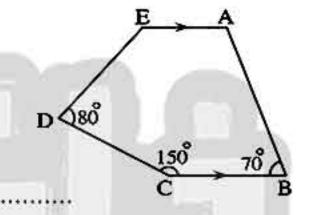


« 90° , 118° »

5 In the opposite figure:

$$\overline{AE}$$
 //  $\overline{BC}$ , m ( $\angle B$ ) = 70°, m ( $\angle C$ ) = 150° and m ( $\angle D$ ) = 80°

Complete the following proof to find m ( $\angle$  E)



Given

R.T.F.

Proof

: AE // BC and ..... is a transversal to them.

$$\therefore$$
 m ( $\angle$  A) + m ( $\angle$  ······) = 180°

(Two interior angles in the same side of the transversal)

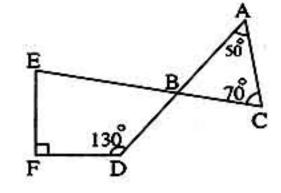
- : ABCDE is a pentagon.
- ... The sum of measures of its interior angles  $= (5 \cdots) \times \cdots = \cdots$

(The req.)

6 In the opposite figure :

$$\overline{CE} \cap \overline{AD} = \{B\}$$
, m ( $\angle A$ ) = 50°  
, m ( $\angle C$ ) = 70°, m ( $\angle D$ ) = 130° and  
m ( $\angle F$ ) = 90°

Complete the following proof to find m (∠ E)



Lesson Two

Given

R.T.F.

Proof

: The sum of measures of the interior angles of the triangle = ...........°

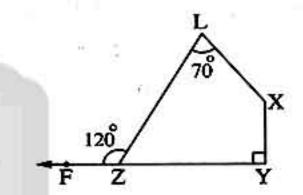
- $\therefore \text{ In } \triangle \text{ ABC} : \text{m} (\angle \text{ ABC}) = 180^{\circ} (\dots + \dots) = \dots = \dots$
- $: CE \cap AD = \{B\}$
- $m (\angle \cdots ) = m (\angle \cdots ) = \cdots (V.O.A.)$
- : The sum of measures of the interior angles of the quadrilateral = ...........°
- $m (\angle E) = \cdots (\cdots + \cdots + \cdots + \cdots) = \cdots$ (The req.)

#### 7 In the opposite figure:

$$F \in \overline{YZ}$$
,  $m (\angle L) = 70^{\circ}$ ,

$$m (\angle Y) = 90^{\circ} \text{ and } m (\angle LZF) = 120^{\circ}$$

Find:  $m (\angle X)$ 



« 140° »

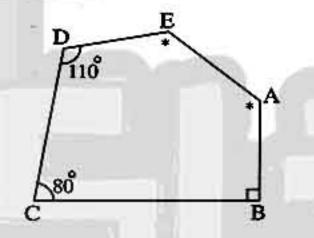
#### 8 In the opposite figure:

If 
$$\overline{AB} \perp \overline{BC}$$
, m ( $\angle C$ ) = 80°,

$$m (\angle D) = 110^{\circ}$$
 and

$$m (\angle A) = m (\angle E)$$

Find:  $m(\angle A)$ 



« 130° »

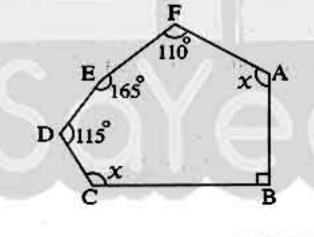
# 9 In the opposite figure :

ABCDEF is a hexagon.

$$m (\angle FAB) = m (\angle DCB)$$

Find:

The value of X

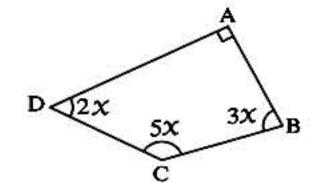


#### 10 In the opposite figure:

ABCD is a quadrilateral

in which:  $m (\angle A) = 90^{\circ}$ 

Find: The value of X



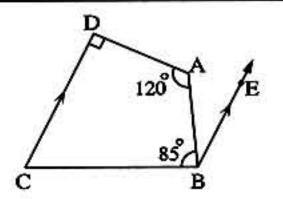
« 27° »

#### [11] In the opposite figure:

$$m (\angle A) = 120^{\circ}, m (\angle D) = 90^{\circ},$$

$$m (\angle ABC) = 85^{\circ} \text{ and } \overline{BE} // \overline{CD}$$

Find: m (∠ ABE)



« 30° »

59

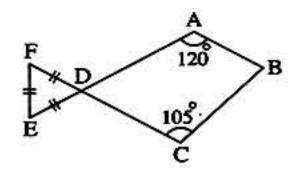
# 12 In the opposite figure:

$$\overline{AE} \cap \overline{CF} = \{D\}$$
,

Δ DEF is an equilateral triangle,

m (
$$\angle$$
 A) = 120° and m ( $\angle$  C) = 105°

Find:  $m (\angle B)$ 



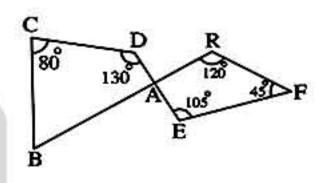
#### 13 In the opposite figure:

$$ED \cap RB = \{A\}, m (\angle F) = 45^{\circ},$$
  
 $m (\angle F) = 120^{\circ}, m (\angle F) = 105^{\circ}$ 

$$m (\angle R) = 120^{\circ}, m (\angle E) = 105^{\circ},$$

 $m (\angle D) = 130^{\circ} \text{ and } m (\angle C) = 80^{\circ}$ 

Find:  $m (\angle B)$ 



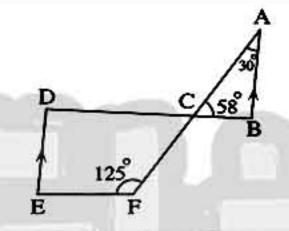
#### [14] In the opposite figure:

$$\overline{BD} \cap \overline{AF} = \{C\}, \overline{AB} / |\overline{ED}|,$$

$$m (\angle A) = 30^{\circ} \text{ and } m (\angle ACB) = 58^{\circ}$$
,

$$m (\angle CFE) = 125^{\circ}$$

Find:  $m (\angle E)$ 



« 85° »

« 75° »

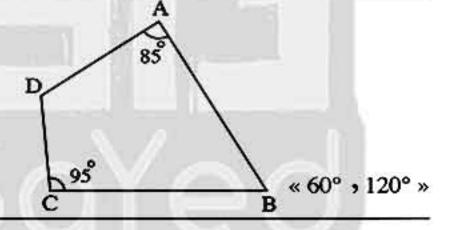
« 60° »

#### 15 In the opposite figure :

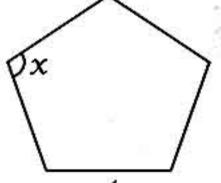
$$m (\angle A) = 85^{\circ} \cdot m (\angle C) = 95^{\circ} \text{ and}$$

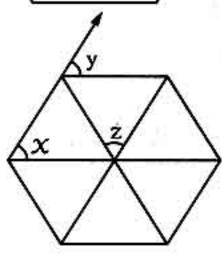
$$m (\angle B) = \frac{1}{2} m (\angle D)$$

Find the measure of each of them.

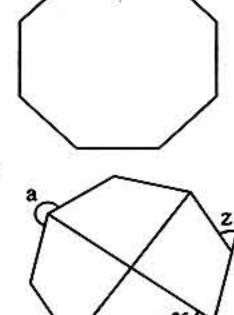


# 16 In each of the following, if the polygon is regular, find the measure of the





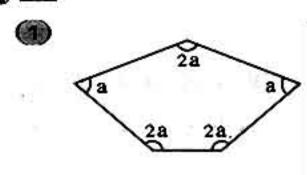


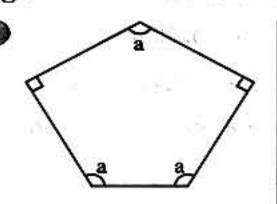


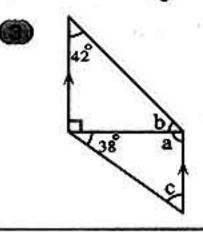
هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمحيولة

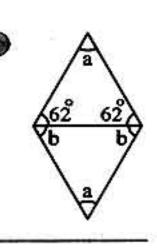
Lesson Two

 $\square$  In each of the following, find the values of the unknown symbols:





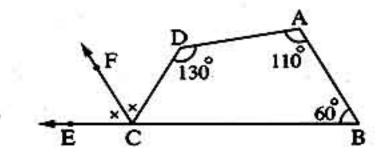




18 In the opposite figure:

m (
$$\angle$$
 A) = 110°, m ( $\angle$  B) = 60°,  
m ( $\angle$  D) = 130°,  $\overrightarrow{CF}$  bisects  $\angle$  DCE and  $C \in \overrightarrow{BE}$ 

Prove that :  $\overrightarrow{CF} // \overrightarrow{AB}$ 

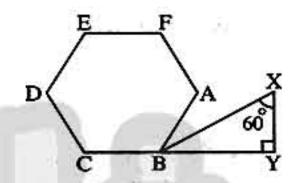


19 In the opposite figure :

ABCDEF is a regular hexagon,

$$Y \in \overrightarrow{CB}$$
,  $\overrightarrow{XY} \perp \overrightarrow{YB}$  and  $m (\angle X) = 60^{\circ}$ 

Prove that: BX bisects ∠ ABY



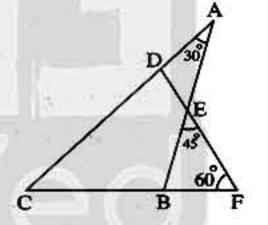
20 In the opposite figure:

ABC is a triangle in which:  $m (\angle A) = 30^{\circ}$ ,

$$\overrightarrow{DE} \cap \overrightarrow{CB} = \{F\}$$
, m ( $\angle F$ ) = 60° and

$$m (\angle BEF) = 45^{\circ}$$

Find the measure of each angle of the figure DEBC



$$\ll$$
 m ( $\angle$  EBC) = 105°, m ( $\angle$  C) = 45°, m ( $\angle$  BED) = 135°, m ( $\angle$  EDC) = 75° »

If the ratio among the measures of the angles of a pentagon is 3:3:2:3:4 find the greatest measure of the angles of this pentagon.

If the measure of the exterior angle of a regular polygon is 30°, how many sides does it have? What is the sum of the measures of its interior angles? « 12, 1800° »

- 23 Is it possible that a regular polygon has an interior angle of measure 100°? Why?
- 24 A polygon of 9 sides. The sum of measures of eight angles of it is 1140°

Find the measure of the remained angle.

« 120° »

« 144° »

(a) Is it possible that this polygon is regular? Explain your answer.

Unit 3

- 25 A polygon has 15 sides:
  - (1) Calculate the sum of the measures of its interior angles.

« 2340° »

(2) If the sum of the measures of five of its exterior angles is 200°, calculate the sum of the measures of the ten interior angles which are not adjacent to the five exterior angles.

« 1640° »



# Life Application

The opposite figure represents a design of the front of one of the house.

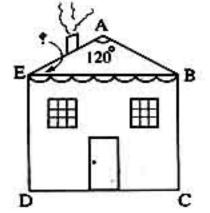
The measure of the angle of the ceiling = 126

The measure of the angle of the ceiling =  $120^{\circ}$ ,

 $\angle ABC \equiv \angle AED$ 

Without using the geometrical tools, find the measure of the angle of ceiling slope on the horizontal line.

« 30° »

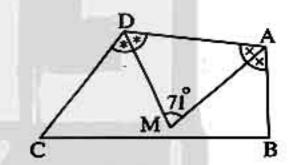


#### For excellent pupils

27 In the opposite figure:

 $\overrightarrow{AM}$  bisects  $\angle$  BAD,  $\overrightarrow{DM}$  bisects  $\angle$  ADC and m ( $\angle$  AMD) = 71°

Prove that:  $m (\angle B) + m (\angle C) = 142^{\circ}$ 

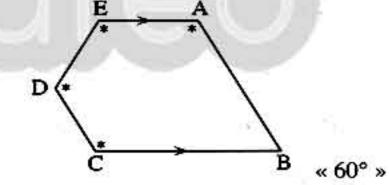


28 In the opposite figure:

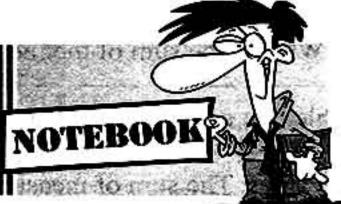
AE // BC,

$$m (\angle A) = m (\angle E) = m (\angle D) = m (\angle C)$$

Find:  $m (\angle B)$ 







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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلوم

Lesson Three

From the school book

#### Exercise On the parallelogram and its properties

#### 1 Complete the following:

- In a parallelogram, every two opposite sides are ......, ......
- (2) In a parallelogram, every two opposite angles are .........
- (3) In a parallelogram, every two consecutive angles are ........
- (4) In a parallelogram, the two diagonals ......
- (5) The quadrilateral in which two sides are parallel is called ..........
- (6) A quadrilateral represents a parallelogram if ...... (write only one answer)
- (B)  $\square$  In the parallelogram XYZL, if m ( $\angle X$ ) =  $\frac{1}{2}$  m ( $\angle Y$ ), then m ( $\angle Y$ ) = .......°

#### 2 In the opposite figure :

ABCD is a parallelogram in which AB = 2 cm. >

AD = 6 cm. and  $m (\angle B) = 105^{\circ}$ 

#### Complete the following:

- 1) BC = ..... cm. , DC = ..... cm.
- ② m (∠ D) = ······° , m (∠ A) = ······° and m (∠ C) = ·····°
- The perimeter of the parallelogram ABCD = ..... cm.

#### 3 In the opposite figure:

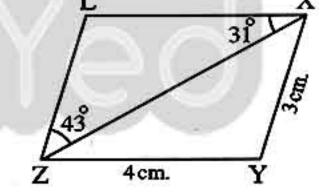
XYZL is a parallelogram in which:

$$XY = 3 \text{ cm.}$$
,  $YZ = 4 \text{ cm.}$ ,  $m (\angle LXZ) = 31^{\circ}$ 

and m ( $\angle$  LZX) = 43°

#### Complete the following proof to find:

( m (∠ Y)



6cm.

#### The perimeter of the parallelogram XYZL

#### Given R.T.F.

Proof

$$\therefore \Delta XLZ \text{ in which } : m (\angle LXZ) = \dots \circ , m (\angle LZX) = \dots \circ$$

The figure XYZL is a parallelogram.

$$\therefore m (\angle Y) = m (\angle \cdots) = \cdots$$
 (First req.)

, The perimeter of the parallelogram XYZL

$$= (XY + \cdots) \times 2 = (3 + \cdots) \times \cdots = \cdots \times \cdots = \cdots \times \cdots = \cdots \times cm.$$
(Second req.)

63

# 4 In the opposite figure :

ABCD is a quadrilateral whose diagonals intersect at M, MA = MC, MB = MD,

m (
$$\angle$$
 AMB) = 110° and m ( $\angle$  MBA) = 25°

Complete the following proof:

- To prove that the figure ABCD is a parallelogram.
- To find m (∠ ACD)

Given

R.T.P.

R.T.F.

Proof

In the figure ABCD:

- : MA = ..... (Given) , MB = ..... (given)
- ... Its diagonals ..... each other.
- ... The figure ABCD is ......

In \( MBA :

- $m (\angle AMB) = \dots m (\angle MBA) = \dots m$
- ∴ m (∠ MAB) = 180° (······°) = ·····°
- , : The figure ABCD is ......
- :. AB // .....
- , : ..... is a transversal to them.
- $\therefore$  m ( $\angle$  ACD) = m ( $\angle$  ·······) = ·······° (······· angles)

(Second req.)

(First req.)

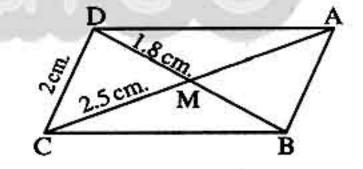
#### 5 In the opposite figure :

ABCD is a parallelogram such that:

$$\overline{AC} \cap \overline{BD} = \{M\} \text{ If } CD = 2 \text{ cm.},$$

MC = 2.5 cm. and MD = 1.8 cm.

Calculate the perimeter of  $\triangle$  AMB



« 6.3 cm. »

#### 6 In the opposite figure:

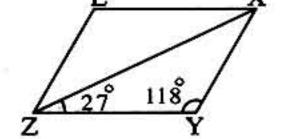
XYZL is a parallelogram in which:

$$m (\angle Y) = 118^{\circ}, m (\angle XZY) = 27^{\circ}$$

Find:

m (∠ YXZ)

- ② m (∠ LZX)
- m (∠ LXZ)
- m (∠ L)



« 35° , 35° , 27° , 118° »

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Lesson Three

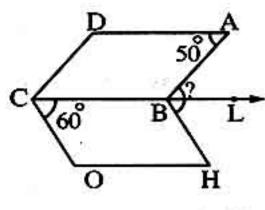
#### 7 In the opposite figure:

ABCD is a parallelogram in which:

m ( $\angle$  BAD) = 50° and BHOC is a parallelogram

in which m ( $\angle$  BCO) = 60°,  $L \in \overrightarrow{CB}$ 

Find with proof: m (∠ ABH)



« 110° »

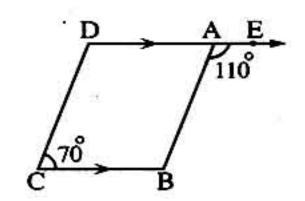
#### 8 In the opposite figure:

ABCD is a quadrilateral in which:

 $\overrightarrow{AD} / / \overrightarrow{BC}, E \in \overrightarrow{DA}, m (\angle BAE) = 110^{\circ}$ 

and m ( $\angle$  DCB) = 70°

Prove that: ABCD is a parallelogram



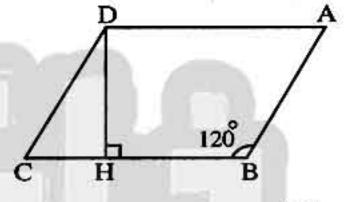
#### 9 In the opposite figure:

ABCD is a parallelogram in which:

m ( $\angle$  B) = 120° and  $\overline{DH} \perp \overline{BC}$ 

where  $\overline{DH} \cap \overline{BC} = \{H\}$ 

Find:  $m (\angle HDC)$ 



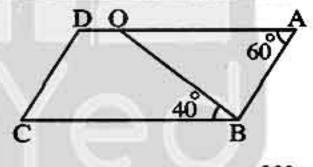
« 30° »

#### 10 In the opposite figure:

ABCD is a parallelogram, in which:

 $m (\angle A) = 60^{\circ}, m (\angle OBC) = 40^{\circ} \text{ where } O \in \overline{AD}$ 

Find: m (∠ ABO)



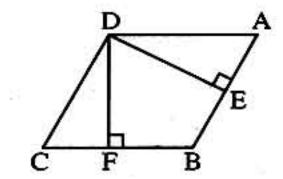
« 80°»

# 11 In the opposite figure:

ABCD is a parallelogram in which:

 $\overline{DE} \perp \overline{AB}$  and  $\overline{DF} \perp \overline{BC}$ 

Prove that:  $m (\angle EDF) = m (\angle A)$ 



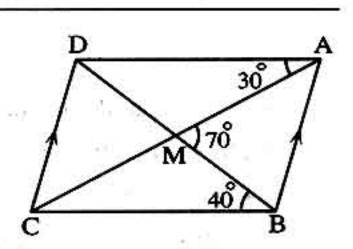
#### 12 In the opposite figure :

ABCD is a quadrilateral where :  $\overline{AC} \cap \overline{BD} = \{M\}$ ,

 $\overline{AB} // \overline{DC}$ , m ( $\angle AMB$ ) = 70°, m ( $\angle MBC$ ) = 40°

and m ( $\angle$  MAD) = 30°

Prove that: ABCD is a parallelogram.

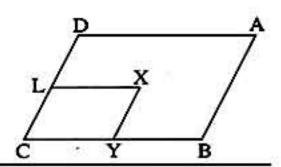


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# 13 In the opposite figure:

If ABCD and XYCL are two parallelograms,

Prove that:  $m (\angle A) = m (\angle X)$ 

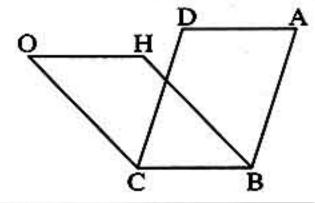


#### 14 In the opposite figure:

Each of ABCD

and HBCO is a parallelogram

Prove that : AD = HO

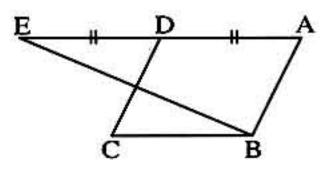


#### 15 In the opposite figure:

ABCD is a parallelogram,

 $E \in \overline{AD}$  in which: AD = DE

Prove that: DC and BE bisect each other.

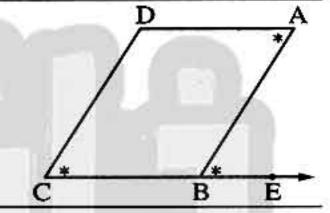


#### 16 In the opposite figure:

ABCD is a quadrilateral,

 $E \in \overline{CB}$  and  $m (\angle BCD) = m (\angle EBA) = m (\angle A)$ 

Prove that : ABCD is a parallelogram.



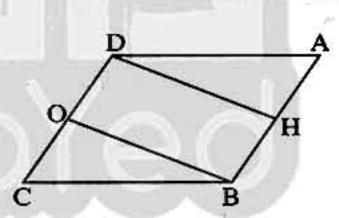
#### 17 In the opposite figure:

ABCD is a parallelogram,

H is the midpoint of AB

and O is the midpoint of DC

Prove that: HBOD is a parallelogram.

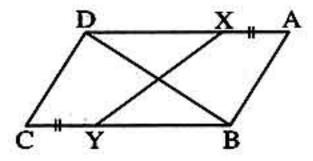


#### [18] In the opposite figure:

ABCD is a parallelogram,

 $X \in \overline{AD}$ ,  $Y \in \overline{BC}$ , if AX = CY

Prove that: XY and BD bisect each other.



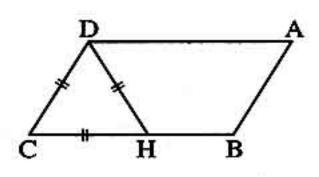
#### 19 In the opposite figure:

ABCD is a parallelogram, H∈BC where:

 $\Delta$  DHC is an equilateral triangle.

1 Prove that : HC = AB

**②** Find:  $m (\angle B)$  and  $m (\angle HDA)$ 



« 120° , 60° »

Lesson Three

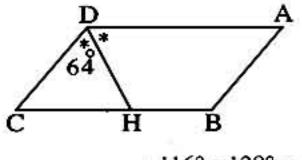
#### [20] In the opposite figure:

ABCD is a parallelogram → H ∈ BC

, DH bisects  $\angle$  ADC and m ( $\angle$  HDC) = 64°

Find: (1) m (\( \subset \text{ DHB} \)

② m (∠ ABC)



« 116° , 128° »

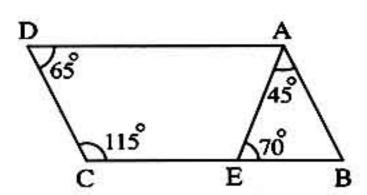
#### In the opposite figure :

 $E \in BC$ ,  $m (\angle BAE) = 45^{\circ}$ ,

 $m (\angle AEB) = 70^{\circ} \cdot m (\angle D) = 65^{\circ}$ 

and m ( $\angle$  C) = 115°

Prove that : ABCD is a parallelogram.



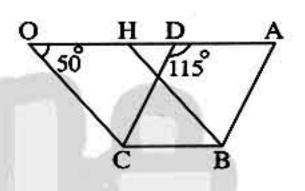
#### [22] In the opposite figure:

ABCD and HBCO are two parallelograms

such that m ( $\angle$  O) = 50°

and m ( $\angle$  ADC) = 115°

Find: m (∠ ABH)



« 65° »

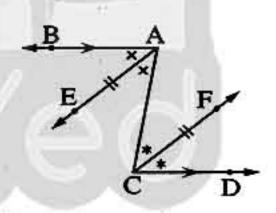
#### 23 In the opposite figure:

AB // CD, AE bisects ∠ BAC,

CF bisects ∠ ACD

If AE = CF,

Prove that: AECF is a parallelogram



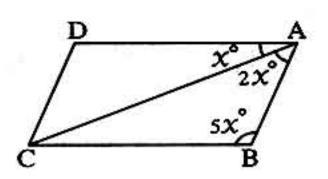
#### 24 In the opposite figure:

ABCD is a parallelogram in which:

 $m (\angle DAC) = X^{\circ}, m (\angle BAC) = 2 X^{\circ}$ 

and m ( $\angle$  ABC) = 5  $X^{\circ}$ 

**Find**:  $m (\angle BCD)$  and  $m (\angle ADC)$  in degrees.



« 67.5° , 112.5° »

#### 25 Choose the correct answer from the given ones:

(1) ABCD is a parallelogram in which:  $m (\angle A) = 50^{\circ}$ , then  $m (\angle C) = \cdots$ 

- (a) 50°
- $(b) 60^{\circ}$

- (c) 130°
- (d) 150°

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- (2) ABCD is a parallelogram in which:  $m (\angle A) + m (\angle C) = 140^{\circ}$ • then m ( $\angle$  B) = .....

  - (a) 70°
- (b) 40°

- (c) 110°
- (d) 220°
- If the lengths of two consecutive sides of a parallelogram are 3 cm. and 5 cm., then its perimeter equals ..... cm.
  - (a) 12
- (b) 14

(c) 16

- (d) 18
- If the perimeter of a parallelogram is 25 cm. and if one of its sides is of length 7 cm., then the consecutive side is of length..... cm.
  - (a) 7

(b) 18

- (c) 12.5
- (d) 5.5

In the opposite figure :

If ABCD is a parallelogram,

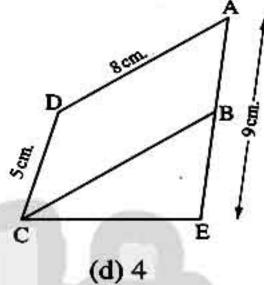
 $E \in \overline{AB}$ , CD = 5 cm., AE = 9 cm.

AD = 8 cm., the perimeter of  $\triangle$  BEC = 18 cm.

- , then the length of EC = ..... cm.
- (a) 8

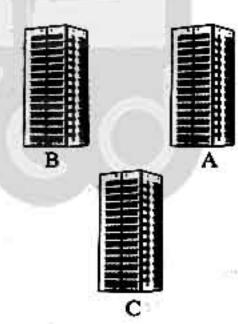
(b) 6

(c) 5





- 26 In one of the new cities, each four buildings are put like A, B, C and D according to the following:
  - The distance between the two buildings A and B equals the distance between the two buildings C and D
  - AB // CD Explain how we can decide the place where the building D will be built.





#### For excellent pupils

ABCD is a parallelogram in which: E is the midpoint of AB,

F is the midpoint of  $\overline{CD}$ , if  $\overline{AF} \cap \overline{DE} = \{M\}$ ,  $\overline{BF} \cap \overline{CE} = \{N\}$ 

Prove that : ED // FB

- FMEN is a parallelogram.
- 28 XYZL is a parallelogram in which :  $m (\angle Y) = 3 m (\angle X)$

Find the measures of the interior angles of XYZL

 $\ll$  m ( $\angle$  Y) = m ( $\angle$  L) = 135° and m ( $\angle$  X) = m ( $\angle$  Z) = 45° »

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Lesson Four

III From the school book

The parallelogical cases of th	Exercise	4	On the special cases of the parallelogra
--	----------	---	--

1	Complet	e the	follo	wing	:

- A parallelogram whose two diagonals are perpendicular is called ...........
- The parallelogram whose two diagonals are ...... is called a rectangle.
- The parallelogram whose two diagonals are equal in length and perpendicular is called .....
- The quadrilateral whose sides are equal in length is called ......
- The quadrilateral whose diagonals bisect each other is called ...........
- The rectangle is a ..... with a right angle.
- The rhombus is a ..... in which its diagonals are perpendicular.
- The square is a ..... with a right angle.
- The rhombus whose two diagonals are equal in length is called .....
- The rectangle in which its two diagonals are perpendicular is called .....
- The rectangle in which its two adjacent sides have the same length is called ......
- If XY // ZL, XY = ZL, then the quadrilateral XYZL is called ......
- If ABCD is a rhombus, then ..... \\_ .....
- The perimeter of the square = ........., The perimeter of the rectangle = ..... and The perimeter of the rhombus = ......
- The rhombus whose perimeter is 42 cm., its side length = ..... cm.

#### Choose the correct answer from the given ones:

- The two diagonals of a rectangle .....
  - (a) are perpendicular.

- (b) are equal in length.
- (c) are perpendicular and equal in length.
- (d) bisect its interior angles.
- The two diagonals of a rhombus are ......
  - (a) perpendicular and are not equal.
  - (b) equal in length and are not perpendicular.
  - (c) perpendicular and equal in length.
  - (d) not equal in length and are not perpendicular.

ا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخ الصف الاول الاعدادي صحيحاكيركي التعليمي كالمعاليمي

 $U_{\rm nit}$  3

- (3) The two diagonals of the square, are ......
  - (a) just perpendicular.
  - (b) just equal in length.
  - (c) perpendicular and equal in length.
  - (d) not equal in length and are not perpendicular.
- (4) If two adjacent sides are equal in length in a parallelogram, then the figure is a ......
  - (a) square.
- (b) rhombus.
- (c) rectangle.
- (d) trapezium.
- (5) If: ABCD is a rectangle in which AC = 5 cm., then: BD = ..... cm.
  - (a) 2.5
- (b) 5
- (c) 10
- (d) 20
- (6) If: ABCD is a square, then: m (\( CAB \) = ......
  - (a) 90°
- (b) 45°
- (c) 60°
- (d) 30°
- (7) If : ABCD is a parallelogram in which m ( $\angle A$ ) = m ( $\angle B$ ), then : ABCD is a  $\cdots$ 
  - (a) rectangle.
- (b) rhombus.
- (c) square.
- (d) trapezium.
- (8) If: ABCD is a rhombus in which m ( $\angle$  ACB) = 32°, then: m ( $\angle$  D) = ......
  - (a) 32°
- (b) 64°
- (c) 116°
- (d) 26°

#### 3 In the opposite figure:

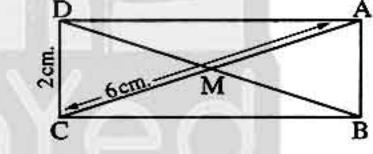
ABCD is a rectangle in which:

$$AC = 6 \text{ cm.} \cdot CD = 2 \text{ cm.}$$

and 
$$\overline{AC} \cap \overline{BD} = \{M\}$$

Complete : (1) AB = ..... cm.

(3) The perimeter of  $\triangle ABM = \cdots cm$ .



#### 4 In the opposite figure:

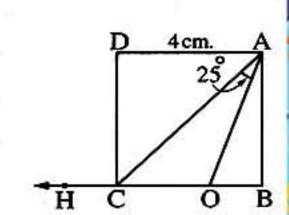
ABCD is a square in which AD = 4 cm.

$$O \subseteq \overline{BC}$$
 such that : m ( $\angle OAC$ ) = 25°

and H∈BC

#### Complete the following:

- (1) The perimeter of the square = ..... cm.
- (2) m (∠ ACH) = ·······°
- ③ m (∠ AOC) = ········

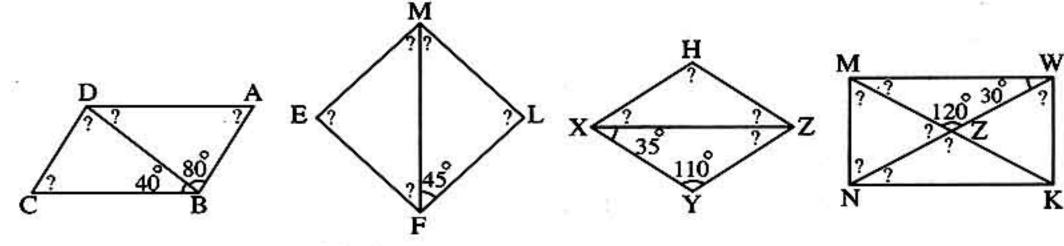


70

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

Lesson Four

5 Find the measures of the angles marked by (?) in each of the following figures:



A parallelogram

Fig. (1)

a square

Fig. (2)

a rhombus

Fig. (3)

a rectangle

Fig. (4)

B

6 In the opposite figure:

ABCD is a square whose side length = 5 cm.,

 $E \in \overline{AC}$  in which m ( $\angle EDC$ ) = 30°

Complete the following proof to find:

- 1 The perimeter of the square ABCD
- (2) m (∠ AED)

Given

R.T.F.

Proof

- : The perimeter of the square = side length × .........
- .. The perimeter of the square ABCD

= ······ × ······ = ····· cm.

, : ABCD is a square, AC is a diagonal

∴ m (∠ ACD) = ·······

In  $\triangle$  DEC:

 $, : E \in \overline{AC}$ 

∴ m (∠ AED) = ······° – ·····° = ·······

(First req.)

(Second req.)

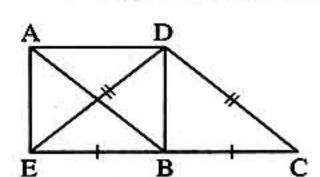
7 In the opposite figure :

ABCD is a parallelogram,

 $E \in \overline{CB}$  where BC = BE, if DE = DC

Complete the following proof to prove that:

The figure AEBD is a rectangle.



هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى إنها المعاصر المعاصر المعاصر

Given

R.T.P.

Proof : ABCD is a parallelogram.

$$, :: EB = \dots, E \in \overrightarrow{CB}$$
 (given)

.. The figure AEBD is a parallelogram.

$$\bullet$$
: DE = ······ (given)

... The two diagonals of the parallelogram AEBD are ......

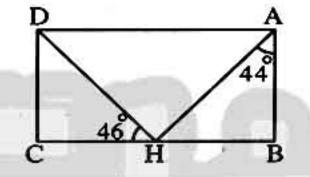
(Q.E.D.)

#### 8 In the opposite figure:

ABCD is a rectangle , H ∈ BC such that :

m (
$$\angle$$
 DHC) = 46° and m ( $\angle$  BAH) = 44°

Calculate: m (∠ AHD)



« 88° »

#### 9 In the opposite figure:

ABCD is a rhombus in which:

$$AC \cap BD = \{M\}$$

H ∈ AB where MH ⊥ AB

If m (
$$\angle$$
 AMH) = 32°,

then calculate the measures of the angles of the rhombus ABCD « 116°, 64°, 116°, 64° »

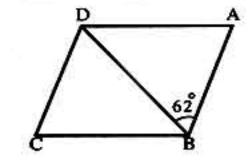
# 10 In the opposite figure

ABCD is a rhombus,

BD is a diagonal in it,

$$m (\angle ABD) = 62^{\circ}$$

Find with proof:  $m (\angle A)$ 



« 56° »

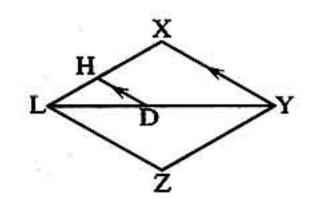
#### 11 In the opposite figure :

XYZL is a rhombus , D∈YL

Draw DH // YX such that :

$$\overrightarrow{DH} \cap \overrightarrow{XL} = \{H\}$$

**Prove that :**  $m (\angle HDL) = m (\angle HLD)$ 





هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى أفايه العمل ال

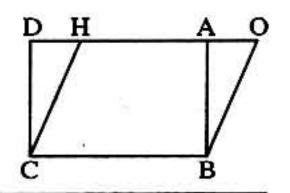
Lesson Four

#### 12 In the opposite figure:

ABCD is a rectangle

and OBCH is a parallelogram

Prove that: DH = AO

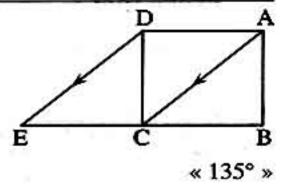


#### 13 In the opposite figure:

ABCD is a square,  $E \in \overrightarrow{BC}$ ,  $\overrightarrow{AC} // \overrightarrow{DE}$ 

Prove that : ACED is a parallelogram.

 $\bigcirc$  Find : m ( $\angle$  ACE)



#### 14 ABCD is a rhombus in which m ( $\angle$ BAC) = 45°

Prove that: ABCD is a square.

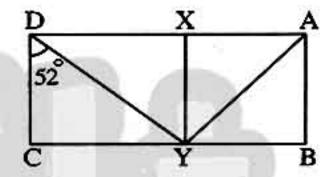
#### 15 In the opposite figure:

ABCD is a rectangle  $X \in \overline{AD}$  and  $Y \in \overline{BC}$  such that:

AXYB is a square.

If m ( $\angle$  YDC) = 52°,

then find with proof: m (∠ AYD)



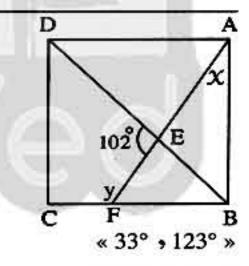
#### « 97° »

#### 16 In the opposite figure:

ABCD is a square,

Find in degrees the value

of each of X and y

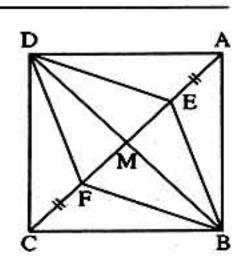


#### 17 In the opposite figure :

ABCD is a square, its diagonals intersect at M,

 $E \in \overline{AC}$ ,  $F \in \overline{AC}$  such that : AE = CF

Prove that: EBFD is a rhombus.



# 18 In the opposite figure :

ABCD is a rectangle,

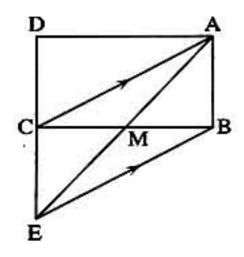
$$\overrightarrow{BE} / / \overrightarrow{AC}, \overrightarrow{BE} \cap \overrightarrow{DC} = \{E\},\$$

$$\overline{BC} \cap \overline{AE} = \{M\}$$

#### Prove that:

$$\bigcirc$$
 DC = CE

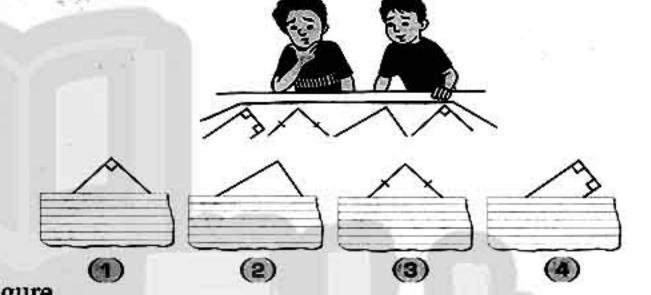
**2** MC = 
$$\frac{1}{2}$$
 AD





# Life Application

19 Eslam drew a parallelogram, a rhombus, a rectangle and a square, then he hid parts of them as in the opposite figure and he asked his friend Bassem to recognize each figure. Help Bassem to name each drawn figure.





#### For excellent pupils

- 20 Use "some" or "all" to get a correct statement :
  - 1) ..... squares are rectangles.
  - (2) ..... quadrilaterals are parallelograms.
  - 3 ..... squares are rhombuses.
  - (4) ..... parallelograms are rectangles.
  - (5) ..... rectangles are parallelograms.
  - (6) .....rhombuses are squares.

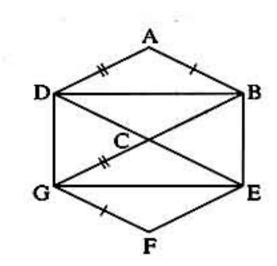
#### 21 In the opposite figure:

ABCD is a parallelogram,

CEFG is a rhombus,

if  $AB = GF \cdot AD = CG$ 

Prove that: BEGD is a rectangle.



هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أ الصف الاول الاعدادي صحيح الصحيح التعليمي

Lesson Five

From the school book

# Exercise

#### On the triangle

1 Com	plete th	e follo	wing :	:
-------	----------	---------	--------	---

- The sum of measures of the inteior angles of a triangle = .....
- (2) The measure of the exterior angle of a triangle is equal to the sum of ..........
- (3) If the measure of an angle in a triangle equals the sum of measures of the other two angles in the triangle, then the triangle is ......
- (4) If the measure of an angle in a triangle is greater than the sum of measures of the other two angles, then the triangle is ......
- (5) In  $\triangle$  ABC: If m ( $\angle$  A) + m ( $\angle$  C) = m ( $\angle$  B), then m ( $\angle$  B) = .....
- (6) In  $\triangle$  ABC: If m ( $\angle$  B) > m ( $\angle$  A) + m ( $\angle$  C), then  $\angle$  B is .......
- (7) It is possible to find a triangle each of its interior angles is of measure .........

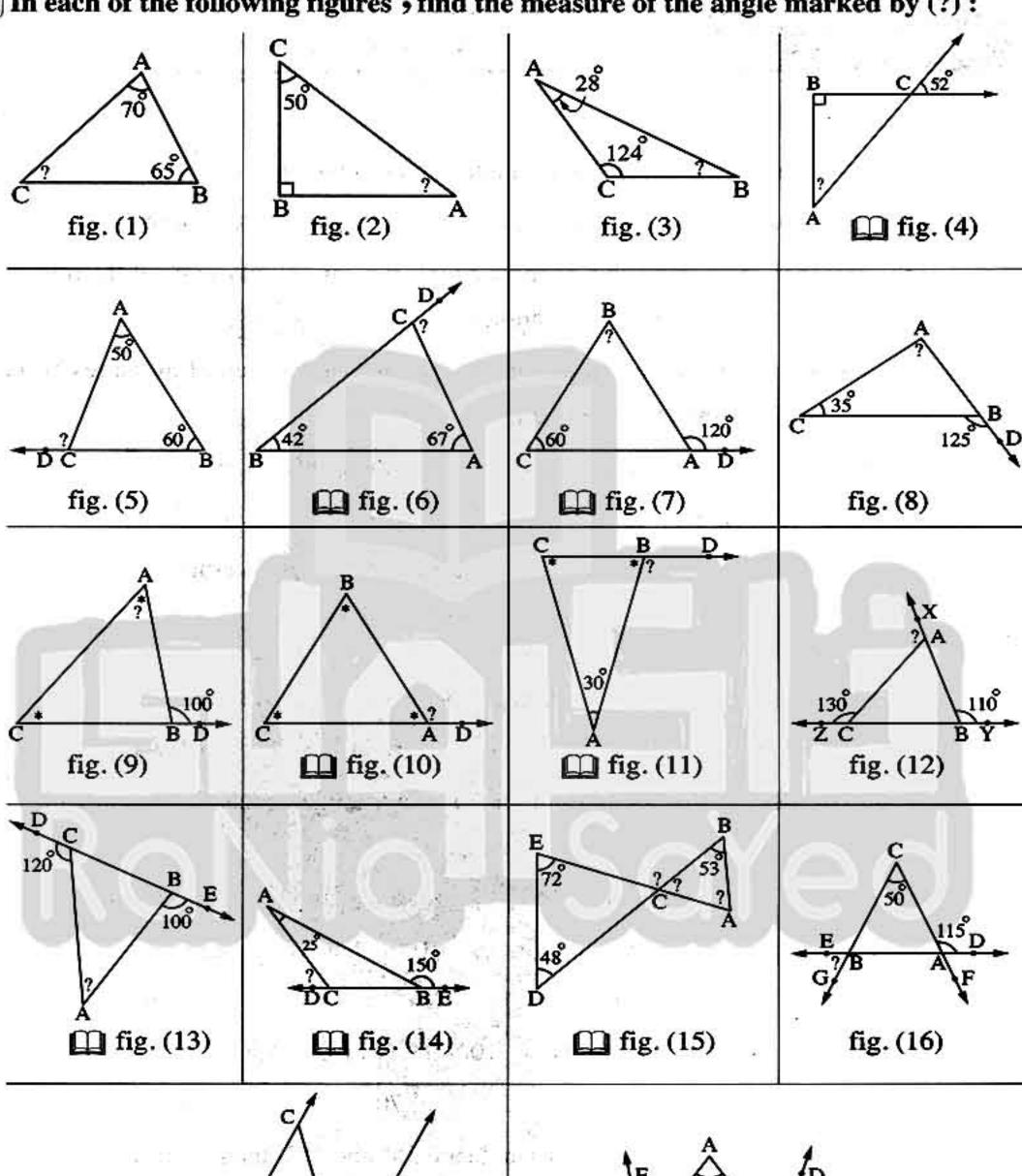
#### 2 Choose the correct answer from the given ones:

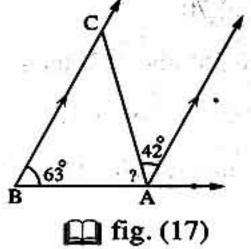
- The triangle contains two ...... angles at least.
  - (a) acute
- (b) obtuse
- (c) right
- (d) reflex
- (2) The sum of measures of the interior angles of a triangle equals the measure of ......... angle.
  - (a) a right
- (b) a straight
- (c) an acute
- (d) a reflex
- (3) In  $\triangle XYZ$ , if: m ( $\triangle X$ ) = 50°, m ( $\triangle Y$ ) = 100°, then: m ( $\triangle Z$ ) = ......
  - (a) 30°
- (b) 50°
- (c) 80°
- (d) 100°
- (a) In  $\triangle$  ABC, if: m ( $\angle$  A) + m ( $\angle$  B) = 110°, then: m ( $\angle$  C) = ......
  - (a) 110°
- (b) 90°
- (c) 70°
- (d) 55°
- (5) If the measures of two angles in a triangle are 35° and 45°, then the triangle is ........
  - (a) acute-angled
- (b) right-angled
- (c) obtuse-angled
- (d) equilateral
- (6) The measure of the exterior angle of the equilateral triangle at any one of its vertices equals .....
  - (a) 60°
- (b) 120°
- (c) 150°
- (d) 30°

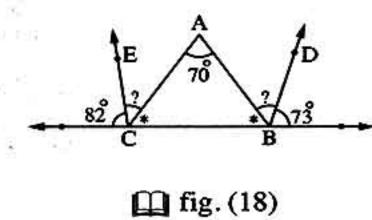
7.5

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى

In each of the following figures , find the measure of the angle marked by (?):







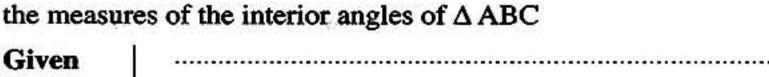
Lesson Five

#### 4 In the opposite figure :

$$\overrightarrow{BD} \cap \overrightarrow{AE} = \{C\}, \overrightarrow{AF} // \overrightarrow{BC}, m (\angle BAF) = 65^{\circ}$$

$$m (\angle DCE) = 55^{\circ}$$

Complete the following proof to find:



R.T.F.

Proof

$$: \overrightarrow{BD} \cap \overrightarrow{AE} = \{C\} \qquad \text{(given)}$$

$$\therefore m (\angle ACB) = m (\angle \dots) = \dots (\dots)$$

$$\cdots$$
  $\overrightarrow{AF}$  //  $\overrightarrow{BC}$  ,  $\overrightarrow{AB}$  is a transversal to them

$$\therefore$$
 m ( $\angle$  FAB) = m ( $\angle$  ·······) = ······· (······ angles)

$$\therefore m (\angle BAC) = \cdots - (\cdots + \cdots) = \cdots$$
 (The req.)

#### 5 In the opposite figure:

$$A \in \overline{DC}$$
,  $\overrightarrow{DE} // \overrightarrow{CB}$ ,  $m (\angle D) = 100^{\circ}$  and

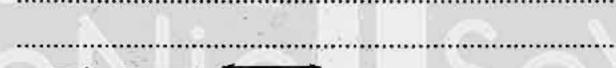
$$m (\angle B) = 40^{\circ}$$

Complete the following proof to find: m (∠ BAD)

Given

R.T.F.

Proof



$$\therefore$$
 m ( $\angle$  D) + m ( $\angle$  C) = ······°

(Two interior angles in the same side of the transversal)

$$\therefore$$
  $\angle$  BAD is an exterior angle of  $\triangle$  .......

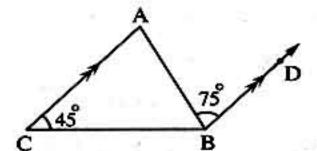
$$\therefore m (\angle BAD) = m (\angle \cdots ) + m (\angle \cdots )$$

#### 6 In the opposite figure:

$$\overrightarrow{BD} // \overrightarrow{CA}$$
, m ( $\angle C$ ) = 45° and

$$m (\angle ABD) = 75^{\circ}$$

Find:  $m (\angle ABC)$ 



100

« 60° »

Unit  $oldsymbol{3}$ 

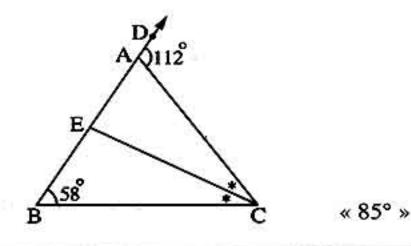
#### 7 In the opposite figure:

ABC is a triangle in which:  $m (\angle B) = 58^{\circ}$ ,

 $E \in \overline{AB}$  such that  $\overline{CE}$  bisects  $\angle ACB$ ,

 $D \in \overrightarrow{BA}$  and m ( $\angle CAD$ ) = 112°

Find:  $m (\angle AEC)$ 



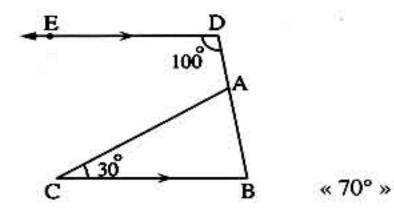
#### B In the opposite figure :

$$\overrightarrow{DE} // \overrightarrow{BC}$$
, m ( $\angle D$ ) = 100°,

 $m (\angle C) = 30^{\circ} \text{ and }$ 

 $A \in \overline{DB}$ 

Find:  $m (\angle BAC)$ 



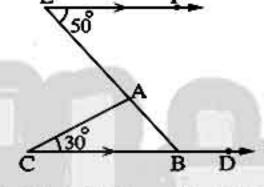
#### 9 In the opposite figure:

 $\overrightarrow{EF} / / \overrightarrow{CD}$ , m ( $\angle E$ ) = 50° and

 $m (\angle C) = 30^{\circ}$ 

Find the measures of the angles

of ∆ ABC and m (∠ ABD)



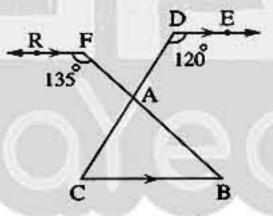
#### $\ll$ m ( $\angle$ ABC) = 50° $\Rightarrow$ m ( $\angle$ BAC) = 100° $\Rightarrow$ m ( $\angle$ ABD) = 130° $\Rightarrow$

# 10 In the opposite figure:

DE // FR // BC,

m ( $\angle$  CDE) = 120° and m ( $\angle$  RFB) = 135°

Calculate the measures of the angles of A ABC



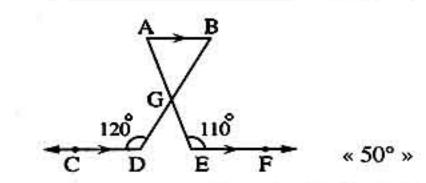
« m (
$$\angle$$
 B) = 45°, m ( $\angle$  C) = 60°, m ( $\angle$  A) = 75° »

# 11 In the opposite figure:

 $\overrightarrow{AB} / \overrightarrow{DC} / \overrightarrow{EF}$ , m ( $\angle E$ ) = 110° and

 $m (\angle D) = 120^{\circ}$ 

Find: m (∠ EGD)



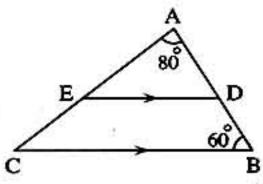
# 12 In the opposite figure:

ABC is a triangle in which:  $m (\angle A) = 80^{\circ}$  and

 $m (\angle B) = 60^{\circ}$ 

 $\overline{DE} // \overline{BC}$  where :  $D \in \overline{AB}$  and  $E \in \overline{AC}$ 

Find: m (∠ AED) and m (∠ DEC)



« 40° , 140° »

78

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلومة

Lesson Five

#### 13 In the opposite figure:

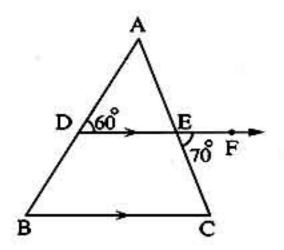
ABC is a triangle,  $m (\angle ADE) = 60^{\circ}$ ,

$$m (\angle FEC) = 70^{\circ}$$
,

$$D \in \overline{AB}$$
,  $\overrightarrow{DF} // \overline{BC}$  and

$$\overline{AC} \cap \overline{DF} = \{E\}$$

Find the measures of the interior angles of  $\triangle$  ABC



$$\ll$$
 m ( $\angle$  C) = 70°  $\Rightarrow$  m ( $\angle$  B) = 60°  $\Rightarrow$  m ( $\angle$  A) = 50°  $\Rightarrow$ 

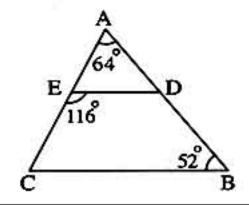
# 14 In the opposite figure:

ABC is a triangle in which  $m (\angle A) = 64^{\circ}$ ,

$$m (\angle B) = 52^{\circ}$$
,

$$m (\angle DEC) = 116^{\circ}, E \in AC \text{ and } D \in AB$$

Prove that : DE // BC



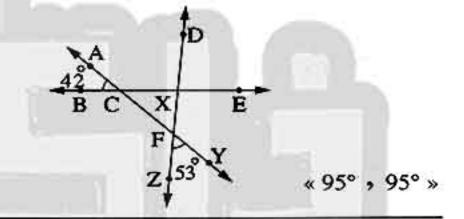
#### 15 🛄 In the opposite figure :

#### Prove that:

 $m (\angle DXE) = 85^{\circ}$ ,

then calculate m (\( \subseteq \text{DXC} \)

and m ( $\angle$  EXF)

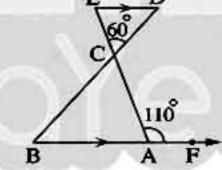


#### 16 In the opposite figure:

ED // BA,  $m (\angle CAF) = 110^{\circ}$ ,

$$\overline{DB} \cap \overline{AE} = \{C\}$$
,

$$m (\angle DCE) = 60^{\circ} \text{ and } F \in \overrightarrow{BA}$$



Find the measures of the angles of the two triangles DCE and ABC

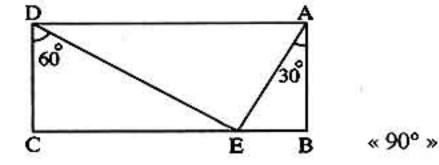
« m (
$$\angle$$
 E) = 70° , m ( $\angle$  D) = 50° , m ( $\angle$  B) = 50° , m ( $\angle$  ACB) = 60° , m ( $\angle$  BAC) = 70° »

#### 17 In the opposite figure:

ABCD is a rectangle , E ∈ BC where :

m (
$$\angle$$
 BAE) = 30° and m ( $\angle$  EDC) = 60°

Find: m (∠ AED)

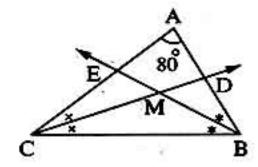


# 18 In the opposite figure:

BM bisects ∠ ABC and CM bisects ∠ ACB

If m (
$$\angle A$$
) = 80°,

find :  $m (\angle EMD)$ 



« 130° »

Unit 3

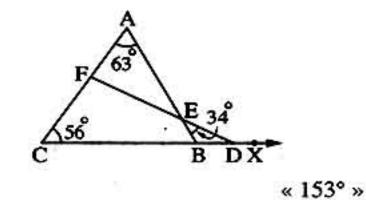
# 19 In the opposite figure:

ABC is a triangle,  $D \in \overrightarrow{CB}$ ,  $X \in \overrightarrow{CB}$ ,

$$m (\angle A) = 63^{\circ}$$
,  $m (\angle C) = 56^{\circ}$  and

$$m (\angle DEB) = 34^{\circ}$$

Find:  $m (\angle EDX)$ 



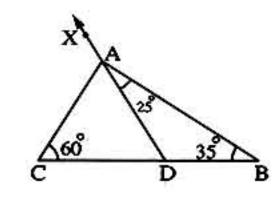
#### 20 In the opposite figure:

ABC is a triangle,  $m (\angle B) = 35^{\circ}$ ,

$$m (\angle C) = 60^{\circ}, m (\angle BAD) = 25^{\circ},$$

 $D \in \overline{BC}$  and  $X \in \overline{DA}$ 

Find:  $m (\angle XAC)$ 



« 120° »

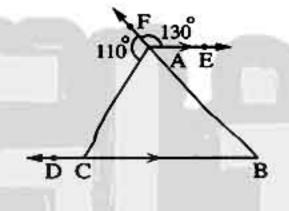
#### 21 In the opposite figure:

ABC is a triangle,  $\overrightarrow{AE} // \overrightarrow{BC}$ ,  $\overrightarrow{D} \in \overrightarrow{BC}$ ,

$$F \in \overline{BA}$$
, m ( $\angle FAE$ ) = 130° and

$$m(\angle FAC) = 110^{\circ}$$

Find: m (∠ ACD)



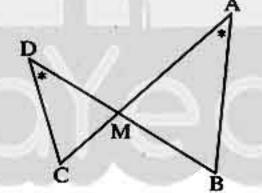
« 120° »

#### 22 In the opposite figure:

 $\overline{AC} \cap \overline{BD} = \{M\}$  and

$$m (\angle A) = m (\angle D)$$

Prove that :  $m (\angle B) = m (\angle C)$ 

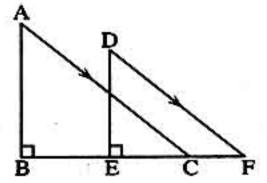


#### 23 In the opposite figure :

The points F, C, E and B are collinear,

$$m (\angle B) = m (\angle DEC) = 90^{\circ} \text{ and } \overline{AC} // \overline{DF}$$

**Prove that:**  $m (\angle A) = m (\angle D)$ 



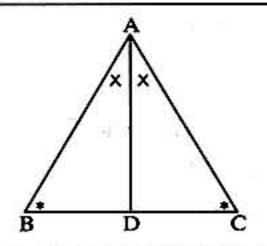
#### 24 In the opposite figure :

ABC is a triangle,

$$m (\angle B) = m (\angle C)$$
 and

AD is the bisector of  $\angle A$ 

Prove that : AB = AC



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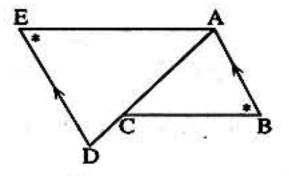
هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

Lesson Five

#### 25 In the opposite figure:

$$\overline{AB} /\!/ \overline{ED}$$
 and

$$m (\angle ABC) = m (\angle AED)$$



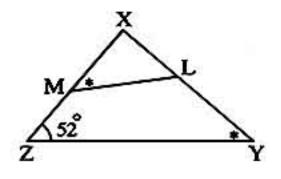
#### 26 In the opposite figure:

XYZ is a triangle in which m (
$$\angle Z$$
) = 52°,

$$L \in \overline{XY}$$
 and  $M \in \overline{XZ}$  such that:

$$m (\angle Y) = m (\angle XML)$$

Find: 
$$m (\angle XLM)$$



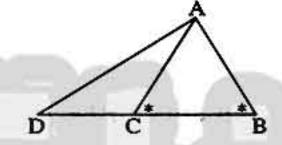
#### « 52° »

#### 27 In the opposite figure:

#### ABC is a triangle in which:

$$m (\angle B) = m (\angle ACB)$$
 and  $D \in BC$ 

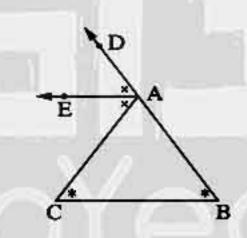
Prove that: 
$$m (\angle B) > m (\angle D)$$



#### 28 In the opposite figure:

#### ABC is a triangle in which:

$$m (\angle B) = m (\angle C) , D \in \overline{BA}$$
 and



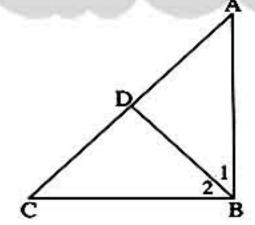
#### 29 In the opposite figure :

#### ABC is a triangle in which: $D \in \overline{AC}$ ,

$$m (\angle 1) = m (\angle A)$$
 and

$$m (\angle 2) = m (\angle C)$$

#### Prove that: ∠ ABC is a right angle.



Unit 3



#### For excellent pupils

30 ABC is a triangle in which:  $m (\angle A) = 2 m (\angle C)$  and  $m (\angle B) = 4 m (\angle C)$ 

**Prove that:**  $\angle$  B is an obtuse angle.

31 ABC is a triangle in which:  $m (\angle C) = 28^{\circ}$ ,  $m (\angle A) = 4x^{\circ}$ 

$$\mathbf{m} (\angle \mathbf{B}) = (2 X + 2)^{\circ}$$

Find:  $m (\angle A)$  and  $m (\angle B)$ 

« 100° , 52° »

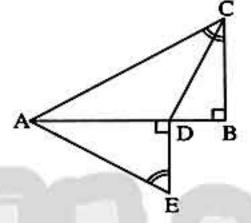
32 In the opposite figure:

ABC is a triangle in which : D ∈ AB

$$m (\angle B) = 90^{\circ}$$
,  $m (\angle ADE) = 90^{\circ}$  and

$$m (\angle ACB) = m (\angle E)$$

Prove that :  $m (\angle BDC) > m (\angle DAE)$ 



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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

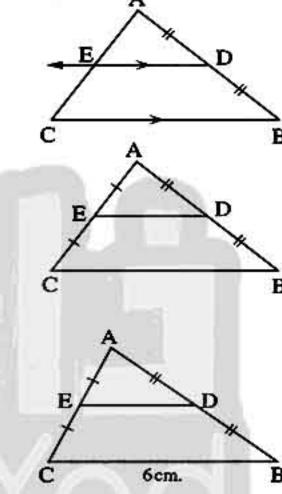
Lesson Six

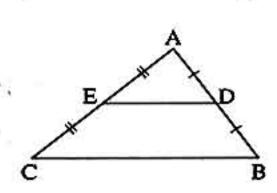
From the school book

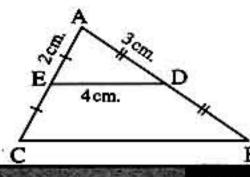
#### On theorem 2 and its corollary, and theorem 3 Exercise

#### 1 Complete the following:

- The ray drawn from the midpoint of a side of a triangle parallel to another side
- (2) The line segment joining the midpoints of two sides of a triangle is ...... the third side.
- (3) The length of the line segment joining the midpoints of two sides of a triangle equals .....
- In the opposite figure : If D is the midpoint of AB, DE // BC
  - then: ..... is the midpoint of .....
- (5) In the opposite figure:
  - If D and E are the midpoints of AB and AC respectively
- , then: ...... // ......
- (B) In the opposite figure :
  - : D and E are the midpoints of AB and AC respectively
  - , BC = 6 cm.
  - ∴ DE = ..... cm
- In the opposite figure :
  - If:  $m(\angle B) = 90^{\circ}$ , D and E are the midpoints of AB and AC respectively
  - then :  $m (\angle ADE) = \cdots$
- (B) In the opposite figure:
  - If: D and E are the midpoints of AB and AC respectively
  - , and the perimeter of the triangle ABC = 24 cm.
  - , then the perimeter of the triangle ADE = ..... cm.
- In the opposite figure :
  - : D and E are the midpoints of AB and AC respectively
  - , AD = 3 cm., AE = 2 cm. and DE = 4 cm.
  - ... The perimeter of the figure DBCE = ..... cm.





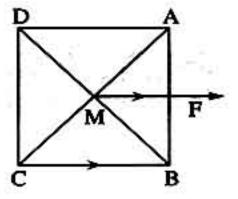


# Unit 3

#### In the opposite figure :

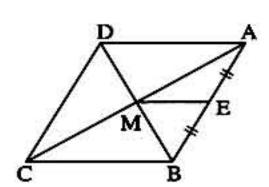
If the perimeter of the square ABCD = 20 cm.

- $, \overrightarrow{MF} // \overrightarrow{CB} \text{ where } F \in \overline{AB}$
- then :  $AF = \cdots cm$ .



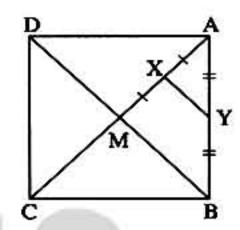
#### In the opposite figure :

- : The perimeter of the rhombus ABCD = 24 cm., E is the midpoint of  $\overline{AB}$
- ∴ ME = ..... cm.



#### • In the opposite figure:

- $\therefore$  ABCD is a square, x and Y are the midpoints of  $\overline{AM}$  and  $\overline{AB}$  respectively and  $\overline{AC} = 12$  cm.
- $\therefore XY = \cdots cm., m (\angle AYX) = \cdots$

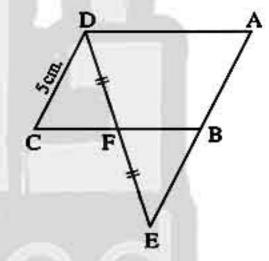


#### 2 In the opposite figure:

ABCD is a parallelogram, DC = 5 cm.

$$, F \in \overrightarrow{BC}, \overrightarrow{DF} \cap \overrightarrow{AB} = \{E\},\$$

if: DF = FE



# Complete the following proof to find the length of $\overline{BE}$

Given |

R.T.F.

Proof :

: ABCD is a .....

, In  $\triangle$  AED :

: F is the midpoint of ......, BF // ....

.. B is the midpoint of .....

∴ AB = .....

, : AB = ..... cm. (Properties of .....)

∴ BE = ..... cm. (The req.)

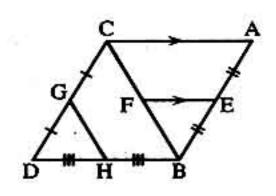
# 3 In the opposite figure :

ABC is a triangle in which CA = CB,

E is the midpoint of AB,  $\overline{EF} // \overline{AC}$ ,

H and G are the two midpoints of BD and CD respectively.

Complete the following proof to prove that : EF = GH



Given

R.T.P.

**Proof** 

In  $\triangle$  ABC:

.. F is the midpoint of .....

 $\therefore EF = \frac{1}{2} \dots$ 

, In A BDC:

: H is the midpoint of .....

, ..... is the midpoint of CD

 $\therefore GH = \frac{1}{2} \dots$ 

, ∵ CA = .....

∴ EF = .....

(Q.E.D.)

# 4 In the opposite figure:

 $AE = EB \cdot EX // BC \cdot XY // CD$ 

and AD = 6 cm.

Find the length of: AY

« 3 cm. »

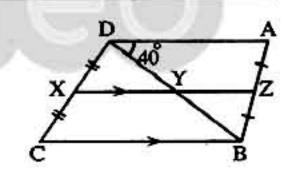
# 5 In the opposite figure :

X is the midpoint of CD

, Z is the midpoint of AB

 $\sqrt{XY} / / \overline{CB}$ , m ( $\angle ADB$ ) = 40°

Find:  $m (\angle ZYB)$ 



« 40° »

# 6 In the opposite figure:

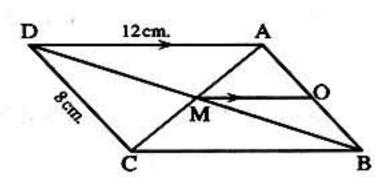
ABCD is a parallelogram  $\rightarrow \overline{AC} \cap \overline{BD} = \{M\}$ 

Draw MO // AD to cut AB at O

If: AD = 12 cm. and DC = 8 cm.

, then find: The perimeter of ABCD

The length of AO

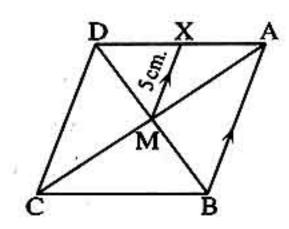


« 40 cm. • 4 cm. »

# 7 In the opposite figure :

ABCD is a parallelogram, its diagonals intersect at M Draw  $\overrightarrow{MX} // \overrightarrow{BA}$  to intersect  $\overrightarrow{AD}$  at X

- (1) Prove that: X is the midpoint of AD
- (2) If MX = 5 cm. , then find the length of CD



« 10 cm. »

# B ABCD is a parallelogram, its diagonals intersect at M, ME // BA and cuts AD at E Prove that : $ME = \frac{1}{2}DC$

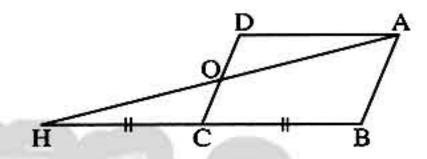
# 9 In the opposite figure:

ABCD is a parallelogram,

$$BC = CH , H \in BC$$

Draw AH to cut DC at O

Prove that : AO = OH

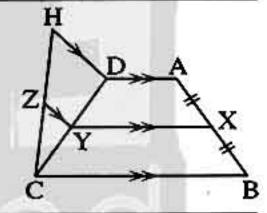


### 10 In the opposite figure :

ABCD is a trapezium, AD // BC, X is the midpoint of AB

If AD // XY where Y EDC, YZ // DH

Prove that : CZ = ZH

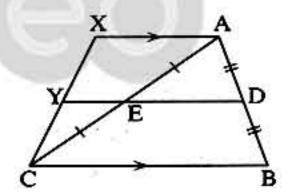


# 11 📖 In the opposite figure :

AD = DB, AE = EC,

 $\overrightarrow{AX} / \overrightarrow{BC}, \overrightarrow{DE} \cap \overrightarrow{XC} = \{Y\}$ 

Prove that: Y is the midpoint of XC



10cm.

# 12 In the opposite figure :

ABCD is a quadrilateral in which:

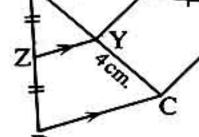
X and Z are the midpoints of  $\overline{AB}$ 

and  $\overline{AD}$  respectively and  $Y \in \overline{AC}$  such that :

YZ // CD and YC = 4 cm.

If BC = 6 cm. and AB = 10 cm., then

find: (1) The length of AY



« 4 cm. , 12 cm. »

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

(2) The perimeter of Δ AXY

Lesson Six

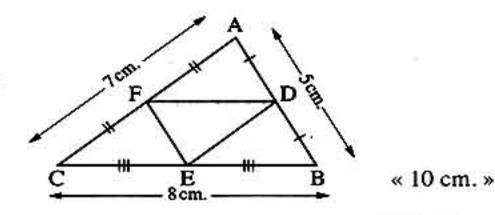
# 13 🕮 In the opposite figure :

$$AB = 5 \text{ cm.}, BC = 8 \text{ cm.},$$

AC = 7 cm., D, E and F are the midpoints of

AB, BC and CA respectively.

Calculate the perimeter of :  $\Delta$  DEF



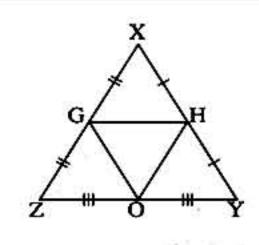
# 14 In the opposite figure:

XYZ is a triangle in which:

H, O and G are the midpoints of XY, YZ and ZX respectively.

If the perimeter of  $\Delta$  HOG is 18 cm.,

then find the perimeter of :  $\Delta XYZ$ 



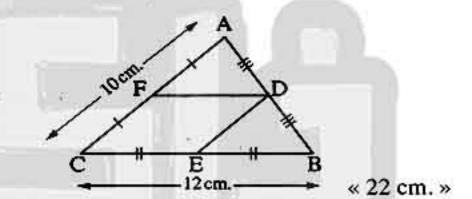
« 36 cm. »

# ABC is a triangle, if X, Y and Z are the midpoints of AB, BC and AC respectively. Prove that: the perimeter of $\Delta XYZ = \frac{1}{2}$ that of $\Delta ABC$

# 16 In the opposite figure:

ABC is a triangle in which D, E and F are the midpoints of AB, BC and CA respectively, BC = 12 cm., AC = 10 cm.

Find the perimeter of the figure DECF



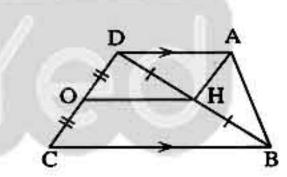
# 17 In the opposite figure:

 $\overline{AD} // \overline{BC}, AD = \frac{1}{2} BC,$ 

H is the midpoint of BD,

O is the midpoint of CD

Prove that: AHOD is a parallelogram.

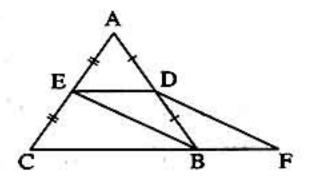


# 18 In the opposite figure :

D and E are the midpoints of AB and AC respectively,

 $F \in \overrightarrow{CB}$  where  $BF = \frac{1}{2}BC$ 

Prove that: BEDF is a parallelogram.



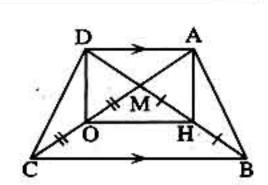
# 19 In the opposite figure:

ABCD is a trapezium in which AD // BC

and  $AD = \frac{1}{2} BC$  and  $\overline{AC} \cap \overline{DB} = \{M\}$ 

Let H and O are the midpoints of MB and MC respectively.

Prove that: AHOD is a parallelogram.





هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى



# [20] [III] In the opposite figure:

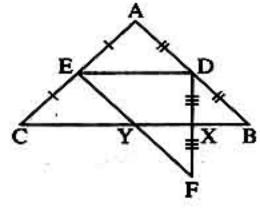
D is the midpoint of  $\overline{AB}$ ,

E is the midpoint of  $\overline{AC}$ ,

$$\overline{DF} \cap \overline{BC} = \{X\}, DX = XF,$$

BC = 12 cm.

Find the length of :  $\overline{XY}$ 



« 3 cm. »

# 21 In the opposite figure:

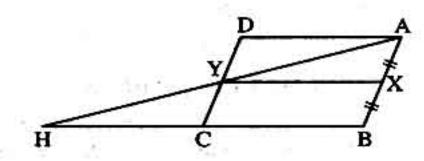
ABCD is a parallelogram,

X is the midpoint of AB

Draw  $\overrightarrow{XY} // \overrightarrow{BC}$  to cut  $\overrightarrow{DC}$  at Y

Draw AY to cut BC at H

Prove that: C is the midpoint of BH



# 22 In the opposite figure:

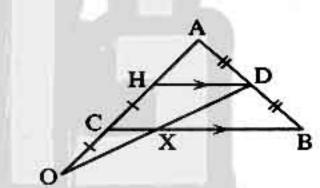
ABC is a triangle, D is the midpoint of AB,

 $\overrightarrow{DH} / / \overrightarrow{BC} , O \subseteq \overrightarrow{AC}$  such that HC = CO

Prove that :  $CO = \frac{1}{3} AO$ 

If we draw DO to cut BC at X, then

prove that : OX = XD



# 23 In the opposite figure:

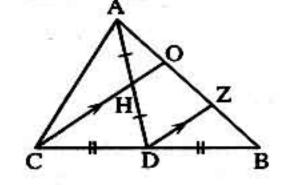
ABC is a triangle , D is the midpoint of BC

and H is the midpoint of AD

Draw CH to cut AB at O,

then draw  $\overline{DZ} // \overline{CO}$  to cut  $\overline{AB}$  at Z

Prove that : AO = OZ = ZB



# ABCD is a parallelogram. M is the intersection point of its diagonals,

draw CE // BD to cut AB at E and AD at F

Prove that :  $\bigcirc$  AB = BE

AD = DF

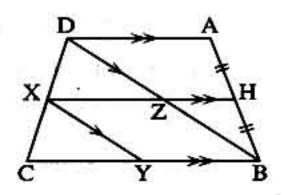
Lesson Six

# 25 In the opposite figure:

ABCD is a trapezium in which  $\overline{AD} /\!/ \overline{BC}$ Let H be the midpoint of  $\overline{AB}$ ,

 $\overline{HX} // \overline{BC}$  and  $\overline{XY} // \overline{DB}$ 

**Prove that:** Y is the midpoint of  $\overline{BC}$ 



# ABCD is a trapezium in which $\overrightarrow{AD}$ // $\overrightarrow{BC}$ , E is the midpoint of $\overrightarrow{AB}$ , draw $\overrightarrow{EX}$ // $\overrightarrow{BC}$ to cut $\overrightarrow{DB}$ at X, $\overrightarrow{DC}$ at Y, and draw $\overrightarrow{YZ}$ // $\overrightarrow{DB}$ to cut $\overrightarrow{BC}$ at Z

Prove that : XD = YZ

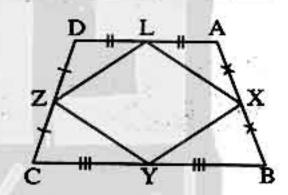
ABC is a triangle in which AB = 9 cm., AC = 8 cm.,  $D \in \overline{AB}$ ,  $E \in \overline{AB}$  such that AD = DE = EB and  $\overrightarrow{DX}$ ,  $\overrightarrow{EY}$  are drawn parallel to  $\overrightarrow{BC}$  and cutting  $\overline{AC}$  at X and Y respectively, where DX = 4 cm.

Calculate: the perimeter of the shape DEYX

# 28 In the opposite figure:

ABCD is a quadrilateral in which  $X \cdot Y \cdot Z$  and L are the midpoints of  $\overline{AB} \cdot \overline{BC} \cdot \overline{CD}$  and  $\overline{DA}$  respectively.

Prove that: XYZL is a parallelogram.

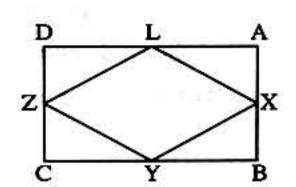


# ABC is a triangle in which AB = AC $\cdot$ X $\cdot$ Y and Z are the midpoints of $\overline{AB}$ $\cdot$ $\overline{BC}$ and $\overline{CA}$ respectively.

Prove that: AXYZ is a rhombus.

# 30 In the opposite figure :

ABCD is a rectangle and  $X \cdot Y \cdot Z$  and L are the midpoints of  $\overline{AB} \cdot \overline{BC} \cdot \overline{CD}$  and  $\overline{DA}$  respectively.



# Prove that:

- XYZL is a rhombus.
- The perimeter of the rhombus = 2 BD

المحاصع ریانشیان لفات اقبارین ۱۱ اِعدادی / تین ۱۲:۲۱

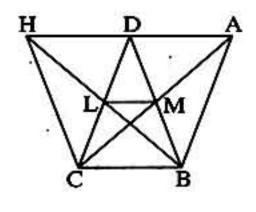
31 In the opposite figure:

ABCD and DBCH are two parallelograms having a common base BC and on one side of BC

Let  $AC \cap BD = \{M\}$  and  $DC \cap BH = \{L\}$ 

Prove that: (1) ML // BC

**2** ML =  $\frac{1}{4}$  AH



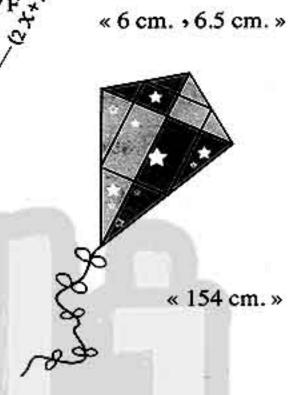
32 Connected with algebra:

In the opposite figure:



Sara wants to design a kite whose two diagonals are 64 cm. and 90 cm.

She want to put a stripe to decorate the kite such that the stripe joins between the midpoints of the sides of the kite. How long is the stripe?



# For excellent pupils

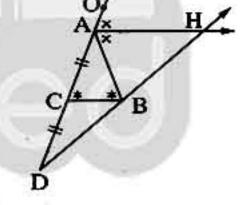
34 In the opposite figure:

ABC is a triangle in which:  $m (\angle ABC) = m (\angle ACB)$ 

 $D \in AC$  such that AC = CD and  $O \in CA$ 

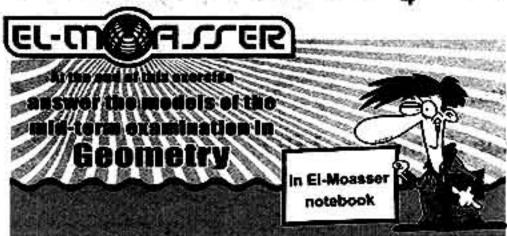
Let AH bisects  $\angle$  BAO such that :  $\overrightarrow{AH} \cap \overrightarrow{DB} = \{H\}$ 

Prove that : DB = BH



BE ABCD is a quadrilateral in which  $\overline{AC} \perp \overline{BD}$  and X, Y, Z and L are the midpoints of  $\overline{AB}$ ,  $\overline{BC}$ ,  $\overline{CD}$  and  $\overline{DA}$  respectively.

**Prove that:** XYZL is a rectangle whose area equals  $\frac{1}{4}$  AC × BD



90

خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

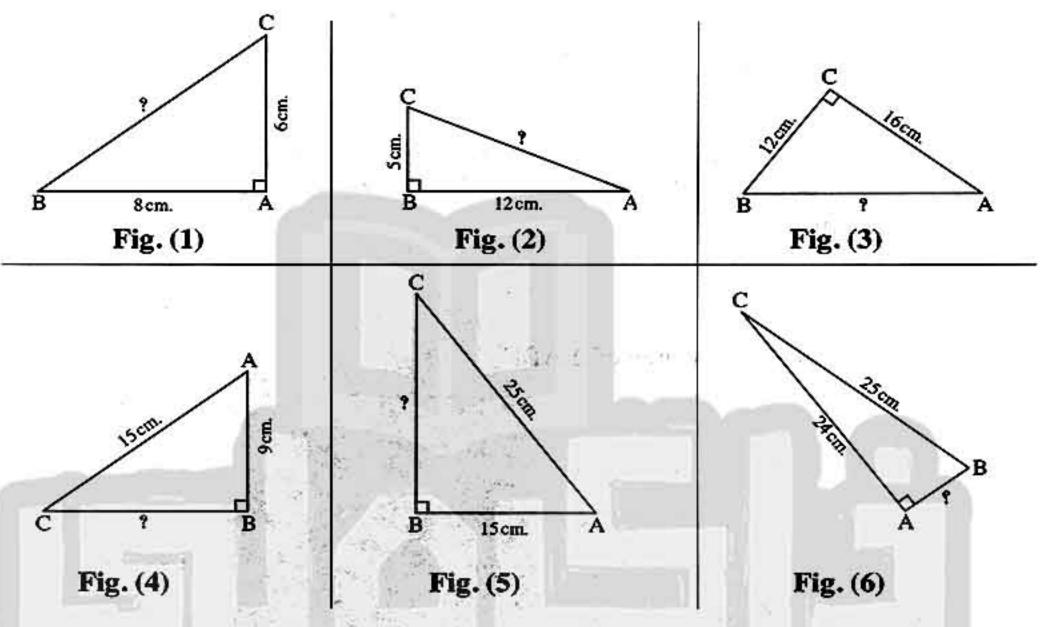
Lesson Seven

From the school book

# Exercise

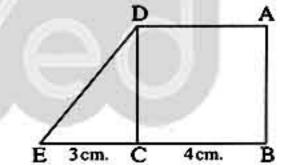
# On Pythagoras' theorem

In each of the following figures, find the length of the unknown side:



# 2 In the opposite figure :

ABCD is a square whose side length = 4 cm. and  $E \in \overline{BC}$  where CE = 3 cm.



# Complete the following proof to find the length of DE

- : ABCD is a square
- $\therefore$  DC = ··········cm.  $\Rightarrow$  m ( $\angle$  DCB) = ········°
- :. In  $\triangle$  DCE:  $(DE)^2 = (\dots)^2 + (CE)^2 = (\dots)^2 + (3)^2$
- ∴ DE = ..... cm. (The req.)

# Unit 3

# In the opposite figure:

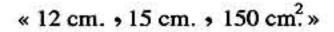
 $\overline{AD} \perp \overline{BC}$ , BD = 9 cm.,

DC = 16 cm. and AC = 20 cm.

#### Find:

- (AD
- The area of ∆ ABC

AB



# 4 In the opposite figure:

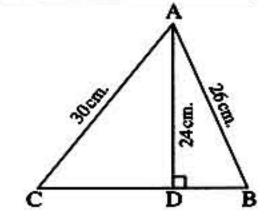
ABC is a triangle and AD \( \text{LBC} \)

If AD = 24 cm.

AB = 26 cm.

and AC = 30 cm.

find BC and calculate the area of  $\triangle$  ABC



« 28 cm. , 336 cm<sup>2</sup>.»

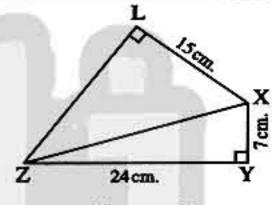
# 5 In the opposite figure:

XYZL is a quadrilateral in which:

$$m (\angle XYZ) = m (\angle XLZ) = 90^{\circ}$$
,

XY = 7 cm., YZ = 24 cm. and XL = 15 cm.

Find the length of each of: XZ and ZL



« 25 cm. , 20 cm. »

12cm. B

# 6 In the opposite figure:

 $m (\angle B) = m (\angle ACD) = 90^{\circ}$ 

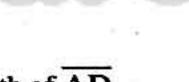
AB = 9 cm. BC = 12 cm.

and DC = 20 cm.

#### Find:

The length of AC

The perimeter of the figure ABCD



The length of AD

The area of the figure ABCD

« 15 cm. , 25 cm. , 66 cm. , 204 cm<sup>2</sup>.»

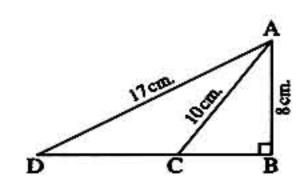
# 7 In the opposite figure :

 $\Delta$  ABD is a right-angled triangle at B

AB = 8 cm. AD = 17 cm.

and  $C \subseteq \overline{BD}$  such that AC = 10 cm.

Find the length of each of : CB , BD and CD



«6 cm. , 15 cm. , 9 cm.»

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى في المعلمات



Lesson Seven

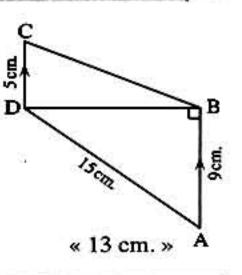
# B In the opposite figure:

$$m (\angle ABD) = 90^{\circ} , \overline{BA} // \overline{CD}$$

$$AB = 9 \text{ cm.}$$
  $AD = 15 \text{ cm.}$ 

and DC = 5 cm.

Calculate the length of : BC



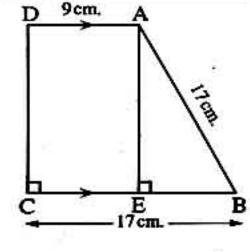
# 9 In the opposite figure :

ABCD is a trapezium, AD // BC

$$, m (\angle DCB) = 90^{\circ}, \overline{AE} \perp \overline{BC}$$

If: 
$$AB = BC = 17$$
 cm. and  $AD = 9$  cm.

, find the length of DC and calculate the area of the trapezium ABCD



« 15 cm. • 195 cm<sup>2</sup>.»

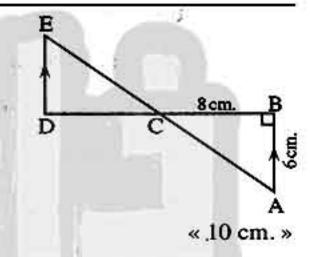
# 10 In the opposite figure:

 $\overline{BD} \cap \overline{AE} = \{C\}, \overline{AB} / / \overline{DE}$ 

AB = 6 cm. BC = 8 cm.

and C is the midpoint of BD

Calculate the length of : CE



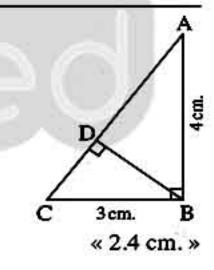
# 11 In the opposite figure:

ABC is a right-angled triangle at B

$$\overline{BD} \perp \overline{AC}$$
,  $AB = 4$  cm.

and BC = 3 cm.

Calculate the length of : BD



# 12 Complete the following:

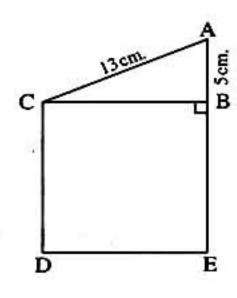
- In the right-angled triangle, the area of the square on the hypotenuse equals ......
- If XYZ is a right-angled triangle at X , XY = 12 cm. and XZ = 9 cm., then YZ = ..... cm.
- If ABC is a right-angled triangle at B, AB = 20 cm. and AC = 25 cm., then BC = ...... cm.

# (4) In the opposite figure :

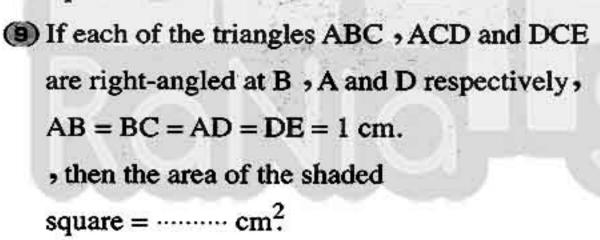
If m (
$$\angle$$
 ABC) = 90°

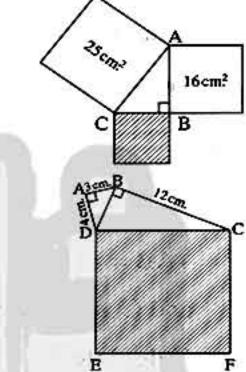
$$AB = 5 cm$$
.

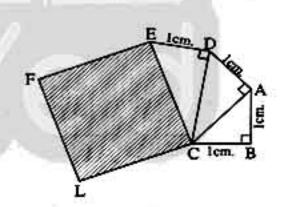
and 
$$AC = 13$$
 cm.



- (5) A rectangle is of length 8 cm. and width 6 cm. , then the length of its diagonal equals ..... cm.
- (6) If the area of a rectangle equals 60 cm<sup>2</sup> and its width is 5 cm., then the length of its diagonal = ..... cm.
- If Δ ABC is right-angled at B , then the side length of the shaded square = ······ cm.
- If A ABD is right-angled at A and  $\triangle$  BCD is right-angled at B, then the area of the shaded square = ..... cm<sup>2</sup>.







# 13 Choose the correct answer from those given:

# (1) In the opposite figure:

Which of the following relations is true?

(a) 
$$x = 4^2 + 3^2$$

(a) 
$$x = 4^2 + 3^2$$
 (b)  $x^2 = 4^2 - 3^3$ 

(c) 
$$x^2 + 9 = 16$$

(d) 
$$x^2 = 25$$

# (2) In the opposite figure :

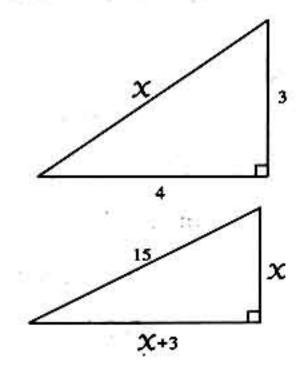
Which of the following relations is true?

(a) 
$$X + 3 + X = 15$$
 (b)  $X^2 + 3X = 108$ 

(b) 
$$x^2 + 3x = 108$$

(c) 
$$(x + 3)^2 = 15 - x^2$$

(c) 
$$(x+3)^2 = 15 - x^2$$
 (d)  $x^2 + 6x + 9 = 225$ 



Lesson Seven

# In the opposite figure :

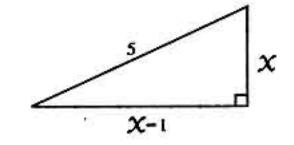
Which of the following relations is true?

(a) 
$$x^2 + (x-1)^2 = 5$$
 (b)  $x + (x-1) = 25$ 

(b) 
$$X + (X - 1) = 25$$

(c) 
$$x^2 - x = 12$$

(c) 
$$x^2 - x = 12$$
 (d)  $(x-1)^2 - x^2 = 25$ 



# (a) If ABCD is a square, then $(AC)^2 = \cdots$

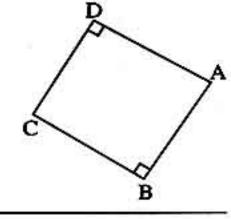
(a) AB

- (b)  $(AB)^2$
- (c)  $2 (AB)^2$
- (d)  $4 (AB)^2$

# 14 In the opposite figure:

If 
$$m (\angle B) = m (\angle D) = 90^{\circ}$$

**Prove that** :  $(AB)^2 + (BC)^2 = (AD)^2 + (DC)^2$ 



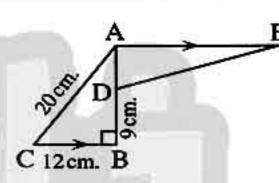
# 15 In the opposite figure :

ABC is a triangle,  $m (\angle B) = 90^{\circ}$ 

$$\overline{AE}$$
 //  $\overline{BC}$   $\overline{BC}$  = 12 cm.  $\overline{AC}$  = 20 cm.

$$D \in AB$$
 where  $BD = 9$  cm. and  $AE = 2$  BC

, find the length of each of : AD and ED

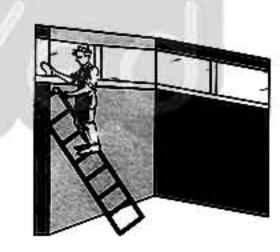


«7 cm. » 25 cm.»

# Life Applications

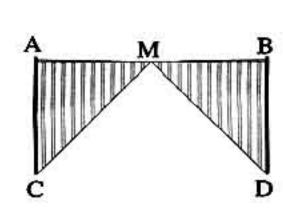
16 A window cleaner has a ladder which is 5 metres long. He places it so that it reaches a window sill 4 metres from the ground.

How far is the wall from the foot of the ladder?



«3 m.»

17 A wooden bridge AB of length 15 m. is built horizontally on two vertical walls AC and BD resting on two supports MC and MD If AC = 4 m. and AM = MB, calculate the length of the support MC

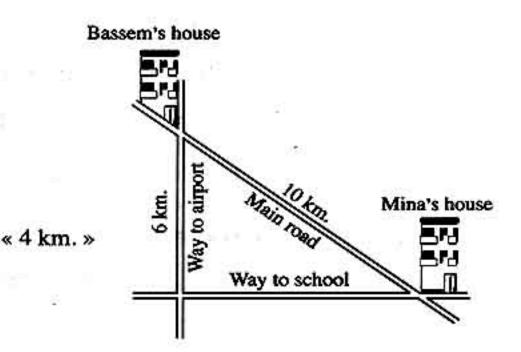


« 8.5 m. »

Unit 3

18 If Mina wants to go to the house of his friend Bassem.

What is the distance he saves if he takes the main road instead of the other two roads?





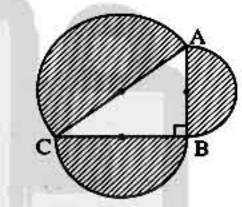
# For excellent pupils

19 If  $\triangle$  ABC is right-angled at B, D is the midpoint of  $\overline{BC}$ ,

**Prove that**:  $(AC)^2 - (AD)^2 = 3 (BD)^2$ 

20 In the opposite figure:

Prove that the sum of areas of the two semicircles drawn on the two sides of the right angle in a right-angled triangle equals the area of the semicircle drawn on the hypotenuse? [Given the area of the circle =  $\pi r^2$ ]



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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمسولة

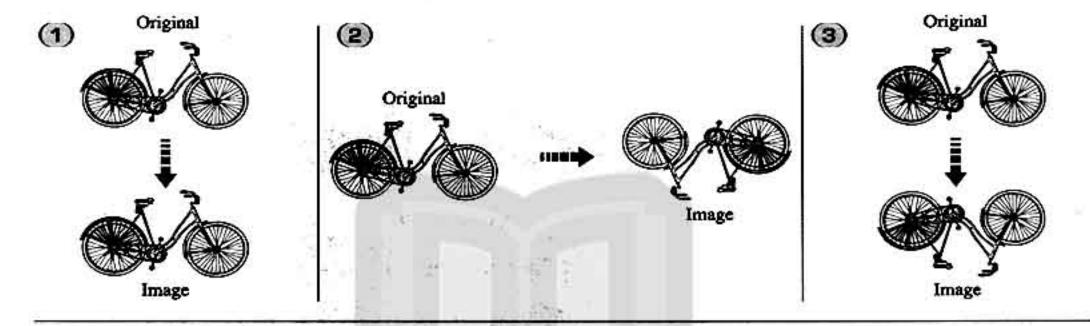
Lesson Eight

III From the school book

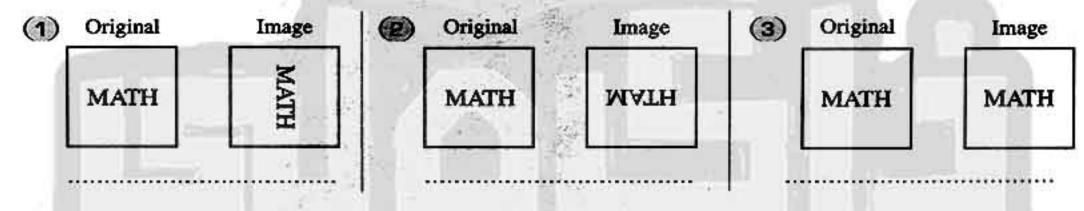
# Exercise 8

# On geometric transformations

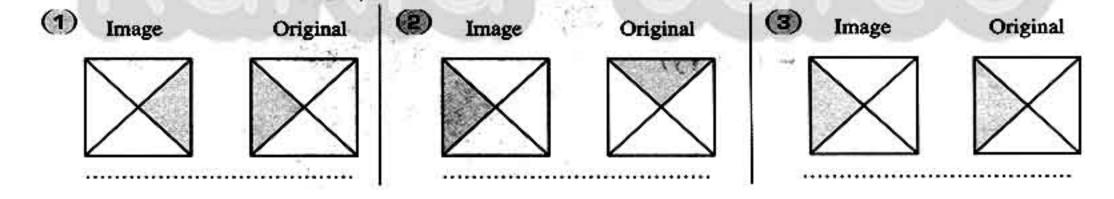
1 Describe the type of the geometric transformation (reflection, translation or rotation) in each of the following:



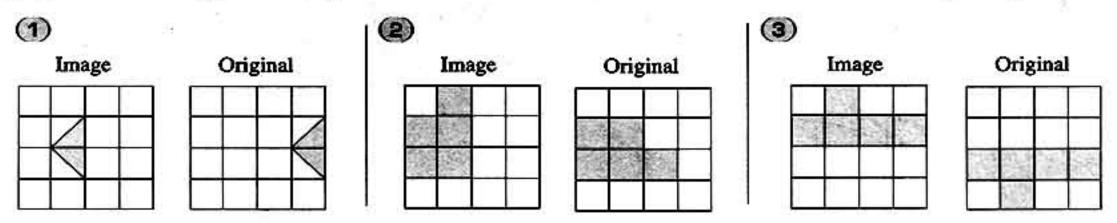
Write below each shape the type of the geometric transformation (reflection > translation or rotation):



3 Write below each shape the type of the geometric transformation (reflection , translation or rotation):

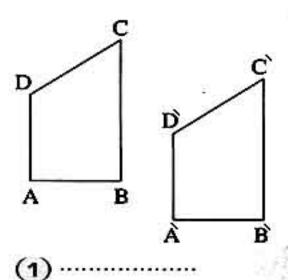


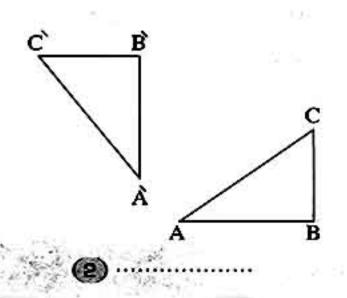
4 Write the type of the geometric transformation in each of the following shapes:

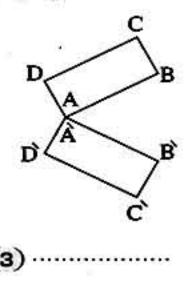


المحاصل ریاشیات لناے (غاریت) / ۱ إعدادی / تیری ۱۳:۲۱۲

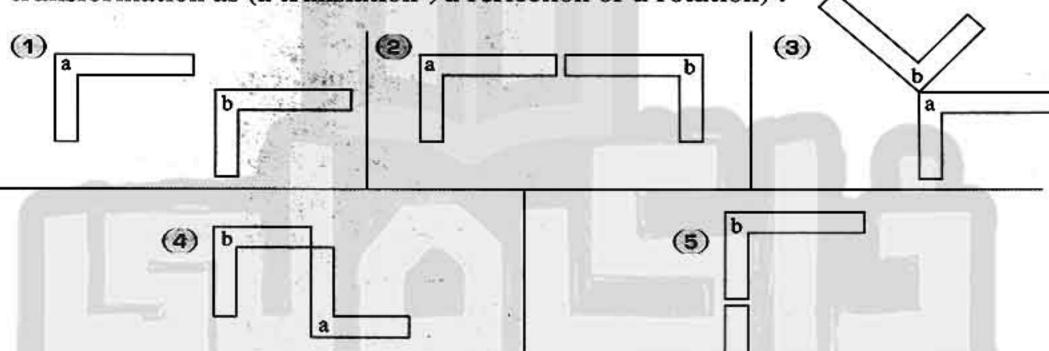
Describe the type of transformation in each of the following figures (reflection , translation , rotation) :



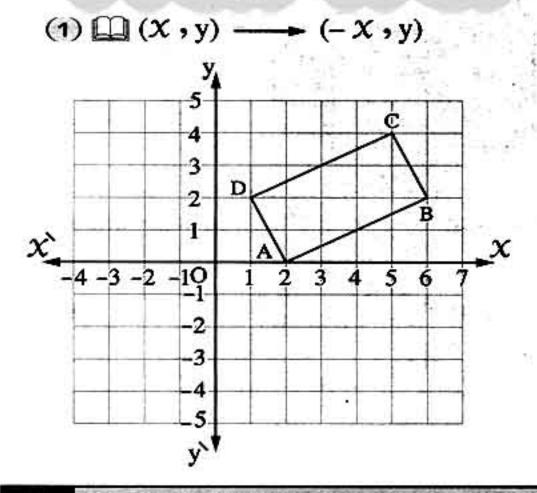




6 Pigure b is the image of figure a by a geometric transformation. Identify each transformation as (a translation , a reflection or a rotation) :



7 Draw the image of each figure according to the shown transformation, then describe each type:

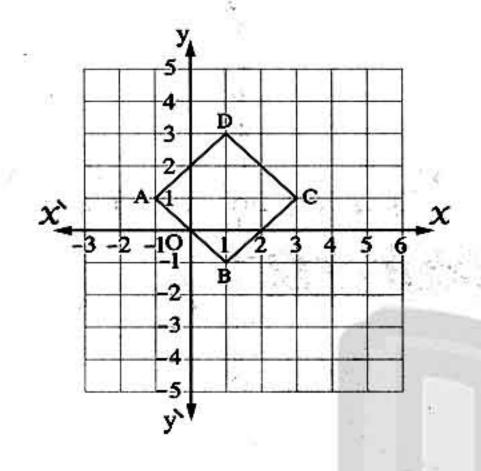


-5 -4 -3 -2 -1Q

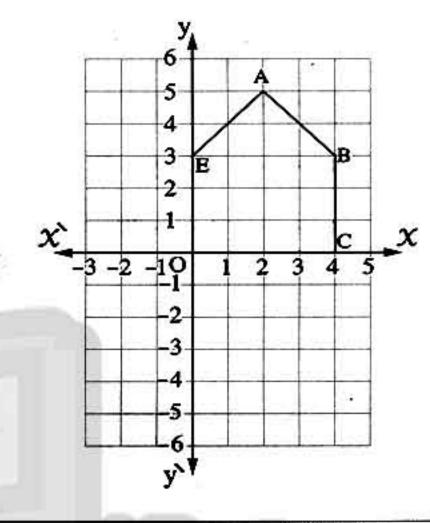
هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلقة

Lesson Eight

(3) 
$$\square$$
  $(x,y) \longrightarrow (x+2,y+3)$ 

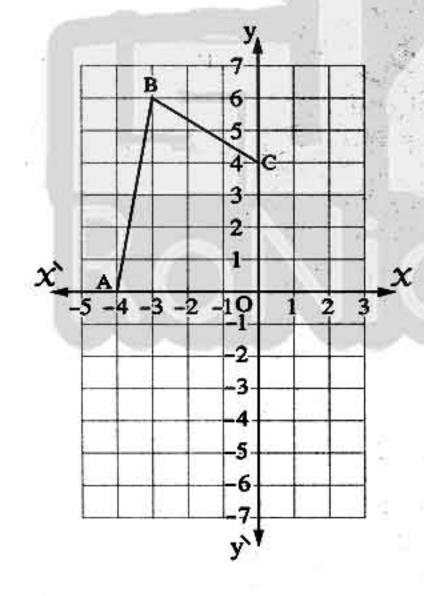


$$(4)(x,y) \longrightarrow (x,y-3)$$

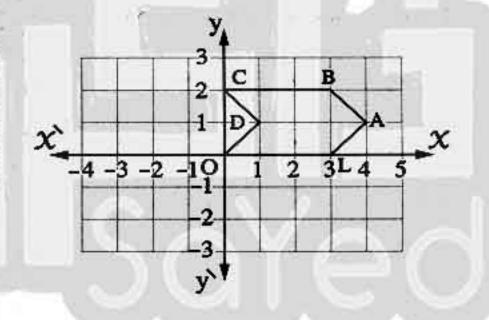


$$(5)(x,y) \longrightarrow (y,-x)$$

2+2



$$(B)(x,y) \longrightarrow (-x,y)$$



∟ <sub>Unit</sub> 3

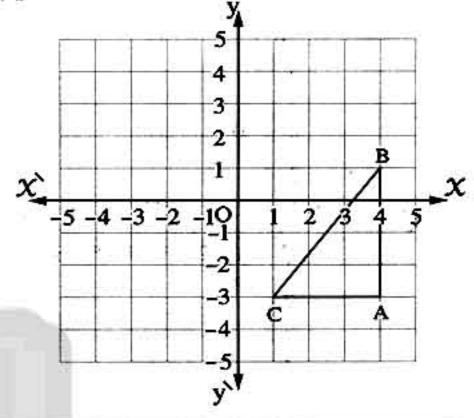
B Map the image of  $\triangle$  ABC where A (4, -3), B (4, 1), C (1, -3) according to the following transformations then describe its type:

(1) 
$$(x,y) \longrightarrow (-x,y)$$

(2) 
$$(X,y) \longrightarrow (-X,-y)$$

(3) 
$$(x,y) \longrightarrow (x,y-2)$$

(4) 
$$(x, y) \longrightarrow (-y, x)$$



9 Draw the image of the polygon ABCDEO according to each transformation and describe the type:

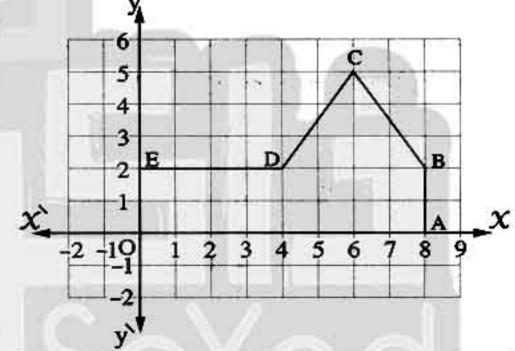
$$(1) (X,y) \longrightarrow (-X,y)$$

(2) 
$$(x,y) \longrightarrow (x,y+5)$$

$$(3) (X,y) \longrightarrow (-X,-y)$$

$$(4) (x,y) \longrightarrow (x-5,y)$$

(5) 
$$(x, y) \longrightarrow (x, -y)$$



10  $\square$  Draw the image of  $\triangle$  ABC where A (1, 2), B (3, 2) and C (3, 5) by the following transformations:

(1) 
$$(x,y) \longrightarrow (x,-y)$$

(2) 
$$(x,y) \longrightarrow (x+1,y-3)$$

(3) 
$$(x,y) \longrightarrow (-y,x)$$

On a square lattice, draw  $\triangle$  ABO where A (3, 1), B (1, 3) and O is the origin point, and draw its images by the following transformations then discribe its type:

(1) 
$$(x,y) \longrightarrow (x+1,y-2)$$

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

Lesson Eight

$$(3)(x,y) \longrightarrow (-y,x)$$

$$(4)(X,y) \longrightarrow (-X,-y)$$

On a square lattice, draw the quadrilateral ABCD where A (1,1), B (4,2), C (3,4) and D (1,4), and draw its image by the following transformation, then discribe its type:

$$\textcircled{1}(X,y) \longrightarrow (y,-X)$$

$$(2)(x,y) \longrightarrow (-x,y)$$

$$(3)(X,y) \longrightarrow (X-1,y+1)$$

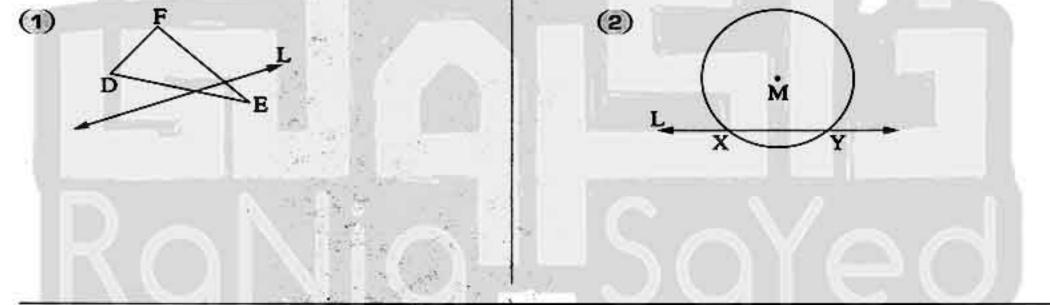
# For excellent pupils

Draw  $\triangle$  ABC whose image  $\triangle$   $\stackrel{\frown}{A}$   $\stackrel{\frown}{B}$   $\stackrel{\frown}{C}$  by the transformation  $(x, y) \longrightarrow (-y, x)$  where  $\stackrel{\frown}{A}$  (1, -1),  $\stackrel{\frown}{B}$  (3, 1) and  $\stackrel{\frown}{C}$  (4, -1), then discribe the transformation type.

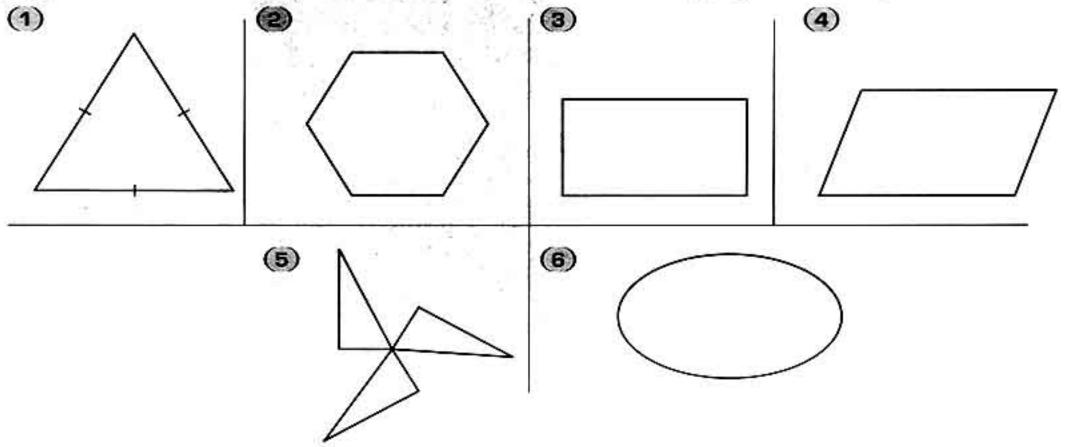


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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلقة



3 Draw the axes of symmetry of each of the following figures if they are existed:



هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمحتوية

Lesson Nine

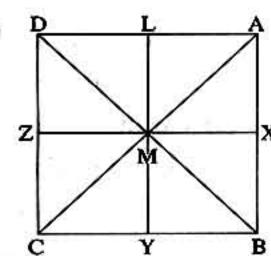
- 4 Draw the triangle ABC in which: AB = 6 cm.,  $m (\angle A) = 90^{\circ}$  and  $m (\angle B) = 30^{\circ}$ Then draw its image by reflection in AB
- Draw the image of  $\triangle$  ABC in which: AB = 3 cm., BC = 4 cm. and AC = 5 cm. by reflection in the straight line containing the shortest side.
- 6 Draw the image of  $\triangle XYZ$  in which: XY = 3 cm., YZ = 5 cm. and ZX = 7 cm. by reflection in the straight line containing the longest side.
- Draw  $\triangle$  ABC in which: AB = 3 cm., BC = 6 cm. and m ( $\angle$  ABC) = 90°, then find its image by reflection in the straight line L which is perpendicular to BC at C
- B Draw the rectangle ABCD in which: AB = 6 cm. and CB = 4 cm., then draw its image by reflection in AD. Say the name of the resulting figure which consists of the rectangle and its image, then find its perimeter. « 32 cm. »
- 9 Draw the image of the circle M whose radius length is 2 cm. , by reflection in the straight line which is far from the centre by 1 cm.
- 10 Draw the circle N with radius length 2.5 cm. then draw its image by reflection in the straight line which is far from its centre by 2.5 cm.
- 11 Draw  $\triangle$  ABC where BC = 3 cm., AB = 4 cm. and AC = 5 cm. If the point D is the image of the point C by reflection in AB Find:
  - (1) The perimeter of  $\triangle$  ACD
  - (2) The area of Δ ACD

« 16 cm. , 12 cm<sup>2</sup>. »

# 12 In the opposite figure:

ABCD is a square. M is the point of intersection of its diagonals X, Y, Z and L are the midpoints of its sides AB, BC, CD and DA respectively. Complete the following:

- (1) The image of the point A by reflection in LY is ........
- (2) The image of the  $\overline{AM}$  by reflection in  $\overline{XM}$  is
- (3) The image of the  $\triangle$  ALM by reflection in  $\overrightarrow{LY}$  is ......
- (4) The image of the  $\triangle$  ALM by reflection in  $\overrightarrow{XZ}$  is ......
- (5) The image of the Δ ALM by reflection in  $\overrightarrow{AM}$  is ........



هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى إ الصف الاول الاعدادي صحيحاكي التعليم

Unit 3

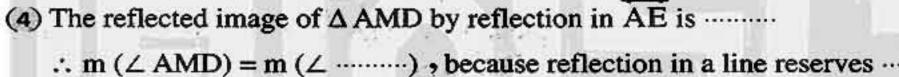
- (6) The image of the  $\triangle$  AMB by reflection in  $\overrightarrow{LY}$  is ......
- The image of the  $\triangle$  AMB by reflection in  $\overrightarrow{XZ}$  is ......
- (9) The image of the square ABCD by reflection in  $\overrightarrow{LY}$  is .......
- $\bullet$   $\bullet$  MZD is the image of  $\bullet$  MZC by reflection in .......
- (1)  $\Delta$  AXM is the image of  $\Delta$  CYM by reflection in ......

# 13 In the opposite figure:

 $\triangle$  ABC is an equilateral triangle, where D, E and F are the midpoints of  $\overline{AB}$ ,  $\overline{BC}$  and  $\overline{AC}$  respectively, and  $\overline{AE} \cap \overline{BF} \cap \overline{CD} = \{M\}$ :

## Complete:

- (1) Axes of symmetry of Δ ABC are ......
- (2)  $\overline{AB}$  is the reflected image of  $\overline{AC}$  by reflection in ......
- (3) The reflected image of  $\overrightarrow{AF}$  by reflection in  $\overrightarrow{BF}$  is ........., and the reflected image of  $\overrightarrow{CF}$  in  $\overrightarrow{AE}$  is ........



- (5) The reflected image of  $\triangle$  AMB by reflection in  $\overrightarrow{AE}$  is .......
- (6) Δ BMC is the reflected image of ......... by reflection in CD, and the reflected image of ...... by reflection in BF
  - ... BM = AM, and CM = AM, because the reflection reserves .......

# 14 Complete the following:

1 The reflection in a plane reserves:

(a) ······ (b) ······

- (c) ····· (d) ····
- (2) If the reflection in a straight line transforms the figure to itself then this straight line is called .........
- (3) The number of axes of symmetry of:

(a) The equilateral triangle is ....... (b) The isosceles triangle is .........

(i) The isosceles trapezium ........... (j) The circle .........

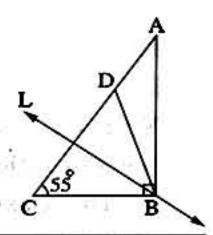
104

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلوم

Lesson Nine

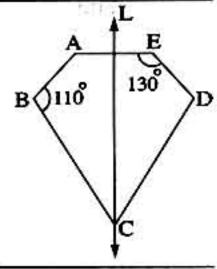
(4) In the opposite figure:

If m (
$$\angle$$
 ABC) = 90°  
and m ( $\angle$  C) = 55°, the straight line L  
is the axis of symmetry of  $\triangle$  DBC, then m ( $\angle$  ABD) = .....°



[15] In the opposite figure :

If the straight line L is the axis of symmetry of the figure ABCDE, calculate: m (∠ BCD)



By using geometric instruments, draw the rectangle ABCD, where AB = 3 cm. and BC = 4 cm. locate A as the reflected image of A by reflection in CD and locate C as the reflected image of C by reflection in AB

Prove that:

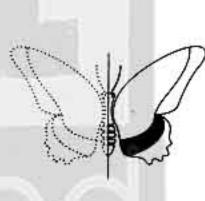
(1) m (
$$\angle$$
 CAC) = 2 m ( $\angle$  CAB)

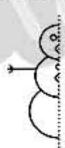
« 60° »



# Life Applications

17 By using the reflection we can complete drawing some of the symmetrical shapes like the butterfly in the opposite figure. Use the reflection to complete each of the following figures:



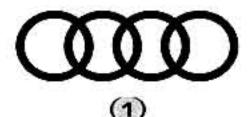








[18] In our daily life, we see many figures having one or more axes of symmetry in front of you, there are some signs of cars. Draw their axes of symmetry if they exist:

















الم**نت** احلا رياضيات لفائع اخاريت / 1 إعدادى / ديري ؟ (؟ : 11)

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

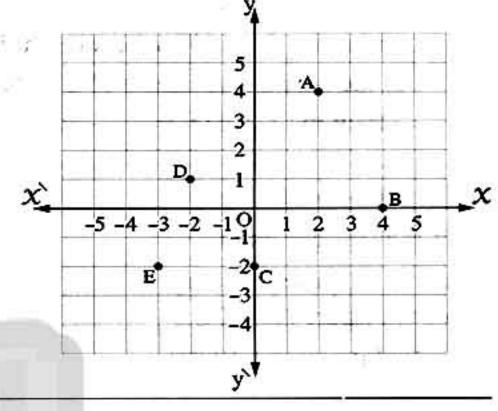
**u**nit **3** 

# Second Problems on reflection in the Cartesian plane :

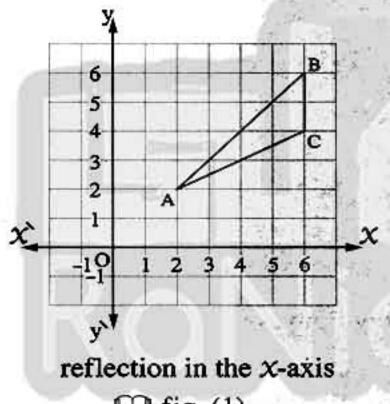
1 In the opposite figure :

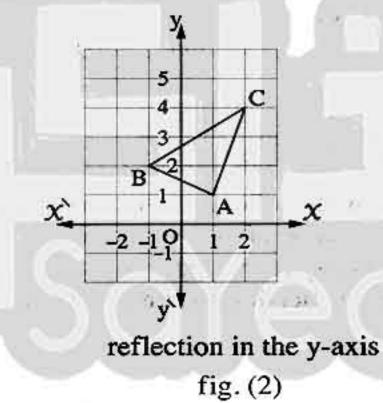
Write the coordinates of the image of each point by reflection in:

- The X-axis
- 2 The y-axis

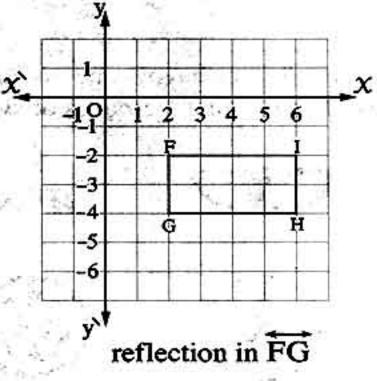


Copy each of the following figures on a lattice and draw the images of the figure by a geometric transformation as shown below each figure, then write the coordinates of each vertex of the figure.





(1) fig. (1)



III fig. (3)

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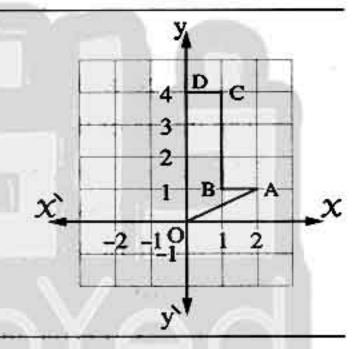
هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلوم

Lesson Nine

B Draw AB where A (4,3) and B (1, -2), then draw its image by reflection in:

(1) The X-axis The y-axis

- 4 If A (3, 1) and B (3, -2), find DC which is the image of AB by reflection in the y-axis and name the figure ABCD and calculate its perimeter. « 18 length units »
- Find the image of  $\triangle$  ABC where A (-6,-1), B (-2,-1) and C (-5,-6)by reflection in the X-axis
- Draw the image of Δ ABC where A (0,0), B (3,0) and C (-1,2) by reflection in the y-axis
- 7 On a square lattice, draw  $\triangle$  ABC where A (2, -2), B (3, 4) and C (-3, 2) then draw  $\triangle \stackrel{>}{ABC}$  which is the image of  $\triangle$  ABC by reflection in the y-axis then draw  $\triangle \overrightarrow{ABC}$  which is the image of  $\triangle \overrightarrow{ABC}$  by reflection in the X-axis
- B Draw the image of the opposite figure by reflection in the X-axis and in the y-axis another time



- 9 On a square lattice, draw the rectangle whose vertices are A (3, 2), B (8, 2) , C (8, 6) and D (3, 6), then draw its image by reflection in the y-axis
- $\square$  Graph the square ABCD and its image: by reflection in the X-axis, then compare the length of the sides and the area where A (0, 2), B (-5, 0), C (-3, -5)and D (2,-3)
- ABCD is a rectangle in which: A (1, 1), B (1, 3) and C (-3, 3) Determine the coordinates of D from the graph, then find the image of the rectangle ABCD by reflection in the X-axis.
- 12 Draw the image of the square ABCD where A (2, 3) and B (2, -1) by reflection in the y-axis. What do you notice?
- 13 Draw the image of the rectangle XYZL where X (2, 2) and Y (-3, 2) with width 3 units by reflection in the x-axis.

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هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخ

Unit 3

# 14 Complete the following table :

No.	The point	Its image by reflection in the X-axis	Its image by reflection in the y-axis
1	(3,-2)	The self a district of the	455 %
2	S4134 4C	(1,2)	Star and American
. 3	C CONTINUES O	1	(-2,4)
4	(0,5)	3000000	
5	in manage of	(3,0)	considéres
6 .	,	<b>\$</b>	(0,0)

# 15 Complete the following:

- (1) The image of the point (1, 3) by reflection in the X-axis is ........
- (2) The image of the point (-2,5) by reflection in the y-axis .........
- (3) The image of the point (2, -3) by reflection in the ..... is (2, 3)
- (4) The image of the point (-1, -4) by reflection in the ...... is (1, -4)
- (5) The image of the point (0, 3) by reflection in the ...... is itself.
- (6) The image of the point (-5,0) by reflection in the ..... is itself.
- (7) The image of the point (2 , 1) by reflection in the X-axis followed by reflection in the y-axis is .........
- (8) The image of the point (2, -3) by reflection in the y-axis followed by reflection in the X-axis is .........
- (9) If A (-2,3) is the image of the point A (2,3) by reflection in y-axis, then the image of the point A by reflection in the y-axis is .........

# For excellent pupils

- Determine on a square lattice the points A (5,4), B (5,1), C (2,1),  $\hat{A}$  (4,5),  $\hat{B}$  (1,5) and  $\hat{C}$  (1,2)
  - If Δ ABC is the image of Δ ABC by reflection in the straight line L, draw this straight line.
  - (2) If the figure ABBA is the image of the figure CBBC by reflection in the straight line M, draw this straight line.
- If the geometric transformation  $(X, y) \longrightarrow (y, X)$  is a reflection in a straight line L, draw on a square lattice the straight line L

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

Lesson Ten

From the school book

# Exercise 10

# On reflection in a point

#### First

# Problems on reflection in the plane:

- 1 Choose the correct answer from the given ones:
  - (1) If AB is the image of AB by reflection in M, then AB ...... AB
    - (a) >

(b) <

(c) =

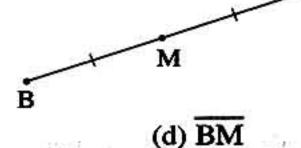
(d) ≠

(2) In the opposite figure :

The image of AB

by reflection in the point M is .....

- (a) AM
- (b) AB , .
- (c) BA



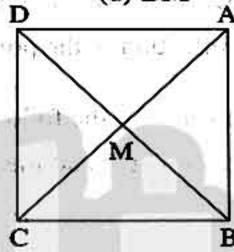
# (3) In the opposite figure:

ABCD is a square whose diagonals intersect at M The image of  $\Delta$  ABM by reflection in M is  $\Delta$ 

(a) ADM

(c) DCM

- (b) BCM
- (d) CDM



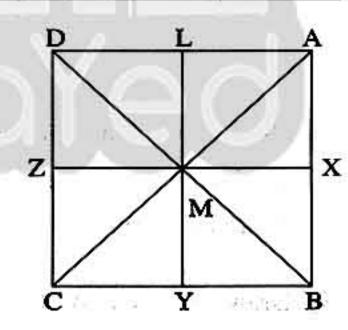
- (4) If A is the image of A by reflection in M and if MA = 5 cm., then AA = ......
  - (a) 5 cm.
- (b) 7 cm.
- (c) 10 cm.
- (d) 15 cm.

# 2 In the opposite figure:

ABCD is a square whose diagonals intersect at M X, Y, Z and L are the midpoints of AB, BC, CD and DA respectively

# Complete the following:

- (1) The image of the point A by reflection in M is ......
- (2) The image of the point X by reflection in M is ......
- The image of AL by reflection in M is ......
- The image of MZ by reflection in M is ......
- (5) The image of BM by reflection in M is .........
- The image of AX by reflection in X is .......
- The image of  $\Delta$  ALM by reflection in M is ......
- (8) The image of Δ BXM by reflection in M is .......
- (9) The image of Δ AMB by reflection in M is ..........
- The image of the square AXML by reflection in M is ......

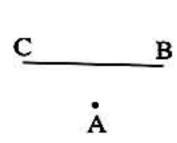


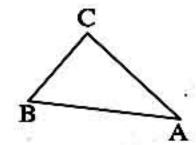
109

هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى والعمولي العملات العمامير المعاصر

Unit 3

Using the geometric tools , draw the image of each of the following by reflection in A (Answer in the same page of the book):





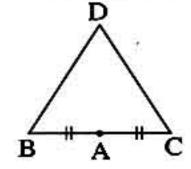
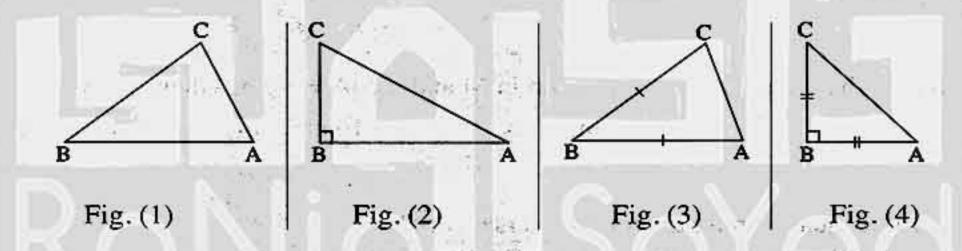


Fig. (1)

Fig. (2)

Fig. (3)

- Draw  $\triangle$  ABC in which AB = BC = 4 cm. and AC = 5 cm., then find its image by reflection in the point B
- In each of the following figures, draw  $\triangle ABC$  as the image of  $\triangle ABC$  by reflection in the point B and mention the name of the figure A CAC giving reason.



- Draw  $\triangle$  ABC in which BC = 3 cm., AB = 4 cm. and m ( $\angle$  B) = 90°, then draw  $\triangle$  ABC as the image of  $\triangle$  ABC by reflection in C Prove that the quadrilateral ABAB is a parallelogram.
- 7 Draw the square ABCD whose side length is 5 cm. then draw its image by reflection in the point M where M is the point of intersection of its diagonals. What do you observe?
- ABC is a triangle, F is the midpoint of AC Draw D as the image of B by reflection in F What is the type of the figure ABCD and what is the type of the triangle ABC required to transfer the figure ABCD to .........

(1) rectangle.

(2) rhombus.

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هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلومة

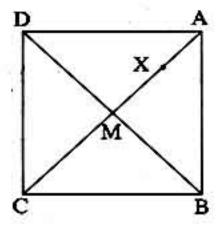
Lesson Ten

# 9 In the opposite figure :

ABCD is a square , M is the point of intersection of its diagonals and  $X \in AM$  Find Y as the image of X by reflection in M then,

**Prove that** : (1)  $\triangle$  DAX  $\equiv \triangle$  BCY

The figure DXBY is a parallelogram.

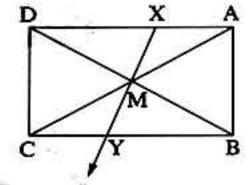


# 10 In the opposite figure :

ABCD is a rectangle, M is the point of intersection of its diagonals,  $X \in \overline{AD}$  and  $\overline{XM} \cap \overline{BC} = \{Y\}$ 

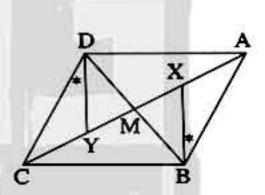
#### Prove that:

- (1) Y is the reflected image of X in M
- (2) The figure AXCY is a parallelogram.



# 11 In the opposite figure:

ABCD is a parallelogram, M is the point of intersection of its diagonals and X EAC, Y EAC such that  $m (\angle ABX) = m (\angle CDY)$ 



#### Prove that:

- (1)  $\triangle$  ABX is the image of  $\triangle$  CDY by reflection in M
- (2) The figure XBYD is a parallelogram.



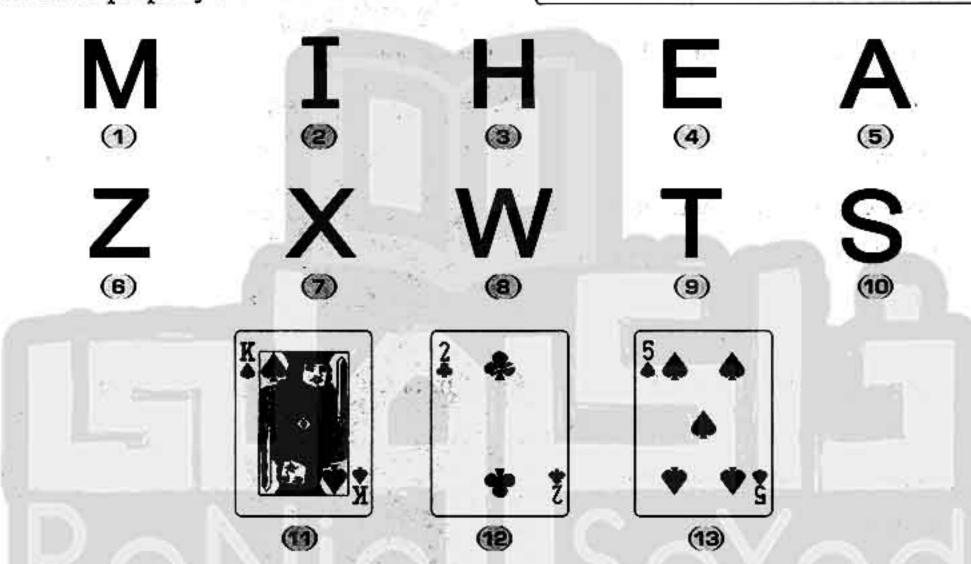
# Life Application

12 In front of you, an English letter. Check that if we find the image of this letter by reflection in the midpoint of the inclined line of the letter, then we get the same letter. And we notice that we will see the same figure if we look at it from above or down , right or left.

Which of the following figures has the same property?

Enrich information

This point is called "point of symmetry"



#### Problems on reflection in the Cartesian plane ; Second

- 1 Choose the correct answer from those given:
  - (1) The image of the point (-3,2) by reflection in the origin point is ........
    - (a)(3,2)
- (b) (-3, -2)
- (c) (3, -2)
- (d)(-3,2)
- (2) The point (5, -2) is the image of the point ...... by reflection in the origin point.

  - (a) (5,-2) (b) (-5,-2)
- (c)(-5,2)
- (d)(5,2)
- (3) The point whose image by reflection in the origin point is itself is .......
  - (a) (0, 1)
- (b) (1,0)

- (c)(0,0)
- (d)(-1,0)
- (4) The image of the point (3 , -2) by reflection in the origin point followed by reflection in X-axis is .....

  - (a) (3,-2) (b) (-3,-2)
- (c)(-3,2)
- (d)(3,2)

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Lesson Ten

- On a square lattice, draw  $\triangle$  ABC where A(3,1), B(1,4) and C(0,0), then find its image by reflection in the point C
- In Xy coordinate plane, draw  $\triangle$  ABC, where : A (-2,4), B (5,0) and C (3,-3), then find the reflected image of  $\triangle$  ABC in the origin point.
- On a square lattice, draw  $\triangle$  ABC where A (2, -2), B (3, 4) and C (-3, 2), then map  $\triangle$   $\triangle$ BC as the image of  $\triangle$  ABC by reflection in y-axis then map  $\triangle$   $\triangle$ BC as the image of  $\triangle$  ABC by reflection in X-axis. What is the image of  $\triangle$  ABC by reflection in the origin point? What do you deduce?
- B ABCD is a rectangle where A (2,5), B (6,5), C (6,8) and D (2,8), then find the image of the rectangle ABCD by reflection in the origin point.

# For excellent pupils

6 In the opposite figure :

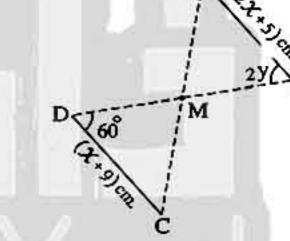
If CD is the image of BA

by reflection in the point M and BA =  $(2 \times + 5)$  cm.

CD = 
$$(X + 9)$$
 cm.  $\Rightarrow$  m  $(\angle A) = 2$  y and m  $(\angle D) = 60^{\circ}$ 

Find: (1) The length of CD

(2) The value of y



« 13 cm. , 30° »

From the school book

# Exercise 11

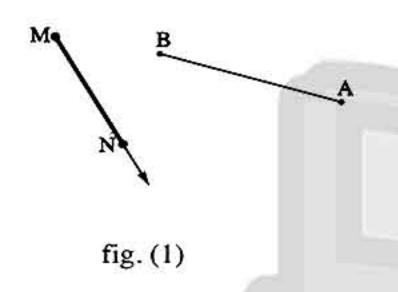
# On translation

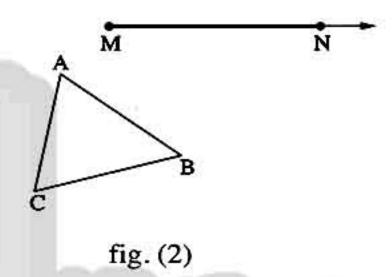
First

Problems on translation in the plane:

Using the geometric tools , draw the image of each of the following:

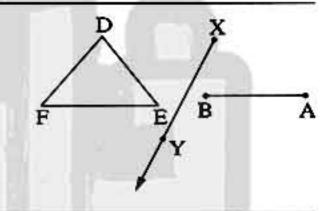
By translation MN in the direction of MN as shown in each case.





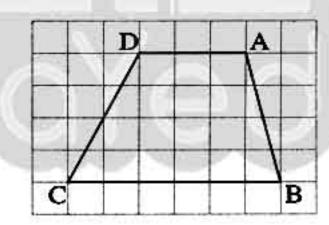
2 In the opposite figure :

Using the geometric tools, find the image of the following figures by the translation of displacement XY in the direction of  $\overrightarrow{XY}$ 



Of the figure ABCD

by the translation of 4 units in the direction of BC



- Draw a line segment  $\overrightarrow{AB}$  where  $\overrightarrow{AB} = 5$  cm., then draw the image of  $\overrightarrow{AB}$  by a translation of magnitude of 8 cm. in the direction of  $\overrightarrow{AB}$
- Using the geometric instruments, draw the square ABCD whose side length is 4 cm., then draw its image by translation of magnitude of 4 cm. in the direction of  $\overrightarrow{AB}$
- Draw  $\triangle$  ABC in which AB = 4 cm., BC = 6 cm. and CA = 5 cm., then draw the image of  $\triangle$  ABC by a translation of magnitude of 3 cm. in the direction of  $\overrightarrow{CB}$

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمحسوس

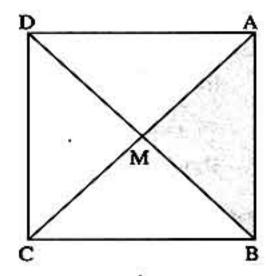
Lesson Eleven

# 7 In the opposite figure :

ABCD is a square whose side length is 4 cm.

M is the point of intersection of its diagonals. Draw:

- The image of  $\triangle$  MAB by the translation of distance 2 cm. in the direction of  $\overrightarrow{AD}$
- (2) The image of  $\triangle$  AMB by the translation AM in the direction of  $\overrightarrow{AM}$

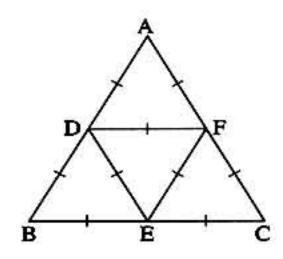


# 8 📖 In the opposite figure :

The triangles ADF, BDE, DEF and EFC are congruent.

#### Complete:

- (1) The image of Δ ADF by a translation of magnitude of AD in the direction of AD is .........
- (2) Δ FEC is the image of Δ DBE by a translation of magnitude ...... in the direction of ........



# 9 In the opposite figure :

ABCDEF is a regular hexagon. Complete the following:

- (1) The image of the point D by translation DM in the direction of  $\overrightarrow{DM}$  is .......
- (2) The image of  $\overrightarrow{AF}$  by translation ED in the direction of  $\overrightarrow{ED}$  is .......
- (3) The image of  $\triangle$  MCD by translation EF in the direction of EF is ........
- (4) The translation which makes  $\Delta$  DME the image of  $\Delta$  MAF is .......

# $D \xrightarrow{E} \xrightarrow{F} A$

# 10 In the opposite figure :

ABCD is a square and all the interior squares are congruent.

# Complete:

- (1) The image of  $\overrightarrow{AE}$  by a translation of magnitude of 2 cm. in the direction of  $\overrightarrow{GK}$  is .........
- A M P D
  2 cm. 2 cm.

  E N H Y
  F G K X
- (2) The image of the square AENM by a translation of magnitude of 4 cm. in the direction of  $\overrightarrow{PK}$  is .........
- (3) The square MNHP is the image of the square GLZK by a translation of magnitude ...... in the direction of .........
- 11  $\square \Delta$  ABC is right-angled at B where AB = 3 cm. and BC = 4 cm. If  $\Delta \stackrel{>}{A}\stackrel{>}{B}\stackrel{>}{C}$  is the image of  $\Delta$  ABC by translation of a distance 3 cm. in the direction of  $\stackrel{\frown}{C}\stackrel{\frown}{B}$  Prove that: The figure AACC is a parallelogram.

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12 Draw  $\triangle$  ABC which is right-angled at B , in which AB = BC = 3 cm. then find the image of  $\triangle$  ABC by translation of a distance 3 cm. in the direction of AB, then

Prove that: The figure BBCC is a square.

13  $\square$  ABCD is a rectangle, where  $E \in AD$  Find the translated image of  $\triangle$  ABE by translation of a magnitude DA in the direction of AD If E is the image of E by the same translation.

Prove that: The figure BCEE is a parallelogram.

14 ABCD is a parallelogram, BE  $\perp$  AD cutting it at E Find  $\triangle$  ABD as the image of  $\triangle$  ABE by translation of a distance ED in the direction of AD, then prove that the figure EBBD is a rectangle.

Second Problems on translation in the Cartesian plane:

- 1 Complete the following:
  - (1) The image of the point (2,5) by translation  $(x,y) \longrightarrow (x+2,y+1)$  is .......
  - (2) The image of the point (3, 2) by translation  $(x, y) \longrightarrow (x+3, y-2)$  is ......
  - (3) The image of the point (-5, 4) by translation  $(x, y) \longrightarrow (x + 4, y 5)$  is ......
  - (4) The image of the point (-2, -5) by translation  $(x, y) \longrightarrow (x-2, y)$  is .......
  - (5) The image of the point (3, -2) by translation  $(x, y) \longrightarrow (x, y + 3)$  is ......
- 2 Choose the correct answer from those given :
  - (1) The image of the point (-1, 2) by translation of magnitude of 3 units in the positive direction of the X-axis is ......

(a) (-1,5)

- (b) (2,2)
- (c)(-2,2)
- (d)(-1,3)
- (2) The image of the point (-3,4) by translation of magnitude of 4 units in the negative direction of the y-axis is .....

(a) (-3,0)

- (b) (-7,4) (c) (-3,8) (d) (-1,4)
- (3) If  $\hat{A}$  (3, -3) is the image of A by translation  $(x, y) \longrightarrow (x-1, y-4)$ , then the point A is .....

(a)  $(2 \rightarrow -7)$ 

- (b) (4,1) (c) (-4,-1) (d) (2,1)
- (4) The image of the point (-1, 4) by the translation (3, -2) followed by reflection in the X-axis is .....

(a)(2,2)

- (b) (-2, 2) (c) (-2, -2)
- (d) (2, -2)
- (5) If the point (a, -1) is the image of (2, 4) by the translation  $(x, y) \longrightarrow (x+1, y-b)$ , then (a, b) is ......
  - (a)(3,3)
- (b) (1,3)
- (c)(3,5)
- (d) (1, -5)

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Lesson Eleven

(6) If: A is the image of the point A (2,3) by reflection in the y-axis, then A is the image of A by the translation .....

(a) 
$$(x, y) \longrightarrow (x+4, y)$$

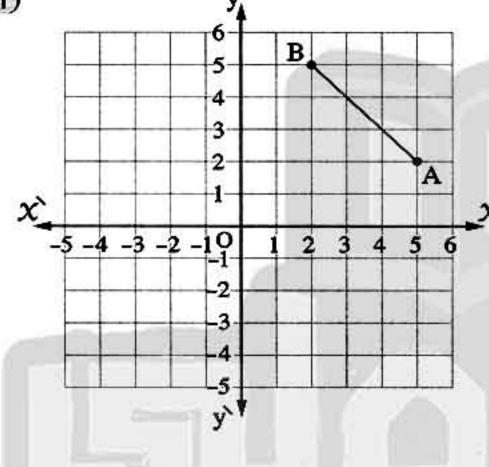
(b) 
$$(x, y) \longrightarrow (x, y + 6)$$

(c) 
$$(x,y) \longrightarrow (x-4,y)$$

(d) 
$$(X, y) \longrightarrow (X, y-6)$$

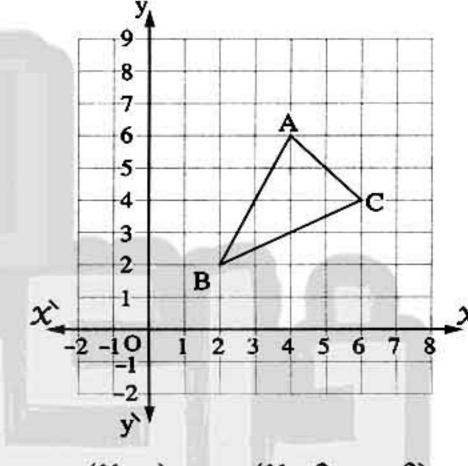
3 Find the image of each of the following figures by the translation shown under each figure:





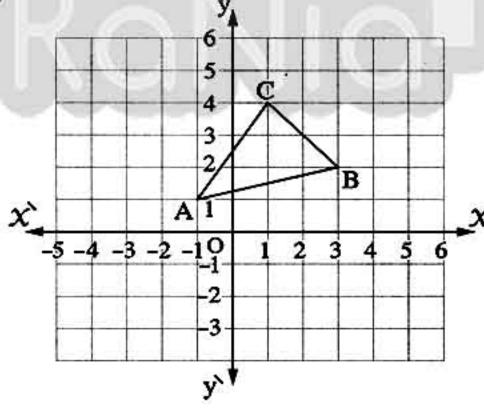
$$(x,y) \longrightarrow (x-3,y-4)$$





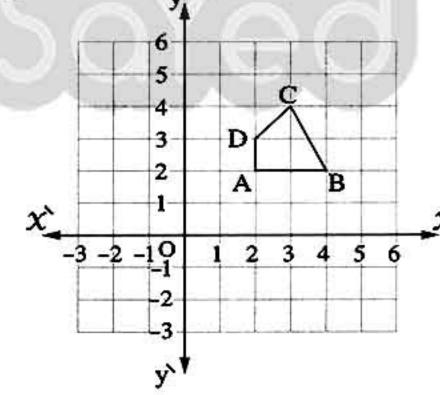
$$(x,y) \longrightarrow (x+2,y+3)$$

# (3)



$$(x,y) \longrightarrow (x+2,y)$$





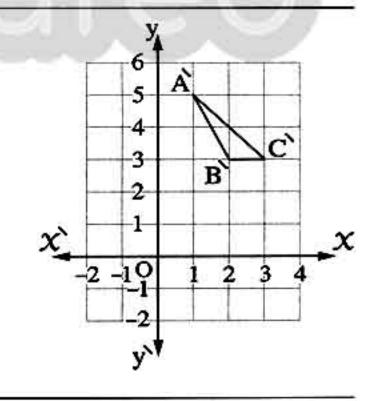
$$(x,y) \longrightarrow (x+3,y-2)$$

Lesson Eleven

- [10] On a square lattice, draw  $\triangle$  ABC where A (2, 1), B (1, -1) and C (0, 1), then draw its image by a translation of 2 AB in the direction of AB
- 11 A square has vertices A (1, 1), B (4, 2), C (3, 5) and D (0, 4)
  - (1) Graph the square and its image under the translation which maps vertex A onto vertex B
  - (2) Write the mapping rule for the translation.
- 12 Use the translation:  $(x, y) \longrightarrow (x + 2, y + 3)$  to locate the point whose image is (2, 3)
- III III If the image of the point A (1, 1) by translation in the plane is A(2, 2), find the images of the points O (0,0), B (-1,3) and C (-3,5) by the same translation.
- If A (-3, 1) and B (1, -2), write the mapping rule of the translation that makes B the image of A
- **15** If A (3,2), B (5,1), find:
  - (1)  $\overrightarrow{C}$  which is the image of C(1,-1) under translation of  $\overrightarrow{AB}$  in the direction of  $\overrightarrow{AB}$
  - (2) D whose image is D (2 , 1) under translation of AB in the direction of AB
- 16  $\square$  The point A (3, -3) is the image of the point A by the translation  $(x, y) \longrightarrow (x-1, y-4)$  Locate A then by the same translation, draw the image of  $\triangle$  ABC where B (5,0) and C (-1,-2)
- [17] [ In the opposite figure :

Copy the graph, then draw the triangle ABC whose image is △ ABC by the translation

$$(x,y) \longrightarrow (x+2,y+3)$$

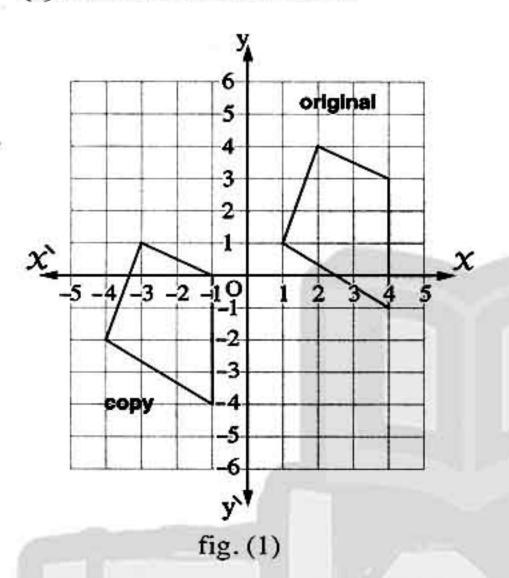


If A (-2,1) and B (1,3), find on a square lattice the image of AB by reflection in X-axis followed by the translation  $(X, y) \longrightarrow (X + 4, y)$ 

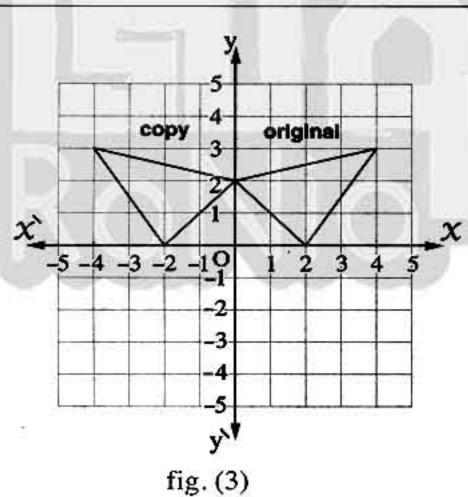
119

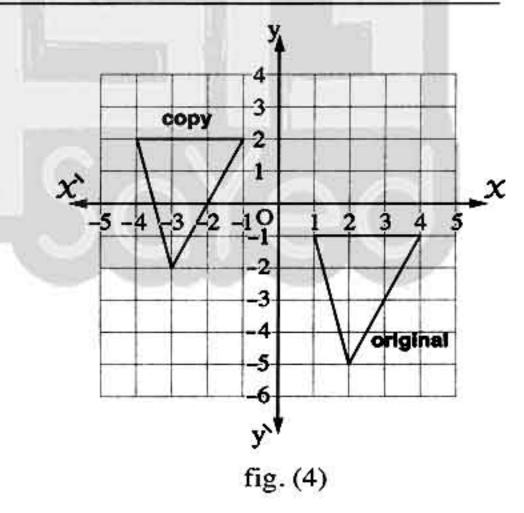
19 A State whether the graph shows a reflection or a translation:

- (1) Name the line of reflection.
- (2) Describe the translation.



original copy fig. (2)





From the school book

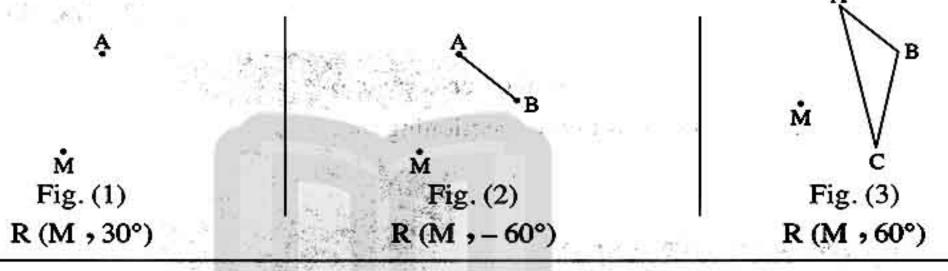
# Exercise 12

# On rotation

First

Problems on rotation in the plane:

1 Draw the image of the point A,  $\overline{AB}$  and  $\triangle ABC$  by the required rotation:



- 2 Use the geometric tools to draw  $\overline{AB}$  with length 3 cm., then draw its image by rotation R (B, 135°).
- Draw the equilateral triangle ABC with side length 6 cm. Draw the image of the triangle ABC by rotation R (A, 60°)
- Draw the triangle ABC in which AB = 5 cm.  $_{2}$ BC = 6 cm. and CA = 7 cm. then draw the image of Δ ABC by rotation

(1) R (A, 180°)

R (A, 360°)

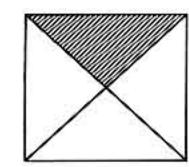
- Draw the triangle XYZ in which XY = XZ = 3 cm. and YZ = 4 cm. , then draw the image of  $\Delta XYZ$  in each of the two cases :
  - By rotation about X with an angle of measure 90°
  - By rotation about X with an angle of measure (270°)
- Draw  $\triangle$  ABC in which AB = 5 cm., AC = 3 cm., m ( $\angle$  A) = 40°, then draw  $\hat{C}$  the image of C by rotation R (A, 40°),  $\hat{B}$  the image of B by rotation R (A, -40°)
- 7 Draw the square ABCD with side length 5 cm. Draw the image of the square ABCD:
  - (B) By rotation R (B, 90°)
  - By rotation R (A, 180°)

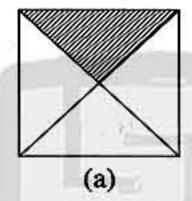
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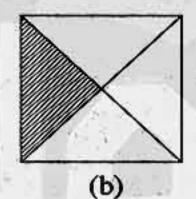
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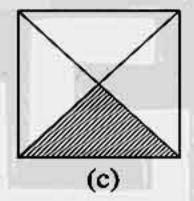
Lesson Twelve

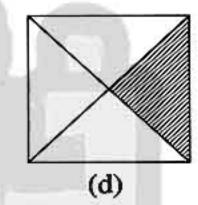
- B Using the geometric tools, draw the square ABCD with side length 4 cm., then draw its image by rotation about its centre (The point of diagonals intersection) with an angle of measure 90°
- Draw the rectangle ABCD in which BC = 6 cm., AB = 4 cm. Draw the image of the rectangle ABCD:
  - (1) By rotation R (A, 90°)
  - By rotation R (M , 180°) where M is the point of intersection of its diagonals.
- 10 Choose the correct answer from those given :
  - Which of these figures represents the rotation of the opposite square about its centre with an angle of measure 270°?



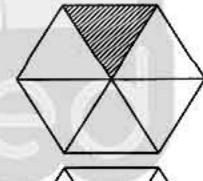


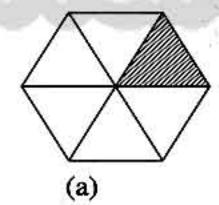


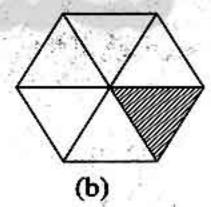


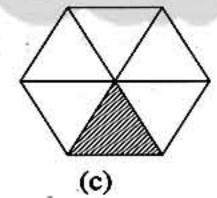


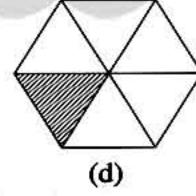
Which of these figures represents the rotation of the opposite regular hexagon about its centre with an angle of measure (- 120°)?





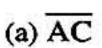






In the opposite figure :

If B is the midpoint of AC, then the image of AC by rotation about B with an angle of 180° is .....



(b)  $\overline{AB}$ 

(c) CA

(d)  $\overline{CB}$ 

In the opposite figure:

CD is the image of AB under

a rotation about M

and the measure of its angle is ......

- (a) 75°
- (b) 30°
- $(d) 150^{\circ}$

In the opposite figure:

 $\triangle AB\hat{C}$  is the image of  $\triangle ABC$ 

by a rotation about A

with an angle of measure ......

- $(a) 110^{\circ}$
- (d) 140°

and graffin a come of the property of the ♠

In the opposite figure:

 $\triangle$  ABC is the image of  $\triangle$  DEC

which is right-angled

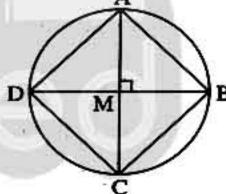
at C by rotation about C with an angle of measure .......

- (a) 90°
- (b)  $-90^{\circ}$
- (c) 180°
- (d) 360°

In the opposite figure:

The radius length of circle M is 3 cm.,

AC and BD are two perpendicular diameters in it.



## Complete:

- By the rotation R (M, 90°), then the image of the point A is ....... and the image of the point B is ......
  - ... The image of AB is ...... and the image of AB is ......
- By rotation R (M  $\rightarrow$  90°) , the image of  $\overline{AB}$  is ........ and the image of AB is ..... and the image of AB is .....
- By rotation R (M, 180°), the image of the point A is ......, the image of the - Caller and Addition of all Allieban and an Addition point B is .....
  - ... The image of AB is ......
- By rotation R (M, -180°), the image of AB is ......



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## 12 In the opposite figure:

ABCDEF is a regular hexagon whose centre is M. Complete the following:

The image of the point E by rotation about M with an angle of measure 120° is ......



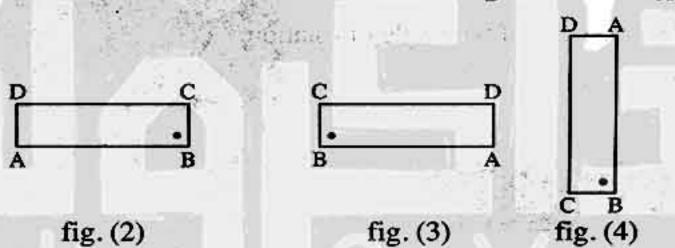
The image of DE by rotation about M with an angle of measure - 60° is ......

The image of  $\Delta$  MCD by rotation about M with an angle of measure 300° is .....

Δ ABM is the image of Δ CDM by rotation about ...... with an angle of measure .......

Δ BMC is the image of ...... by rotation about M with an angle of measure (- 120°)

## 13 A Referring to the opposite figure, choose the correct answer from those given:



The image of the figure by reflection in AD is ......

(a) fig. (1)

fig. (1)

(b) fig. (2)

(c) fig. (3) (d) fig. (4)

The image of the figure by rotation about A with an angle of measure 90° is ......

(a) fig. (1)

(b) fig. (2) (c) fig. (3) (d) fig. (4)

The image of the figure by translation to the right is .....

(a) fig. (1)

(b) fig. (2)

(c) fig. (3)

(d) fig. (4)

The image of the figure by rotation about A with an angle of measure 180° is ......

(a) fig. (1)

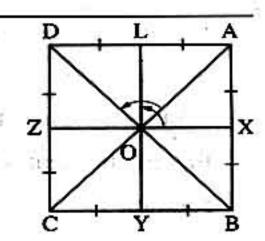
(b) fig. (2)

(c) fig. (3)

(d) fig. (4)

## 14 In the opposite figure:

ABCD is a square, O is the point of intersection of its diagonals X, Y, Z and L are the midpoints of AB, BC, CD and DA respectively.



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Unit 3

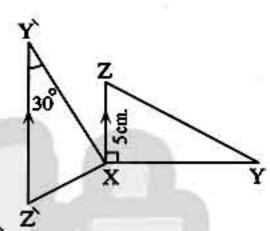
#### Find:

- (1) The image of  $\triangle$  AXO by reflection in  $\overrightarrow{AO}$  followed by another reflection in  $\overrightarrow{LO}$
- (2) The image of Δ AXO by rotation R (O, 90°)
- 15 ABC is a right-angled triangle with AB = 5 cm. and BC = 12 cm. Find:
  - (11) X as the image of B by translation 9 cm. in the direction of BA
  - 2 Y as the image of B by rotation R (A, -90°)
  - 3 The length of  $\overline{XY}$

## 16 In the opposite figure:

If the point X is the centre of rotation such that  $\hat{Y}$  is the image of Y and  $\hat{Z}$  is the image of Z If  $\overline{XZ}//\overline{\hat{Y}Z}$ , find:

- 1 The measure of the angle of rotation.
- (2) The length of  $\overline{XZ}$



« 120° , 5cm. »

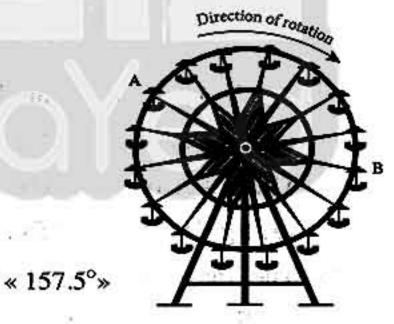


#### Life Applications

## 17 In the opposite figure:

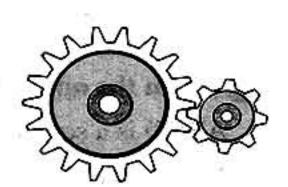
The wheel is one of the rides in the funfair, if the wheel moves from position A to position B.

What is the measure of the rotation angle in this case?



Gears are used to change the speed and direction of rotating parts of some machines

In the opposite figure, if the smaller gear makes one complete rotation clockwise direction, then what is the measure of the angle of rotation of the greater gear, and what is the direction of its



« 160°»

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rotation?

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Lesson Twelve

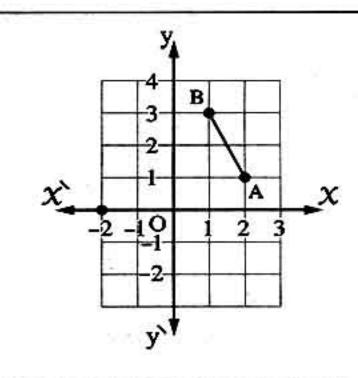
#### Second Problem on rotation in the Cartesian plane:

#### 1 Complete the following:

- The image of the point (2, -3) by rotation about the origin point with an angle of measure 90° is ...... and with an angle of measure 180° is .....
- (2) The image of the point (-1,0) by rotation about the origin point with an angle of measure 90° is ...... and with an angle of measure 360° is .....
- (3) The point (3, -2) is the image of the point (2, 3) by rotation about the origin point with an angle of measure .....
- The image of the point ..... by rotation about the origin point with an angle of measure 90° is (-1,4)
- The image of the point ..... by rotation about the origin point with an angle of measure  $(-180^\circ)$  is (5, -2)
- (B) The image of the point (-3,7) by rotation 90° about the origin point followed by reflection in y-axis is .....
- The image of the point (-2,0) by translation  $(x,y) \longrightarrow (x+3,y-1)$  followed by rotation about the origin point with an angle of measure 90° is ......
- (B) The rotation with an angle of measure 90° about the origin point maps the point (x, -y) onto the point ......
- (3) The image of (a , b) is the same point by rotation about the origin point with an angle of measure .....
- (10) If the image of the point (x, y) by rotation about the origin point with an angle of measure 90° is (a,b), then  $a + y = \dots$

## 2 In the opposite figure:

The point A (2, 1) and B (1, 3)Find the image of AB by rotation about the origin point with an angle of measure 90°

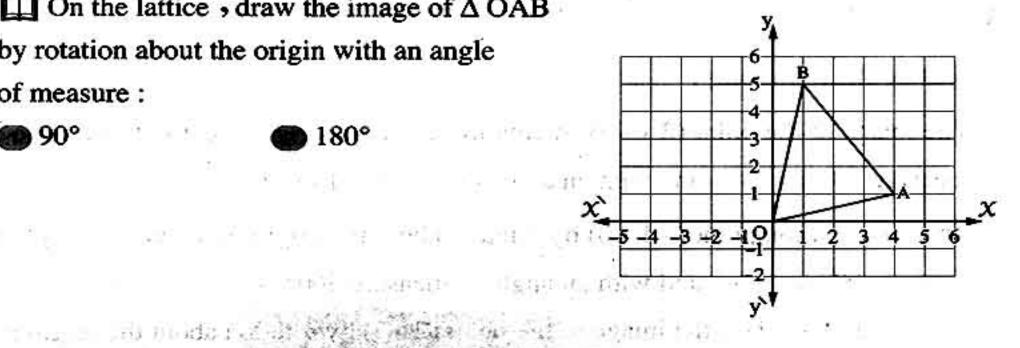


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∟ Unit 🏅

3 Ω On the lattice, draw the image of Δ OAB by rotation about the origin with an angle of measure:

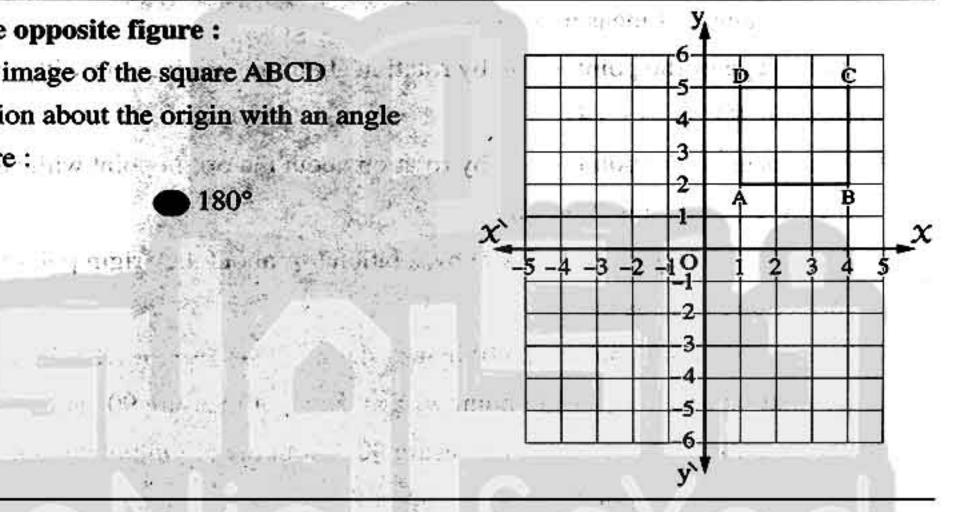
90°



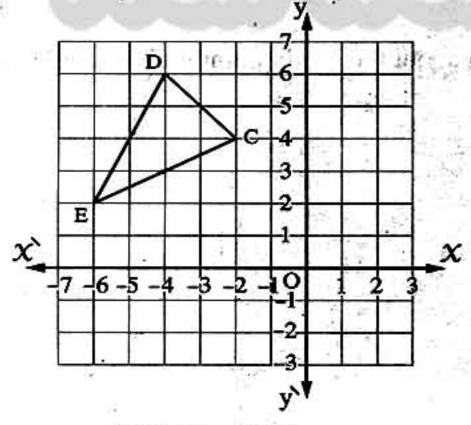
4 In the opposite figure :

Draw the image of the square ABCD by a rotation about the origin with an angle of measure:

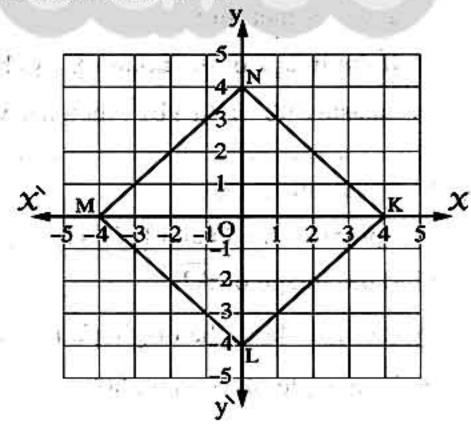
90°



Copy each figure on a graph paper. Draw their images under the transformation indicated. Give the coordinates of the images vertices in each case.



Rotation of 90° Clockwise about O



Rotation of 90° anticlockwise about O

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(c) Draw three images formed by rotating the rectangle about its centre through an angle of measure

(1) 90°

2 180°

270°



#### For excellent pupils

#### 14 In the opposite figure:

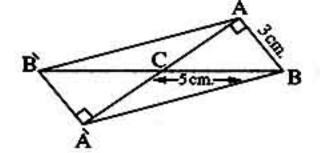
ABC is a right-angled triangle at A

AB = 3 cm. and BC = 5 cm.

If:  $\triangle CAB$  is the image of  $\triangle CAB$ 

by rotation about C and with an angle of measure 180°

Find the area of  $\triangle A \hat{A} \hat{B}$ 



« 12 cm<sup>2</sup>. »



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General Exercises

# General Exercises on Unit Three "Geometry and Measurement"

J.	rst : Completion questions :
) (	Complete the following:
0	If two straight lines intersect, then each two vertically opposite angles are
•	The sum of the measures of the accumulative angles at a point equals
6	The sum of measures of the interior angles of the heptagon = ·······°
0	The measure of the interior angle of the regular octagon =°
(	The number of diagonals of the pentagon =
0	The quadrilateral in which two sides are parallel is called
(	In a parallelogram, every two opposite sides are,
0	ABCD is a parallelogram in which m ( $\angle A$ ) = 70°, then m ( $\angle B$ ) =°
0	The parallelogram whose two diagonals are equal in length is called
(	The parallelogram whose two diagonals are equal in length and perpendicular is called
0	The quadrilateral whose sides are equal in length is called
0	The rectangle is a with a right angle.
(	The square is a with a right angle.
0	The square is a in which its diagonals are perpendicular.
0	If XYZL is a rhombus, then
0	The rhombus whose perimeter is 82 cm., its side length = cm.
0	The sum of measures of the interior angles of a triangle = ······ °
0	B The measure of the exterior angle of a triangle is equal to the sum of
6	is In $\triangle$ ABC: If m ( $\angle$ A) + m ( $\angle$ C) = m ( $\angle$ B) , then m ( $\angle$ B) =°
(	The ray drawn from the midpoint of a side of a triangle parallel to another side
(	The length of the line segment joining the midpoints of two sides of a triangle equals
6	2 In the right-angled triangle, the area of the square on the hypotenuse equals
(	A rhombus whose diagonals lengths are 16 cm. and 12 cm., then its side length = cm.
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#### 2 Complete the following:

- (11) The image of the point (-3,2) by reflection in y-axis is .........
- (2) The reflection in a plane reserves: ....., , ......

The measure of the equals	ne exterior angle of the ed	quilateral triangle at	any one of its vertices
(a) 60°	(b) 120°	(c) 150°	(d) 30°
then DE =	953799 (SAS)		576 100 000 0000
(a) 16	(b) 8	(c) 4	(d) 2
	length 4 cm. and width 3	cm., then the length	of its diagonal
= ······· cm. (a) 25	(b) 3	(c) 4	(d) 5
In Δ ABC, if m (	$\angle A$ ) = 90°, BC = 25 cm	n. and AC = 20 cm.,	then AB = ····· cm.
(a) 20	(b) 25	(c) 10	(d) 15
Choose the correct	answer from those give	n :	100 201
The image of the	point $(-3, -5)$ by reflect	ction in the X-axis is	<b></b> 1
(a) $(3, -5)$	(b) (3,5)	(c) (-3,5)	(d) (-3,-5)
The number of ax	es of symmetry of the eq	uilateral triangle is .	
(a) zero	(b) 1	(c) 2	(d) 3
The image of the	point (2, -7) by reflecti	on in the origin poin	t is
(a) (2,7)	(b) (-2,7)	(c) $(-2, -7)$	(d) $(2, -7)$
If A is the image of	f A by reflection in M and	MA = 6  cm., then A.	À =
(a) 6 cm.	(b) 3 cm.	(c) 12 cm.	(d) 9 cm.
	point (-2 , 3) by translation	The state of the s	units in the negative
(a) (2,3)	(b) (-2,7)	(c)(-6,3)	(d) $(-2, -1)$
<b>(B)</b> If A (4, −5) is the point A is	e image of A by translation	$n(x,y) \longrightarrow (x-2)$	(2, y + 1), then the
Ž	(b) $(4, -4)$	(c) $(2, -4)$	(d) (6, -6)
The image of the measure 90° is	point (-4,2) by rotatio	n around the origin p	ooint with an angle of
	(b) $(-2, -4)$	(c) $(4, -2)$	(d) $(2, -4)$
The image of the measure – 90° is	square by rotation around	₹ <del>5</del> 77 <del>5</del> .	th an angle of
Market and a said a said	(b) a square		(d) a trapezium
The image of the measure 180° is	triangle by rotation arous	nd the origin point w	ith an angle of
(a) a triangle	(b) a line segment	(c) a point	(d) a straight line

- (10) If the image of the point (5, -2) by rotation around the origin point is the same point , then the measure of the rotation angle = ......
  - (a) 90°

- (b) 180°
- (c) 270°
- (d) 360°

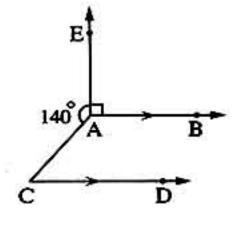
## Third: Essay questions

1 In the opposite figure : AB // CD,  $m (\angle EAC) = 140^{\circ}$ 

and m ( $\angle$  EAB) = 90°

Find:

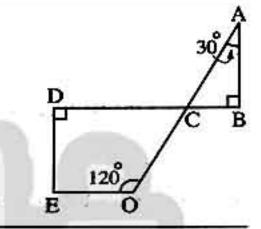
- m (∠ BAC)
- (2) m (4 C)



2 In the opposite figure:

AB \( BD \), ED \( DB \)  $, \overline{BD} \cap \overline{AO} = \{C\}, m(\angle A) = 30^{\circ}$ and m ( $\angle$  EOC) = 120°

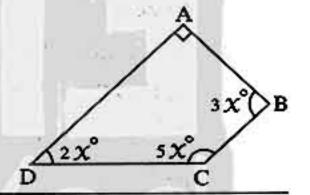
Find:  $m (\angle E)$ 



3 In the opposite figure :

ABCD is a quadrilateral in which m ( $\angle A$ ) = 90°

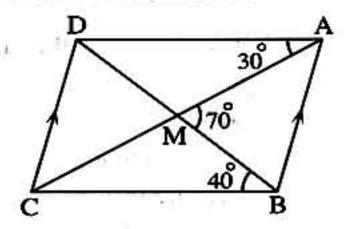
Find the value of : X



- 4 If the measure of the exterior angle of a regular polygon is 45°, how many sides does it have? What is the sum of the measures of its interior angles?
- 5 In the opposite figure:

ABCD is a quadrilateral where  $AC \cap BD = \{M\}$ , AB // DC,  $m (\angle AMB) = 70^{\circ}$ ,  $m (\angle MBC) = 40^{\circ}$ and m ( $\angle$  MAD) = 30°

Prove that: ABCD is a parallelogram.



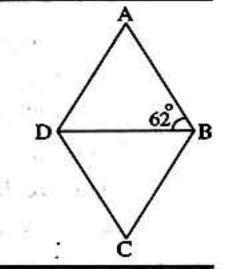
6 In the opposite figure :

ABCD is a rhombus,

BD is a diagonal in it,

 $m (\angle ABD) = 62^{\circ}$ .

Find with proof :  $m (\angle A)$ 



هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

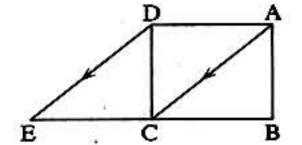
General Exercises

7 In the opposite figure:

ABCD is a square,  $E \in \overline{BC}$ ,  $\overline{AC} // \overline{DE}$ 

**Prove that:** ACED is a parallelogram.

**②** Find : m (∠ ACE)

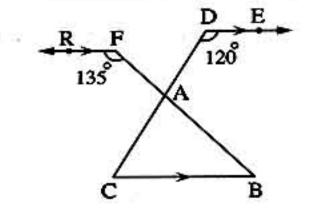


8 In the opposite figure:

DE // FR // BC,

m ( $\angle$  CDE) = 120° and m ( $\angle$  RFB) = 135°

Calculate the measures of the angles of :  $\triangle$  ABC



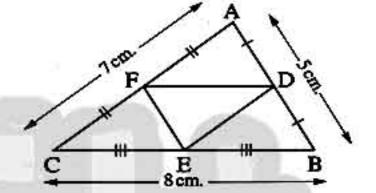
9 In the opposite figure :

AB = 5 cm., BC = 8 cm.,

AC = 7 cm., D, E and F are the midpoints of

AB, BC and CA respectively.

Calculate the perimeter of :  $\triangle$  DEF



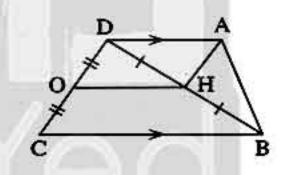
10 In the opposite figure:

 $\overline{AD} // \overline{BC}$ ,  $AD = \frac{1}{2} BC$ ,

H is the midpoint of BD,

O is the midpoint of CD.

Prove that: AHOD is a parallelogram.

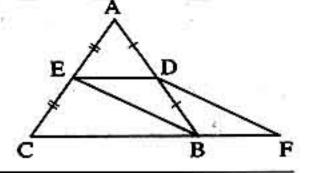


[11] In the opposite figure:

D and E are the midpoints of  $\overline{AB}$  and  $\overline{AC}$  respectively,

 $F \in \overrightarrow{CB}$  where  $BF = \frac{1}{2}BC$ 

Prove that: BEDF is a parallelogram.



12 In the opposite figure :

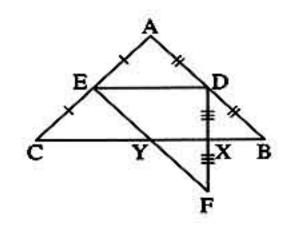
D is the midpoint of  $\overline{AB}$ ,

E is the midpoint of  $\overline{AC}$ ,

 $\overline{DF} \cap \overline{BC} = \{X\}, DX = XF,$ 

BC = 12 cm.

Find the length of: XY



# Unit 3

## 13 In the opposite figure:

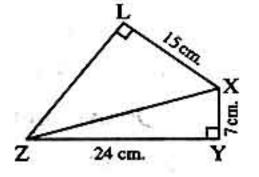
XYZL is quadrilateral in which:

$$m (\angle XYZ) = m (\angle XLZ) = 90^{\circ}$$

$$XY = 7 \text{ cm.}$$
  $YZ = 24 \text{ cm.}$ 

and XL = 15 cm.

Find the length of each of :  $\overline{XZ}$  and  $\overline{LZ}$ 



#### 14 In the opposite figure:

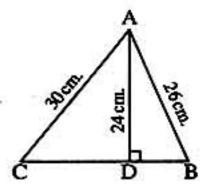
ABC is a triangle in which: AD ⊥ BC

If 
$$AD = 24 \text{ cm.}$$
,  $AB = 26 \text{ cm.}$ 

and AC = 30 cm.

Find: BC

Calculate the area of : Δ ABC



- Draw the image of  $\triangle$  ABC in which: AB = 3 cm., BC = 4 cm. and AC = 5 cm. by reflection in the straight line containing the greatest side.
- Draw the image of Δ ABC where A (0,0), B (4,1) and C (-1,3) by reflection in the y-axis.
- Draw the triangle ABC in which: A(1,-1), B(2,3) and C(0,4), then find its image by reflection in the origin point.
- 18 Δ ABC is right-angled at B where AB = 3 cm. and BC = 4 cm. If Δ ABC is the image of Δ ABC by translation of a distance 3 cm. in the direction of CB

  Prove that: The figure AACC is a parallelogram.
- Draw  $\triangle$  ABC in which: A (1, 1), B (4, -2) and C (6, 3), then find its image by rotation R (O, -90°).

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# Worksheet on lesson 1 unit 3

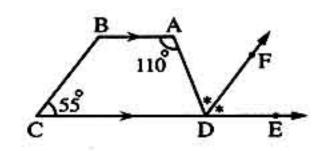
#### Answer the following questions:

#### 1 In the opposite figure:

$$\overrightarrow{AB} / / \overrightarrow{CD}, E \in \overrightarrow{CD}, m (\angle A) = 110^{\circ}$$

$$m (\angle C) = 55^{\circ}$$
,

DF bisects ∠ ADE



## Complete the following proof to prove that DF // BC

#### Proof:

- : AB // ..... , AD is a transversal to them
- ∵ DF bisects ∠ .....
- ∴ m (∠ EDF) = m (∠ .....) = ......°
- $m (\angle \dots ) = m (\angle C)$  but they are  $m (\angle C)$
- ∴ DF // ....

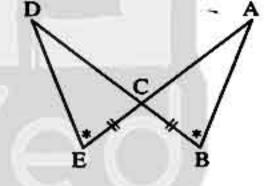
(Q.E.D)

#### 2 In the opposite figure:

$$\overline{AE} \cap \overline{BD} = \{C\}, BC = CE$$

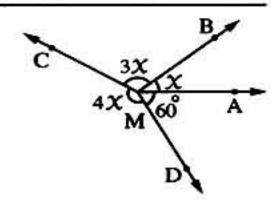
$$m (\angle B) = m (\angle E)$$
 prove that :

- (1) AB = DE
- (2) AE = BD



## 3 In the opposite figure :

Find by proof the value of X



کراسة المعاصر ریاضیات (لغات) ۱/ إعدادی / تیرم ۲ (۲ : ۲)

The second section of the second section is a second section of the second section in the second section is a second section of the second section in the second section is a second section of the second section in the second section is a second section of the second section in the second section is a second section of the second section in the second section is a second section of the second section is a second section of the second section is a second section in the second section is a second section of the second section of the second section is a second section of the second section of the second section of the second section of the section of th

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلود

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# Worksheet 2 till lesson 2 unit 3

#### Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The sum of measures of the interior angles of a polygon with n sides = .........

- (b)  $n \times 180^{\circ}$  (c)  $(n-2) \times 180^{\circ}$  (d)  $\frac{(n-2) \times 180^{\circ}}{2n}$
- (2) The measure of the interior angle of the regular octagon equals ......
  - (a) 1080°
- (b) 180°
- (3) The sum of measures of the accumulative adjacent angles at a point = ......

(c) 135°

(d) 108°

- (a) 180° (b) 90° (c) 360° (d) 270° (4) The sum of measures of the exterior angles of a triangle = .........
  - (a) 180°
- (b) 360°
- (c) 90°
- (d) 100°
- (5) If the measure of an interior angle of a regular polygon = 120° then the number of its sides = .....
  - (a) 3

(b) 4

- (c) 5
- (d) 6

- (B) The two vertically opposite angles are ........
  - (a) complementary. (b) supplementary. (c) adjacent.
- (d) equal in measure.

#### 2 Complete the following:

- (1) The sum of measures of the interior angles of heptagon = .........
- (2) In the opposite figure:

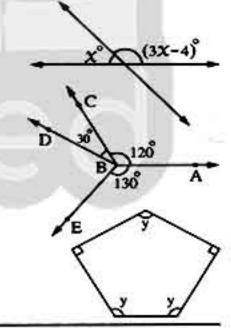
(3) In the opposite figure:

$$m (\angle ABC) = 120^{\circ} \cdot m (\angle CBD) = 30^{\circ}$$

$$m (\angle ABE) = 130^{\circ}$$
,

then m (
$$\angle$$
 EBD) = ·········°

(4) In the opposite figure:

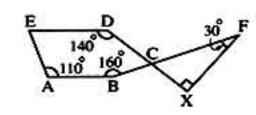


#### 3 In the opposite figure:

$$\overline{BF} \cap \overline{DX} = \{C\}, \overline{FX} \perp \overline{DX}, m (\angle F) = 30^{\circ}$$

$$m (\angle B) = 160^{\circ} m (\angle D) = 140^{\circ} m (\angle A) = 110^{\circ}$$

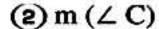
Prove that : AB // ED

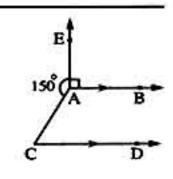


#### 4 In the opposite figure:

$$\overrightarrow{AB} // \overrightarrow{CD}$$
, m ( $\angle EAC$ ) = 150°

(1) m (\( \subseteq \text{BAC} \)







هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع



# The answer of worksheet 2



1	Shade	the	circle	that 1	represents	vour	choice	for	the	correct	answer	
	,	~~~				J					A TOTAL CONTRACTOR OF THE PARTY	7

- (1)(a)
- **b**
- (c)
- **d**

(2)(2·)

(3)(a)

**b** 

**(b)** 

0

(C)

0

- (4)(a)
- **(b)**
- 0
- **d**

- (5) (a)
- **(b)**
- 0
- <u>u</u>

- (B) (a)
- **b**
- 0
- **d**



- (s) .....
- (3) .....
- (4) .....

بذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى [طعمولية



Answer	the	following	questions:	
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## 1 Choose the correct answer from those given:

- (1) ABCD is a parallelogram in which:  $m (\angle A) = 120^{\circ}$ , then  $m (\angle B) = \dots$ 
  - (a) 120°

- (b) 180°
- (c) 60°
- (d) 100°
- (2) The measure of the interior angle of the regular hexagon = .........
  - (a) 108°

- (b) 120°
- (c) 135°
- (d) 90°
- (3) The sum of the measures of the exterior angles of a polygon with n sides = .........
  - (a) 90°

- (b) 180°
- (c)  $(n-2) \times 180^{\circ}$  (d)  $360^{\circ}$
- (4) If ABCD is a parallelogram whose perimeter = 24 cm. and AB = 8 cm. , then BC = ..... cm.
  - (a) 8
- (b) 4
- (c) 6
- (d) 10
- (5) The sum of the measures of four accumulative angles at a point ...... the sum of the measures of five accumulative angles at a point.
  - (a) =

- (b) <
- (c) >
- (d) ≠
- (6) The sum of the measures of the interior angles of the quadrilateral equals the measure of .....
  - (a) two right angles

(b) three right angles

(c) four right angles

(d) right angle

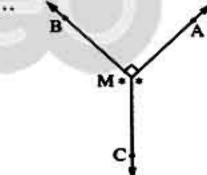
## 2 Complete the following:

- (1) If two straight lines intersect, then each two vertically opposite angles are .........
- (2) If ABCD is a parallelogram in which m (∠ A) + m (∠ C) = 110°, then m (∠ D) = ·······°
- (3) The quadrilateral in which there are two parallel sides is called .........
- (4) In the opposite figure:

MB L MA,

MC bisects ∠ AMB (reflex angle)

, then m (∠ AMC) = ......°

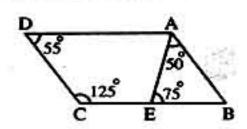


#### 3 In the opposite figure :

 $E \in BC$ ,  $m (\angle BAE) = 50^{\circ}$ 

 $m (\angle AEB) = 75^{\circ} , m (\angle D) = 55^{\circ} , m (\angle C) = 125^{\circ}$ 

Prove that: the figure ABCD is a parallelogram.

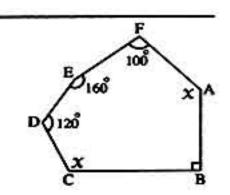


## 4 In the opposite figure:

ABCDEF is a hexagon and

 $m (\angle A) = m (\angle C) = X$ 

Find the value of X



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# The answer of worksheet



1	Shade	the circ	le that	represents	your	choice	for	the	correct	answer	:
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- (1)(a)
- (C)
- **(d)**

- (2)(a)

- **d**

(3)(a)

(4)(a)

ⓒ

**d** 

**d** 

- (5) (a)
- 0
- **(d)**

- (B) (a)
- **(b)**
- **d**)



# Worksheet (2) till lesson 4 unit 3

#### Answer the following questions:

1	Choose	the	correct	answer	from	those	given	9
---	--------	-----	---------	--------	------	-------	-------	---

- (1) If ABCD is a parallelogram,  $m (\angle A) = 80^{\circ}$ , then  $m (\angle C) = \dots$ 
  - (a) 80°

- (b) 120°
- (c) 100°
- (d) 60°
- (2) A rhombus of side length 8 cm. , its perimeter = ........
  - (a) 16 cm.
- (b) 24 cm.
- (c) 32 cm.
- (d) 64 cm.
- (3) If two adjacent sides in a rectangle are equal in length, then it will be ......
  - (a) a square.
- (b) a rhombus.
- (c) a rectangle.
- (d) a trapezium.

- (4) If ABCD is a square, then m (∠ CAB) = ········°
  - (a) 30°

- (b) 45°
- (c) 60°
- (d) 90°
- (5) ..... is a parallelogram in which one of its angles is a right angle.
  - (a) The rectangle
- (b) The square
- (c) The rhombus
- (d) The trapezium
- (6) The measure of the interior angle of a regular octagon = .........
  - (a) 120°
- (b) 108°
- (c) 135°
- (d) 140°

#### 2 Complete the following:

- (1) The quadrilateral in which the two diagonals bisect each other is called .........
- (2) The two diagonals in ...... and ..... are equal in length.
- (4) The polygon which has an interior reflex angle is called .......

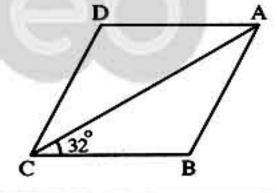
#### 3 In the opposite figure:

ABCD is a rhombus,

AC is a diagonal in it

 $m (\angle ACB) = 32^{\circ}$ 

Find:  $m(\angle D)$ 



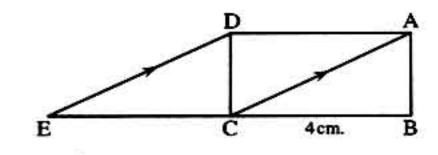
4 [a] If the measure of the exterior angle of a regular polygon equals 30°, what is the number of sides of this polygon and what is the sum of measures of its interior angles?

#### [b] In the opposite figure:

ABCD is a rectangle:

AC // DE , E ∈ BC

- (1) Prove that : ACED is a parallelogram
- (2) Find: the length of CE





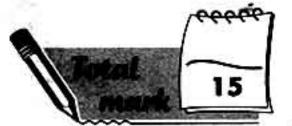
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# The answer of worksheet





Shade the circle that represents your choice for the correct an	swer:
---	-------

- (1)(a)

- (2)(a)

- **d**

(4)(a)

(3)(a)

- 0

0

**d** 

- (5) (a)
- 0
- **d**

- (6) (a)
- 0

2 ①	
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## Answer the following questions:

#### Choose the correct answer from those given:

- (1) The sum of measures of the interior angles of the triangle = .......
  - (a) 108°
- (b) 180°
- (c) 630°
- (d) 360°
- (2) If the measures of two angles in a triangle are 40° and 45°, then the triangle is .........
  - (a) acute-angled
- (b) right-angled (c) obtuse-angled
- (d) equilateral
- (3) In the parallelogram ABCD, if ∠ A is acute, then ∠ C is .........
  - (a) acute.

(b) obtuse.

(c) right.

- (d) reflex.
- (4) The parallelogram in which one of its angles is right is ........
  - (a) a trapezium.
- (b) a square.
- (c) a rhombus.
- (d) a rectangle.
- (5) The measure of the exterior angle of the equilateral triangle = ..........
  - (a) 30°

- (b) 60°
- (c) 90°
- (d) 120°
- (6) The number of sides of the regular polygon in which the measure of an interior angle = 120° is ......
  - (a) 5

(b) 6

(c)7

(d) 8

#### 2 Complete the following:

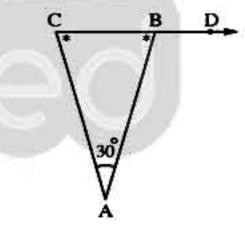
- 1) The measure of the exterior angle of the triangle equals ..........
- (2) In the opposite figure:

 $D \in CB$ ,  $m(\angle A) = 30^{\circ}$ ,

then m (∠ ABD) = ..... °

(3) In the parallelogram ABCD, if  $m (\angle A) = \frac{1}{2} m (\angle B)$ , then  $m (\angle B) = \dots$ 

(4) The two diagonals of the rhombus are ...... and .......

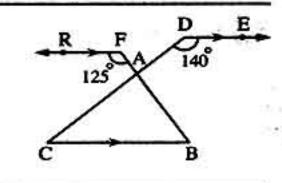


#### In the opposite figure :

DE // FR // BC

 $m (\angle D) = 140^{\circ} \cdot m (\angle F) = 125^{\circ}$ 

Calculate the measures of the angles of  $\triangle$  ABC



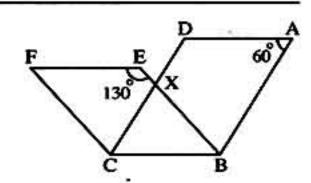
## In the opposite figure :

ABCD and EBCF are two

parallelograms,  $m (\angle A) = 60^{\circ}$ 

 $m (\angle E) = 130^{\circ}$ 

**Find**: by proof m ( $\angle$  BXC)





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ALL SECTION	The answer	of worksh	eet 5	Metal man	15
1 Shade the cire	cle that represents	your choice for	the correct ans	wer:	
(1) (a)	<b>b</b>	(C)	<b>d</b>	5	
(2) (a)	<b>b</b>	©	<b>d</b>		
(3) (a)	<b>b</b>	- C	<b>d</b>		3
(4)(a)	<b>b</b>	©	<b>d</b>		
(5) (a)	<b>b</b>	©	<b>d</b>		
(B) (a)	<b>(b)</b>	©	<b>d</b>		
2 ①					
(S)					_
(a)	a chin	A 1944		Arried .	1-

	(S)	
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	(4)	
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# Worksheet 6 till lesson 6 unit 3

#### Answer the following questions:

#### 1 Choose the correct answer from those given :

- (1) The sum of measures of the interior angles of the heptagon = .........
  - (a) 540°
- (b) 720°
- (c) 900°
- (d) 180°
- (2) The side length of a rhombus is 5 cm., then its perimeter = ...... cm.
  - (a) 10

- (b) 15
- (c) 20

(d) 25

- (3) The concave polygon should has a ..... angle. (b) right (c) obtuse
  - (a) acute

(b)  $80^{\circ}$ 

(c) 100°

(4) ABCD is a parallelogram in which m ( $\angle A$ ) + m ( $\angle C$ ) = 160°, then m ( $\angle B$ ) = ......

(d) 110°

(d) reflex

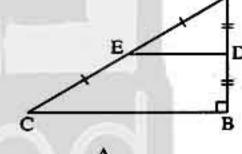
- (a) 20° (5) The sum of measures of the interior angles of the triangle = the measure of ......... angle.
  - (a) a right.
- (b) a straight.
- (c) acute.
- (d) reflex.
- (6) The length of the line segment joining the midpoints of two sides of a triangle equals ..... the length of the third side.
  - (a)  $\frac{1}{4}$

- (b) twice
- (c)  $\frac{1}{2}$
- (d)  $\frac{1}{3}$

#### 2 Complete the following:

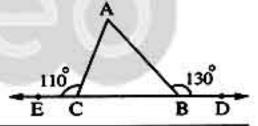
- (1) The measure of each interior angle in a regular polygon of n sides = .........
- (2) The ray which is drawn from the midpoint of a side of a triangle parallel to one of the other sides .....
- (3) In the opposite figure:

If m ( $\angle$  B) = 90°, D and E are the midpoints of AB and AC respectively then m (\( \alpha \text{ ADE} \) = .............°



(4) In the opposite figure:

If  $D \in CB$  and  $E \in BC$ , then m  $(\angle A) = \dots \circ$ 



## 3 In the opposite figure:

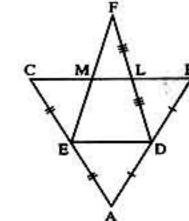
D is the midpoint of AB,

E is the midpoint of  $\overline{AC}$ ,

L is the midpoint of FD

BC = 20 cm.

Find: the length of LM

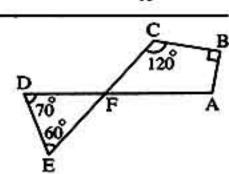


## 4 In the opposite figure :

 $AD \cap CE = \{F\}$ ,  $m (\angle B) = 90^{\circ}$ 

 $m (\angle C) = 120^{\circ}, m (\angle E) = 60^{\circ}, m (\angle D) = 70^{\circ}$ 

Find:  $m (\angle A)$ 



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# The answer of worksheet 6





1	Shade the ci	ircle that represents	your choice for	r the correct :	answer :
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- (1) (a)

- **d**

- (2) (a)

- (3) (a) (4) (a)
- **b**
- 0
- **d**

- (5) (a)
- **b**
- **d**

**d** 

- (6) (a)
- **(b)**
- 0

2 (1)	 	 	

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# Worksheet till lesson 7 unit 3

#### Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The measure of the interior angle of a regular hexagon = .........
  - (a) 120°
- (b) 102°
- (c) 180°
- (d) 360°
- (2) In  $\triangle$  ABC, if m ( $\angle$  A) = m ( $\angle$  B) = 50°, then m ( $\angle$  C) = ......
  - (a) 130°
- (b) 100°
- (c) 80°
- (d) 50°
- (3) The parallelogram whose one of its angles is aright angle is called ...........
  - (a) trapezium.
- (b) square.
- (c) rhombus.
- (d) rectangle.
- (4) A rectangle whose length = 4 cm. and width = 3 cm., then the length of its diagonal = ..... cm.
  - (a) 3

(b) 4

(c) 5

- (d) 25
- (5) The number of sides of the regular polygon which the measure of one of its interior angles is 144° = .....
  - (a) 4 sides.
- (b) 6 sides.
- (c) 8 sides.
- (d) 10 sides.
- (6) In  $\triangle$  ABC, if m ( $\angle$  B) = m ( $\angle$  A) + m ( $\angle$  C), then  $\angle$  B is ......
  - (a) acute.
- (b) right.
- (c) obtuse.
- (d) reflex.

#### 2 Complete the following:

- (1) In the right-angled triangle, the area of the square on the hypotenuse equals ..........
- (2) The square is ..... with a right angle.
- (3) The line segment joining the midpoints of two sides of a triangle is ...... the third side and its length equals .....
- (4) If ABCD is a parallelogram in which m (∠ A) = 40°, then m (∠ B) = ·······°

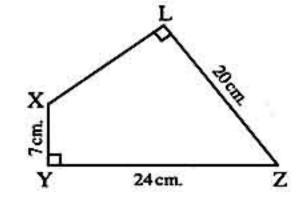
#### 3 In the opposite figure :

$$m (\angle Y) = m (\angle L) = 90^{\circ}$$

$$XY = 7 \text{ cm.} YZ = 24 \text{ cm.}$$

and LZ = 20 cm.

Find: the length of XL



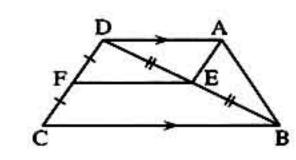
## 4 In the opposite figure:

 $\overline{AD} // \overline{BC} , AD = \frac{1}{2} BC$ 

, E is the midpoint of BD

and F is the midpoint of CD

Prove that: AEFD is a parallelogram.



خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على موا





الصف الأول الأعدادي



# The answer of worksheet



93		THE GHOVE	OI WOIRSHEE		mar	15
[1]	Shade the circle	e that represents y	our choice for th	e correct ans	wer:	
	①(a)	<b>(b)</b>	©	<b>d</b>		
	(s) (a)	Ъ	©	<b>d</b>		
	(3)(a)	Ъ	©	<b>d</b>		3
	(4) (a)	<b>b</b>	©	<b>d</b>		
	(5) (a)	<b>b</b>	©	<b>d</b>		930
	(6) (a)	<b>b</b> .	©	<u>d</u>		
2	① ····································					
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	(3)		,			2
	<b>(4)</b>					
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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى



#### Answer the following questions:

#### Choose the correct answer from those given :

(1) The sum of measures of the interior angles of the hexagon = .........

(b) 5 right angles.

- (a) 4 right angles.
- (c) 6 right angles.
- (d) 8 right angles.

- (2) If ABCD is a square, then  $(AC)^2 = \dots$ 
  - (a) AB

- (b)  $(AB)^2$
- (c)  $2 (AB)^2$
- $(d) 4 (AB)^2$
- (3) In  $\triangle$  ABC, if m ( $\angle$  B) =  $\frac{1}{2}$  m ( $\angle$  A) = 30°, then the triangle will be ..... triangle.
  - (a) acute-angled
- (b) right-angled (c) equilateral (d) isosceles
- (4) The image of the point (1, 2) by the transformation  $(x, y) \longrightarrow (x, -y)$  is .......
  - (a) (-1, 2)
- (b) (-1, -2)
- (c) (1, -2)
- (d) (2,-1)
- (5) The sum of measures of the exterior angles of a polygon of n sides equals .........
  - (a) 180°
- (b) 360°
- (c)  $(n-2) \times 180^{\circ}$
- (d)  $\frac{(n-2) \times 180}{r}$
- (6) In  $\triangle$  ABC, if D and E are the midpoints of AB and AC respectively and BC = 8 cm., then  $DE = \cdots cm$ .
  - (a) 16

- (b) 12
- (c) 4

(d)2

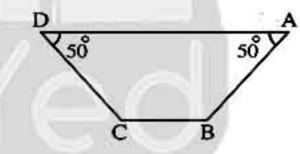
#### 2 Complete the following:

- (1) If two straight lines intersect, then each two vertically opposite angles are ..........
- (2) If  $\triangle XYZ$  is a right angled triangle at Z, then  $(XZ)^2 =$
- (3) In the opposite figure:

 $m (\angle A) = m (\angle D) = 50^{\circ}$ 

AB and DC intersect at E not shown in the figure.

, then m  $(\angle E) = \cdots$ 



- (4) The quadrilateral in which two opposite sides are parallel is ..........
- [a] If the ratio among the measures of the interior angles of a quadrilateral is 2:2:3:5, find the measure of the greatest angle in the quadrilateral.

## [b] In the opposite figure:

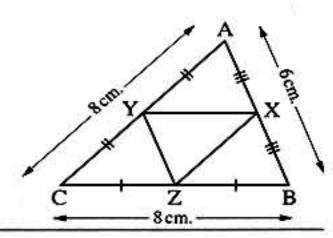
ABC is a triangle in which

X , Y and Z are the midpoints

of AB, AC and BC respectively

It AB = 6 cm., BC = 8 cm., AC = 8 cm.,

- (1) calculate the perimeter of  $\Delta XYZ$
- (2) determine the type of the figure XYCZ



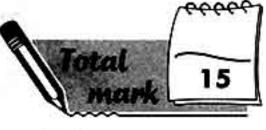
On lattice, draw Δ ABC where A (1, 2), B (4, 2), C (4, 4), then map its image by the transformation  $(x, y) \longrightarrow (y, -x)$ 



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# The answer of worksheet 8



- (1) (a)
- **b**
- (C)
- (d)

(2) (a)

(3)(a)

- 0
- 0
- (d)

- (4)(a)
- (p)
- 0
- **d**

(6) (a)

(5) (a)

- **(b)**
- 0
- **d**



- **(2)** ·
- (3) ...
- 4

30



#### Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The number of axes of symmetry of the square is .........
  - (a) 1

(b) 2

- (c) 3
- (d) 4
- (2) The image of the point (3, -5) by the reflection in X-axis is .......
  - (a)(3,5)

(a) 40°

(3) ABC is a triangle in which m ( $\angle A$ ) = 60°, m ( $\angle B$ ) = 2 m ( $\angle C$ ), then m ( $\angle B$ ) = ......

(b) 60°

- (c) 70°
- (d) 80°
- (4) The image of the point (2,3) by the reflection in y-axis is .........
  - (a) (-2,3)
- (b) (2, -3)
- (c) (-2, -3)

(b) (-3,5) (c) (-3,-5) (d) (3,-5)

- (d)(3,2)
- (5) The sum of measures of the exterior angles of the octagon = ........
  - (a) 540°
- (b) 360°
- (c) 720°
- (d) 1080°
- (B) ABC is a right angled triangle at B in which AB = 3 cm. and BC = 4 cm. , then AC = ..... cm.
  - (a) 2.5

(b) 5

- (c) 16
- (d) 9

#### 2 Complete the following:

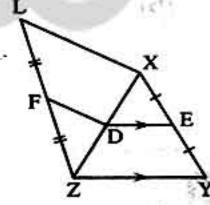
- (1) The measure of the exterior angle of the triangle equals .........
- (2) The image of the point (-5, 4) by the transformation  $(x, y) \longrightarrow (-y, x)$  is ......
- (3) If ABCD is a rhombus, then ...... \pm .....
- (4) The reflection in a straight line keeps ......, ......, ......

#### [a] In the opposite figure:

 $XE = EY \cdot \overline{ED} // \overline{YZ}$ 

F is the midpoint of ZL

Prove that : DF // XL

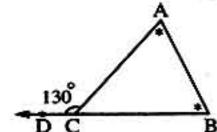


## [b] In the opposite figure:

ABC is a triangle , D∈BC

 $m (\angle ACD) = 130^{\circ}$ 

Find:  $m (\angle B)$ 



#### On lattice, find the image of $\triangle$ ABO where

A(2,2), B(4,2), O(0,0) by reflection in y-axis.



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# The answer of worksheet



Shade the circle that represents your choice for the correct answ	er:
---	-----

- (1)(a)

- (2)(a)

(4)(a)

(3)(a)

**b** 

**(b)** 

- 0
- **d d**

(B) (a)

(5) (a)

**b** 

**b** 

- **d**
- - (3) .....



# Worksheet 10 till lesson 10 unit 3

#### Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The point (2, -4) is the image of the point ........ by reflection in the origin point.
  - (a)(2,4)
- (b) (-2,4)
- (c) (-2,-4)
- (d) (2, -4)
- (2) The measure of the exterior angle of a triangle is ...... the measure of any interior angle of the triangle except its adjacent angle.
  - (a) >

(c) =

(d) ≤

- (3) If ABCD is a rectangle, then AC = .....
  - (a) AB

- (b) BC
- (c) BD
- (d) CD
- (4) The parallelogram whose two diagonals are perpendicular and the measure of one of its angles is 90° is called .....
  - (a) rectangle.
- (b) rhombus.
- (c) square.
- (d) trapezium.
- (5) The number of axes of symmetry of the rectangle is ........
  - (a) 1

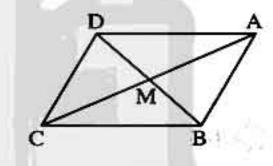
(b) 2

(d)4

#### (6) In The opposite figure:

If ABCD is a parallelogram, then the image of  $\triangle$  AMD by reflection in the point M is  $\triangle$  .......

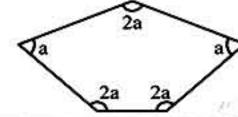
- (a) AMB
- (b) DMC
- (c) CMB
- (d) DMA



## 2 Complete the following:

- (1) If the reflection in a straight line transforms the figure to itself, then this straight line is called .....
- (2) The sum of the measures of the accumulative angles at a point is .........
- (3) The ray drawn from the midpoint of a side of a triangle parallel to another side ....... the third side.
- (4) In the opposite figure:

The value of  $a = \dots$ 



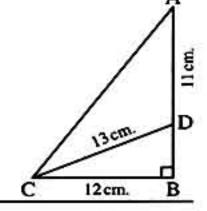
## 3 In the opposite figure :

ABC is a triangle in which  $m (\angle B) = 90^{\circ}$ 

 $D \in AB$ , where AD = 11 cm. BC = 12 cm.

and DC = 13 cm.

Find the length of : BD and AC



- 4 Draw on a lattice Δ ABC, where A (5, 1), B (2, 1) and C (5, 3), then draw its image by reflection in the origin point.



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# The answer of worksheet (10)

Total 15

1	Shade	the circle	that represents	your c	hoice for	the correct	answer:
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- (1) (a)
- **(b)**
- **d**

(2) (a)

(3) (a)

- **b b**
- (C) ©
- **d**

**d** 

- (4)(a)
- **b**

**b** 

- 0
- (d)

**d** 

(**6**) (**a**)

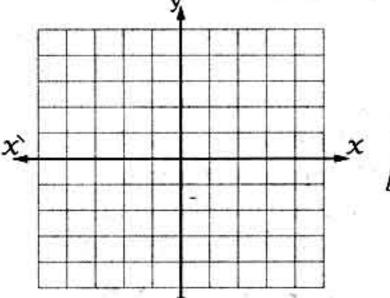
(5) (a)

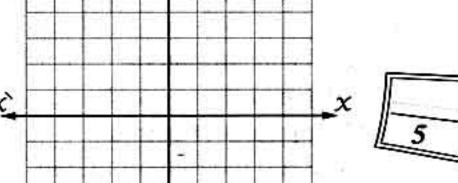
- **b**
- © ©
- **d**



......

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	/ 1





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# Worksheet till lesson 11 unit 3

#### Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) ABC is a triangle in which m ( $\angle A$ ) = 4  $X^{\circ}$ , m ( $\angle B$ ) = 2  $X^{\circ}$  and m ( $\angle C$ ) = 3  $X^{\circ}$ , then ∠ A is ......
  - (a) acute.
- (b) right.
- (c) obtuse.
- (d) reflex.
- (2) The quadrilateral in which each two opposite sides are equal in length is .......... (a) a parallelogram. (b) a trapezium.
  - (c) a square.
- (d) a rectangle.
- (3) The image of the point (-2,3) by a translation of magnitude 5 units in the positive direction of the X-axis is ......
  - (a) (-2, -2)
- (b) (-7,3)
- (c)(-2,8)
- (d)(3,3)
- (4) The image of the point (0,5) by reflection in the X-axis is ........
  - (a) (0,5)
- (b) (0, -5)
- (c)(5,0)
- (d)(-5,0)
- (5) The image of the point (x, -y) by reflection in the origin point is .......
  - (a) (X, y)
- (b) (-x, y)
- (c) (x, -y) (d) (-x, -y)
- (6) If A (3,5) is the image of the point A by the translation (x,y) = (x+4,y-2), then the point A is ......
  - (a) (7,3)
- (b) (7,7)
- (c)(-1,7)
- (d)(-1,3)

#### 2 Complete the following:

- (1) If the measure of an exterior angle of a regular polygon = 30°, then the number of sides of the polygon = .....
- (2) The line segment which joins the two midpoints of the two sides of a triangle ...... and .....
- (3) The translation keeps ......
- (4) The translation is determined by two things, they are ........ and ..........
- 3 On lattice, draw  $\triangle$  ABC where A (-3,2), B (-1,1) and C (-2,4) then draw its image.
  - (1) by the translation  $(x, y) \longrightarrow (x + 4, y 3)$
  - (2) by reflection in X-axis.

#### 4 [a] In the opposite figure:

ABCD is a quadrilateral in which

 $m (\angle A) = 120^{\circ} \cdot m (\angle B) = 80^{\circ}$ 

Δ CEF is an equilateral

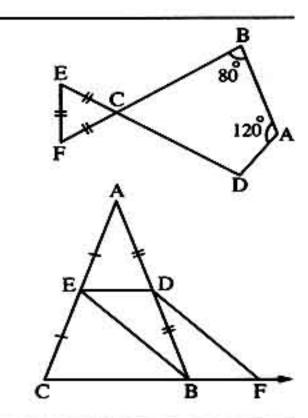
Find by proof:  $m (\angle D)$ 

[b] In the opposite figure:

D and E are the two midpoints of AB and AC respectively,

 $F \in \overline{CB}$  where  $BF = \frac{1}{2}BC$ 

Prove that: the figure BEDF is a parallelogram.



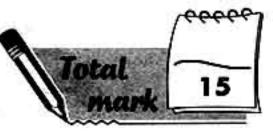


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# The answer of worksheet



[1	Shade the circ	e that represents	your choice	for the	correct	answer	:
----	----------------	-------------------	-------------	---------	---------	--------	---

- (1)(a)
- **(b)**
- ©
- **d**

(2) (a)

(3) (a)

- ©
- (d)

- (4) (a)
- **b**
- ©

0

(d)

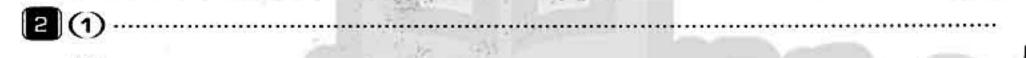
(6) (a)

(5) (a)

**(b)** 

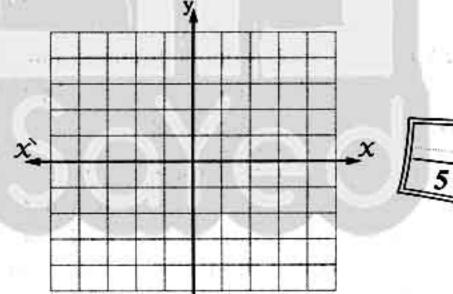
**b** 

- 0
- **d**



- (e) ..
- (3) ..
- (4)





4 [a] ······

74.000

.. 5

45

Final Examinations

#### Model Examinations of the school book

# Model

Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The sum of the measure of interior angle of a triangle equals ......
  - (a) 90°
- (b) 180°
- (c) 270°
- (d) 360°
- (2) The image of the point (-1,3) by translation (4,-2) is ......
  - (a)(3,1)
- (b) (3, -1)
- (c)(5,1)
- (3) The measure of the exterior angle of the equilateral triangle is .........
  - (a) 30°
- (b) 45°
- (c) 60°
- (d) 120°
- (4) In a parallelogram if the adjacent sides are equal in the length, then the shape is ..........
  - (a) square.
- (b) rhombus.
- (c) rectangle.
- (d) trapezium.
- (5) The number of the diagonals of a pentagon is ......
  - (a) 3
- (b) 5
- (c) 7
- (d) 9

#### 2 Complete the following:

- (1) The image of the point (2, 1) by reflection in X-axis is .......
- (2) The image of the point (2, -1) by rotation about the origin point with an angle of measure 180° is .....
- (3) The square is a rectangle in which ......
- (4) ABCD is a parallelogram in which m ( $\angle A$ ) = 60°, then m ( $\angle B$ ) = ......
- (5) The image of the point (5,3) by translation:  $(x,y) \longrightarrow (x+3,y-1)$  is ......

## [3] [a] In the opposite figure :

$$m (\angle A) = m (\angle B) = 25^{\circ}$$

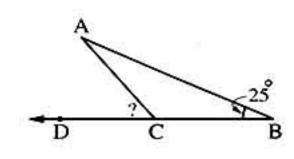
Find:  $m (\angle ACD)$ 

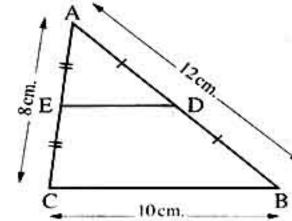
#### [b] In the opposite figure:

 $\triangle$  ABC in which: AB = 12 cm.

$$BC = 10 \text{ cm.}, AC = 8 \text{ cm.}$$

Find the perimeter of :  $\triangle$  ADE





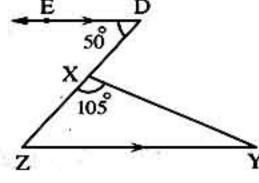
#### Final Examinations

#### 4 [a] In the opposite figure:

 $\overline{DE} // \overline{YZ}$ , m ( $\angle ZDE$ ) = 50°

$$m (\angle YXZ) = 105^{\circ}$$

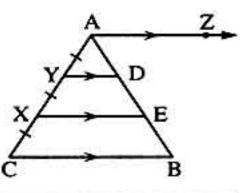
Find:  $m(\angle Z)$ ,  $m(\angle Y)$ ,  $m(\angle YXD)$ 



#### [b] In the opposite figure:

$$AY = YX = XC$$
,  $AB = 18$  cm.,

Find the length of: EB

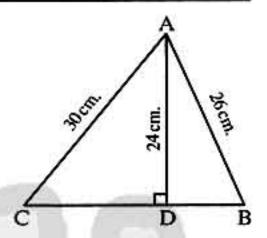


## 5 In the opposite figure:

$$\overline{AD} \perp \overline{BC}$$
, if  $AD = 24$  cm.,

$$AB = 26 \text{ cm.}$$
,  $AC = 30 \text{ cm.}$ 

- (1) Find the length of: BC
- (2) Find the area of :  $\triangle$  ABC

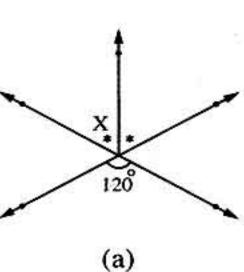


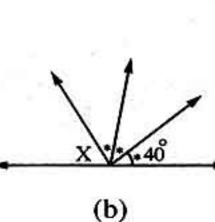
# Model

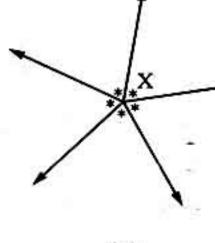
#### Answer the following questions:

## 1 Choose the correct answer from those given:

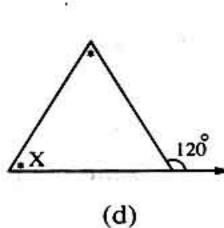
- (1) The image of the point (2, -5) by reflection in X-axis is ......
  - (a) (2, -5)
- (b) (2,5)
- (c) (-2, -5)
- (d)(5,2)
- (2) The measure of each angle of regular hexagon equals .......
  - (a) 60°
- (b) 108°
- (c) 120°
- (d) 135°
- (3) The two diagonals are equal in the length and not perpendicular in ........
  - (a) parallelogram. (b) rectangle.
- (c) rhombus.
- (d) square.
- (4) All the following shapes m ( $\angle X$ ) = 60° except the shape .......







(c)



#### (5) In the opposite figure:

The area of shaded part from the area of all shape equal .....

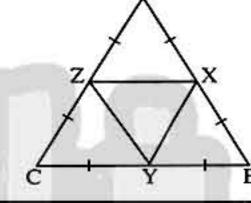
- (a)  $\frac{1}{8}$
- (b)  $\frac{1}{4}$
- (c)  $\frac{3}{8}$
- (d)  $\frac{3}{4}$

# 2 Complete the following:

- (1) The sum of the measures of the angles of the quadrilateral equals ......
- (a) The image of the point (2,3) by translation MN, in direction MN, where M (2,-1), N (5 , 1) is ......
- (3) ABCD is parallelogram in which m ( $\angle A$ ) = 60°, then m ( $\angle B$ ) = ......
- (4) The ray drawn parallel to one side of a triangle and passing through the midpoint of another side .....

# (5) In the opposite figure:

The image of the triangle XBY by translation XZ in direction XZ is .....



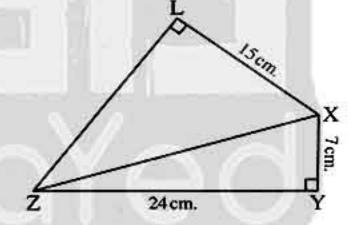
#### [3] [a] In the opposite figure:

XYZL is quadrilateral in which

$$m (\angle Y) = m (\angle L) = 90^{\circ}$$
,  $XY = 7$  cm.,

$$YZ = 24 \text{ cm.}$$
,  $XL = 15 \text{ cm.}$ 

Find the length of each of: XZ, LZ



[b] Using the square lattice, draw AB where

A 
$$(4,3)$$
, B  $(-1,1)$  then find the image  
of  $\overline{AB}$  by translation  $(x,y) \longrightarrow (x+2,y-1)$ 

[a] Draw the image of triangle ABC where A(1,1), B(3,4), C(5,2) by reflection in X-axis.

# [b] In the opposite figure:

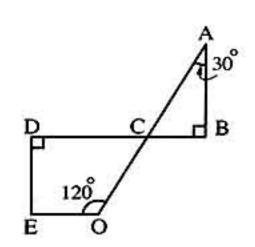
AB and ED, are perpendicular to

$$\overline{BD}^{\bullet}, \overline{BD} \cap \overline{AO} = \{C\}$$

$$m (\angle A) = 30^{\circ}$$

, m (
$$\angle$$
 EOC) = 120°,

Find:  $m (\angle E)$ 

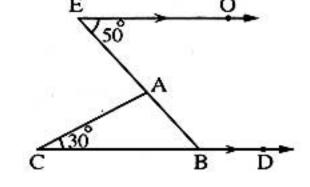


# [5] [a] In the opposite figure:

$$\overrightarrow{EO} // \overrightarrow{CD}$$
, m ( $\angle E$ ) = 50°

$$, m (\angle C) = 30^{\circ}$$

Find the measures of angles of  $\triangle$  ABC  $\rightarrow$  m ( $\angle$  ABD)

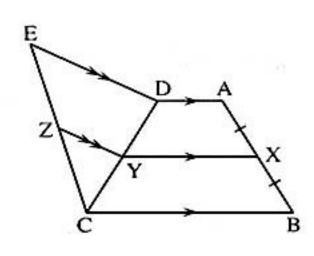


#### [b] In the opposite figure:

X is the midpoint of AB

$$,Y \in \overline{CD}, Z \in \overline{CE}$$

$$,\overline{AD} // \overline{XY} // \overline{BC}, \overline{YZ} // \overline{DE}$$



#### Model

# Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The image of the point (3, -5) by reflection in y-axis is ......
  - (a)(3,5)
- (b) (-3, -5)
- (c)(-3,5)
- (d)(-5,3)
- (2) The sum of the measures of interior angles of a pentagon is .......
  - (a) 360°
- (b) 450°
- (c) 540°
- (d) 720°
- (3) The number of diagonals of quadrilateral is ........
  - (a) 2
- (b) 3
- (c) 4
- (d) 5

# (4) In the opposite figure:

 $\triangle AB \hat{C}$  is the image of  $\Delta$  ABC by rotation about A and with angle of measure .....

- (a) 30°
- (b) 80°
- (c) 110°
- (d) 140°
- (5) The diagonal of a square divided its vertex angle in two angles of the measure of each of them is .....
  - (a) 30°
- (b) 45°
- (c) 60°
- (d) 90°

# 2 Complete the following:

- (1) The rhombus is a parallelogram in which ......
- (2) Each opposite angles in a parallelogram are ........
- (3) (-3, 2) is the image of the point (3, 2) by reflection in .... axis.
- (4) The line segment joining the midpoint of two sides of a triangle is .......
- (5) The image of the point (4,6) by geometric transformation  $(X,y) \longrightarrow (-X,y-7)$ is .....

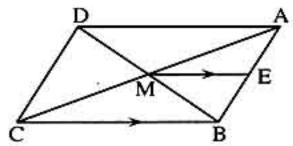
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[3] [a] Using the lattice, draw Δ ABC where A (1,0), B (0,2) and C (-3,1), then draw its image by reflection in X-axis.

#### [b] In the opposite figure:

ABCD is a parallelogram  $\bullet$  M is the intersection of its diagonals Draw  $\overrightarrow{ME}$  //  $\overrightarrow{CB}$ 

is AE = EB ? giving reason.



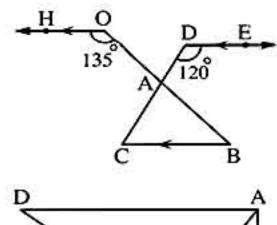
#### 4 [a] In the opposite figure:

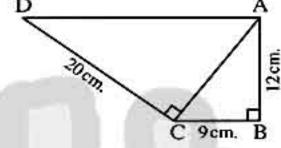
 $\overrightarrow{DE}$  //  $\overrightarrow{OH}$  //  $\overrightarrow{BC}$ , m ( $\angle$  ADE) = 120° , m ( $\angle$  AOH) = 135°, Calculate the measures of the angles of the triangle ABC



m (
$$\angle$$
 B) = m ( $\angle$  ACD) = 90°,  
AB = 12 cm., BC = 9 cm., CD = 20 cm.

Find the length of each of: AC, AD

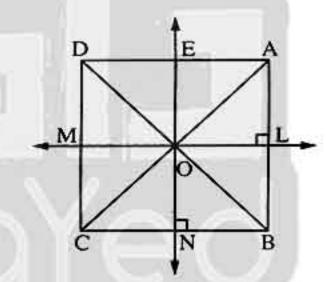




# 5 In the opposite figure:

ABCD is a square of side length 6 cm. and the origin point its center. Find:

- (1) The image of  $\triangle$  AOL by translation 3 cm. in direction  $\overrightarrow{AB}$
- (2) The image of  $\Delta$  AOL by reflection in  $\overline{EN}$
- (3) The image of  $\Delta$  AOL by rotation about O and with an angle of measure (-90°)



# Model 4

Answer the following questions:

#### 1 Choose the correct answer from those given :

- (1) The parallelogram whose diagonals are perpendicular and not equal in length is called ..........
  - (a) rhombus.
- (b) square.
- (c) rectangle.
- (d) trapezium.
- (2) The measure of each angle of a fegular pentagon is .....
  - (a) 90°
- (b) 108°
- (c) 120°
- (d) 136°
- (3) The triangle contains at least two ...... angles.
  - (a) acute
- (b) obtuse
- (c) right
- (d) reflex

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هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلوم

- (4) If ABCD is a parallelogram in which BC = 8 cm., CD = 6 cm., then its perimeter = .......
  - (a) 14 cm.
- (b) 28 cm.
- (c) 48 cm.
- (d) 56 cm.
- (5) The image of the point (2, -1) by reflection in X-axis is .......
  - (a)(2,1)
- (b) (1, 2)
- (c) (-2,-1)
- (d)(-1,2)

#### 2 Complete the following:

- (1) The line segment joining the midpoint of two sides of a triangle is ........
- (2) In a parallelogram each opposite angles are ........
- (3) The quadrilateral is a parallelogram if ......
- (4) The image of the point (5, -3) by translation 3 units in negative direction of X-axis is .........
- (5) The image of the point (3, 2) by rotation with an angle of measure 180° about the origin is .........

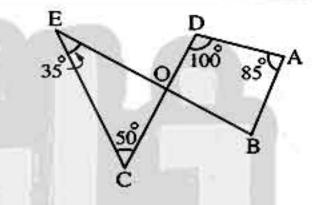
# 3 In the opposite figure:

$$\overline{DC} \cap \overline{BE} = \{O\}, m (\angle A) = 85^{\circ}$$

$$m (\angle D) = 100^{\circ} , m (\angle E) = 35^{\circ} , m (\angle C) = 50^{\circ}$$



- (1) m (∠ DOB)
- (2) m (\( \alpha \) B)

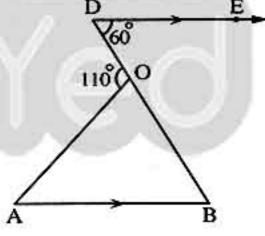


- [4] [a] Find the length of the diagonal of a rectangle whose area 48 cm<sup>2</sup> and of width 6 cm.?
  - [b] In the opposite figure:

$$m (\angle D) = 60^{\circ}$$

$$, m (\angle AOD) = 110^{\circ}$$

Find with proof:  $m (\angle A)$ 

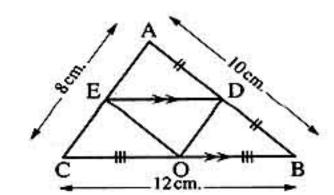


- [5] [a] If the point A is the image of point B (-1,2) by reflection in y-axis, find the image of A by translation (-1,2)
  - [b] In the opposite figure:

ABC is a triangle in which D is the midpoint of  $\overline{AB}$ , O is the midpoint of  $\overline{BC}$ ,  $E \subseteq \overline{AC}$  Such that  $\overline{DE}$  //  $\overline{BC}$ ,

AB = 10 cm., BC = 12 cm., AC = 8 cm.

- (1) Prove that: DBOE is a parallelogram.
- (2) Find the perimeter of :  $\Delta$  EDO



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هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلوم

# Model

Answer the following questions:

# 1 Choose the correct answer from those given:

- (1) The image of the point (-3,4) by reflection in y-axis is .........
  - (a) (3, -4)
- (b) (3,4)
- (c) (-3, -4)
- (d) (4, -3)
- (2) The sum of the measure of the exterior angles of a triangle equals .........
  - (a) 90°
- (b) 108°
- (c) 180°
- (d) 360°
- (3) The diagonals which are equal in the length and perpendicular in .........
  - (a) square.
- (b) rhombus.
- (c) rectangle.
- (d) parallelogram.
- (4) The image of the point (-3, 5) by rotation about the origin and with an angle of measure 90° is .....
  - (a) (5,3)
- (b) (-5,3) (c) (3,5)
- (d)(-5,-3)
- (5) The measure of each angle of regular octagon equals .....
  - (a) 108°
- (b) 120°
- (c) 135°
- (d) 144°

# Complete the following:

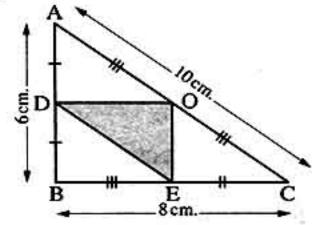
- (1) The parallelogram whose diagonals are perpendicular is .......
- (2) If the measure of an interior angle of a triangle is equal to the sum of the measures of the other two interior angles , then the triangle is .......
- (3) Any triagnle has at least two ..... interior angles.
- (4) The triagnle of the point (2, -4) by reflection in X-axis is .......
- (5) The image of the point (3, -2) by translation  $(x, y) \longrightarrow (x-1, y+6)$  is ......
- 3 [a] Prove that the ray drown parallel to one side of a triangle and passing through the midpoint of another side bisects the third side of the triangle

# [b] In the opposite figure:

D, E, O are midpoints of AB, BC, AC resectively, AB = 6 cm.,

BC = 8 cm., AC = 10 cm.

Find the perimeter of :  $\Delta$  DEO

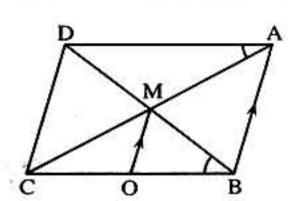


# [a] In the opposite figure:

ABCD is a parallelogram its diagonals are intersect at M, MO // AB

, MO  $\cap$  BC =  $\{0\}$ 

Prove that : BO = OC



كراسة المعاصر رياضيات (لغات) /١ إعدادي / تيرم ٢ (٢ : ١٢)



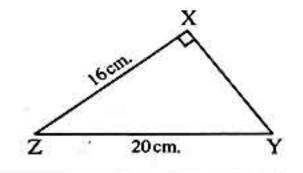


#### [b] In the opposite figure:

XYZ is a triangle in which m  $(\angle X) = 90^{\circ}$ ,

YZ = 20 cm., XZ = 16 cm.

Find the length of: XY

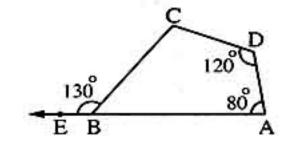


#### 5 [a] In the opposite figure :

$$m (\angle A) = 80^{\circ} , m (\angle D) = 120^{\circ}$$

$$m (\angle CBE) = 130^{\circ}$$

Find:  $m (\angle C)$ 



- [b] On a square lattice, draw the triangle whose vertices are A(4,4)B(4,2), C(1,2) then determine each of the following:
  - (1) The coordinates of the image of  $\triangle$  ABC by translation 2AB in direction AB
  - (2) The image of  $\triangle$  ABC by rotation about B and with an angle of measure 180°

# Model

#### Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The measure of each angle of the regular pentagon is ........
  - (a) 90°
- (b) 108°
- (c) 120°
- (d) 144°
- (2) The smallest number of the acute angle in any triangle is .......
  - (a) zero
- (b) 1
- (c) 2
- (d).3
- (3) The rhombus of diagonals are equal in length is ......
  - (a) square.
- (b) rectangle.
- (c) parallelogram. (d) trapezium.
- (4) The image of the point (2, -1) by reflection in X-axis is .......
  - (a)(2,1)
- (b) (1, 2)
- (c) (-2,-1) (d) (-1,2)
- (5) The image of the square by rotation about the origin point with an angle of measure 90° is .....
  - (a) rectangle.
- (b) square.
- (c) rhombus.
- (d) trapezium.

# 2 Complete the following:

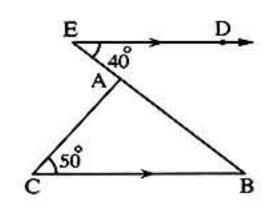
- (1) The measure of the exterior angle of a triangle is .........
- (2) The parallelogram whose diagonals are equal in length and perpendicular is ........
- (3) ABCD is a parallelogram in which m ( $\angle A$ ) = 50°, then m ( $\angle B$ ) = ......
- (4) The image of the point (-4,5) by translation (2,-3) is ......

3 [a] In the opposite figure:

$$\overrightarrow{ED} // \overrightarrow{CB}$$
, m ( $\angle C$ ) = 50°

$$m (\angle E) = 40^{\circ}$$

Prove that : AC \( \precedet \) BE



[b] Draw  $\triangle$  OBC on a square lattice where O (0,0), B (3,0), C (0,4)then find its image by rotation about the origin point with an angle of measure 180°

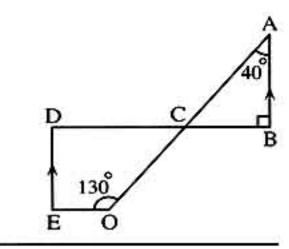
4 In the opposite figure :

$$\overline{BD} \cap \overline{AO} = \{C\}, \overline{AB} // \overline{DE},$$

$$m (\angle A) = 40^{\circ}, m (\angle B) = 90^{\circ},$$

$$m (\angle COE) = 130^{\circ}$$

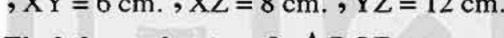
Find:  $m (\angle E)$ 

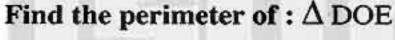


[5] [a] In the opposite figure:

XYZ is a triangle in which D, E, O are midpoints of XY, XZ, YZ respectively

$$XY = 6 \text{ cm.}$$
  $XZ = 8 \text{ cm.}$   $YZ = 12 \text{ cm.}$ 



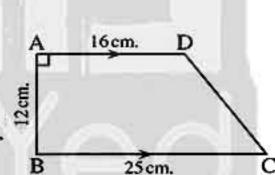


[b] In the opposite figure:

ABCD is a trapezium in which AD // BC

$$m (\angle A) = 90^{\circ} AB = 12 \text{ cm.} BC = 25 \text{ cm.} AD = 16 \text{ cm.}$$

Find the length of: DC



Model

Answer the following questions:

Choose the correct answer from those given:

- (1) The measure of each angle of the regular hexagon is .......
  - (a) 108°
- (b) 120°
- (c) 136°
- (d) 144°
- (2) Any triangle has at least two ..... interior angles.
  - (a) acute
- (b) right
- (c) obtuse
- (d) straight

(3) The diagonals of the rectangle are ......

(a) parallel.

(b) perpendicular.

(c) equal in the length.

(d) equal in length & perpendicular.

- (4) The image of a triangle by rotation about the origin point with an angle of measure 180° is .....
  - (a) triangle.
- (b) line segment. (c) point.
- (d) straight line.
- (5) The image of the point (3, -2) by reflection in y-axis ......
  - (a)(3,2)
- (b) (-3, -2) (c) (-3, 2) (d) (-2, 3)

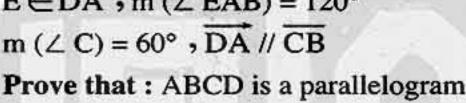
# 2 Complete the following:

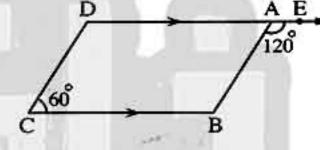
- (1) The sum of the measures of the interior angles of a pentagon equals .........
- (2) The measure of the exterior angle of an equilateral triangle = .......... at one of its vertices.
- (3) The rectangle is a parallelogram in which one of its angles is .........
- (4) The image of the point (-4, 5) by translation (2, -3) is ......
- (5) If the image of the point (-4,0) by rotation about the origin point is (0,-4), then the measure of rotation angle is .....

# 3 [a] In the opposite figure:

$$E \in \overline{DA}$$
,  $m (\angle EAB) = 120^{\circ}$   
 $m (\angle C) = 60^{\circ}$ ,  $\overline{DA} // \overline{CB}$ 

Prove that: ABCD is a parallelogram.





#### [b] In the opposite figure:

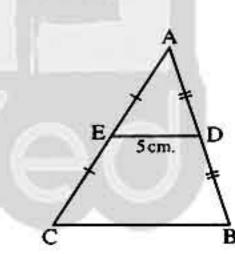
ABC is a triangle in which D

, E are the midpoints

of AB, AC respectively

DE = 5 cm.

Find the length of: BC



#### 4 [a] In the opposite figure:

ABCDE is a pentagon in which m ( $\angle A$ ) = 70°

$$m (\angle B) = 120^{\circ} , m (\angle C) = 150^{\circ}$$

$$, m (\angle E) = 110^{\circ}$$

**Find**:  $m (\angle D)$  with proof.

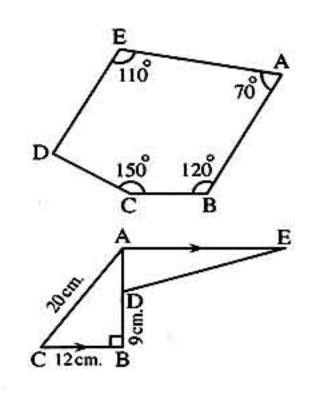
# [b] In the opposite figure:

 $\triangle$  ABC in which m ( $\angle$  B) = 90°, AE // BC,

if BC = 12 cm. 
$$AC = 20$$
 cm.  $D \in \overline{AB}$ 

such that: BD = 9 cm., AE = 2 BC,

Find the length of each :  $\overline{AD}$ ,  $\overline{ED}$ 



هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

8cm.

# [a] In the opposite figure:

ABCD is a parallelogram in which

$$AB = 5 \text{ cm.}, BC = 8 \text{ cm.}, m (\angle B) = 135^{\circ}$$

#### Find:

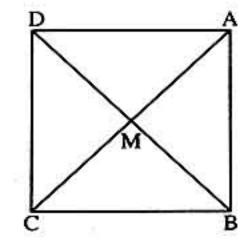
- (1) m (\(\perp C\))
- (2) The perimeter of parallelogram ABCD

#### [b] In the opposite figure:

ABCD is a square, whose diagonals intersect at M.

#### Find:

- (1) The image of  $\triangle$  ABC by reflection in  $\overrightarrow{AC}$
- (2) The image of Δ MAB by rotation about M with measure (– 90°)



#### Model

#### Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The diagonal of square makes angle of measure ...... with any of its sides.
  - (a) 45°
- (b) 60°
- (c) 90°
- (d) 120°
- (2) The measure of any of the exterior angle of an equilateral triangle equals ......
  - (a) 60°
- (b) 90°
- (c) 120°
- (d) 180°
- (3) In  $\triangle$  ABC if m ( $\angle$  A) > m ( $\angle$  B) + m ( $\angle$  C) then the angle A is .......
  - (a) acute.
- (b) right.
- (c) obtuse.
- (d) straight.
- (4) The sum of the measures of any two consecutive angles in a parallelogram equals .......
  - (a) 90°
- (b) 180°
- (c) 270°
- (d) 360°
- (5) The image of the point (5, -3) by rotation about the origin point is itself, then the measure of rotation angle is .........
  - (a) 90°
- (b) 180°
- (c) 270°
- (d) 360°

# 2 Complete the following:

- (1) The length of a line segment joining the midpoints of two sides of a triangle equals .........
- (2) The parallelogram whose diagonals are perpendicular and of equal in length is .........
- (3) The parallelogram whose perimeter 24 cm. and the length of one of its sides is 7 cm., then the length of its adjacent side equals ..........
- (4) The image of the point (3, 4) by reflection in the X-axis is .......... and its image by reflection in the y-axis is ...........
- (5) If the image of the point (-1,3) by a translation is (1,4) then the image of the point (3,-2) by the same translation is .........

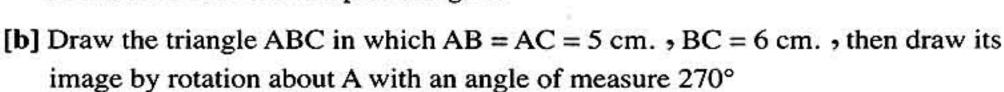
93

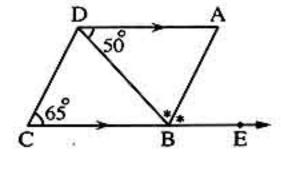
# [3] [a] In the opposite figure:

DA // BE , BA bisects ∠ DBE

$$m (\angle ADB) = 50^{\circ} m (\angle C) = 65^{\circ}$$

Prove that: ABCD is a parallelogram



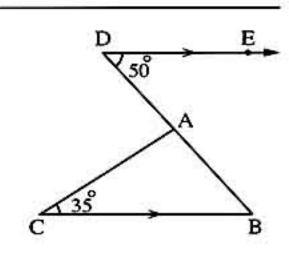


# [4] [a] In the opposite figure:

$$\overrightarrow{DE} // \overrightarrow{CB}$$
, m ( $\angle D$ ) = 50°

$$m (\angle C) = 35^{\circ}$$

Find: (1) m  $(\angle B)$ 



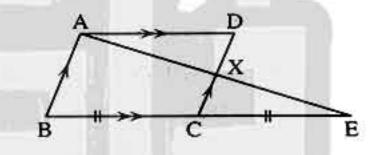
[b] Draw the triangle ABC in which AB = 3 cm., BC = 4 cm., m ( $\angle$  ABC) = 90°, then draw its image by reflection in straight line  $\overrightarrow{BC}$ 

# 5 [a] In the opposite figure:

ABCD is a parallelogram , E ∈ BC

Such that : 
$$CE = BC \cdot AE \cap DC = \{X\}$$

Prove that : AX = XE



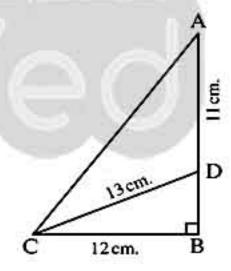
# [b] In the opposite figure:

ABC is a triangle in which m ( $\angle B$ ) = 90°, D  $\in \overline{AB}$ 

Such that : 
$$AD = 11$$
 cm.

, if 
$$BC = 12 \text{ cm.}$$
,  $DC = 13 \text{ cm.}$ ,

Find the length of each of :  $\overline{BD}$ ,  $\overline{AC}$ 



#### **School Examinations**

# Cairo Governorate

#### **El-Sahel Educational Zone**

Gawad Ali Hosni Exp. Language School

Answer the following questions:

# 1 Choose the correct answer:

- (1) The sum of measures of the interior angles of the hexagon = .........
  - (a) 540°
- (b) 720°
- (c) 900°
- (d) 1080°
- (2) The identity rotation about any point is with an angle of measure .........
  - (a) 90°
- (b) 180°
- (c) 270°
- (3) In the parallelogram ABCD if m ( $\angle A$ ) + m ( $\angle C$ ) = 100°, then m ( $\angle B$ ) = ......
  - (a) 50°
- (b) 80°
- (c) 130°
- (4) The image of the point (2, -3) by translation (1, -1) is ......
  - (a) (3, -4)
- (b) (1, -2)
- (c)(2,3)
- (d)(3,2)
- (5) In the triangle ABC, if m ( $\angle$  A) = m ( $\angle$  C) = 65°, then m ( $\angle$  B) = ......
  - (a) 50°
- (b) 65°
- (c) 120°
- (d) 130°

# 2 Complete each of the following:

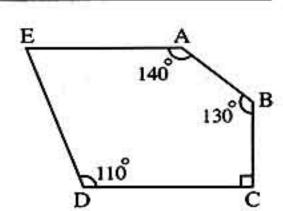
- (1) The length of the line segment joining the midpoints of two sides of a triangle is equal to .....
- (2) Each two opposite angles of a parallelogram ........
- (3) A parallelogram whose two diagonals are equal in length is called .........
- (4) The sum of measures of the interior angles of a triangle equals ..........°
- (5) The image of a point (0,5) by reflection in y-axis is ........

#### [3] [a] In the opposite figure:

$$m (\angle A) = 140^{\circ} , m (\angle B) = 130^{\circ}$$

$$m (\angle C) = 90^{\circ} \cdot m (\angle D) = 110^{\circ}$$

Find:  $m (\angle E)$ 



#### [b] Draw on square lattice $\triangle$ ABC

Where: A (1,3), B (3,5), C (5,0)

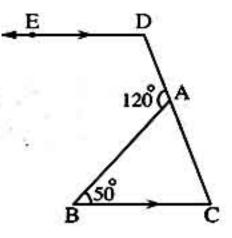
Find the image of  $\triangle$  ABC by reflection in y-axis

# [4] [a] In the opposite figure:

$$m (\angle DAB) = 120^{\circ}$$

$$(\angle B) = 50^{\circ}$$

Find by proof:  $m (\angle D)$ 

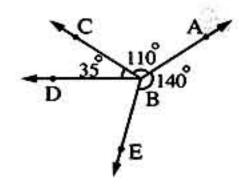


#### [b] In the opposite figure:

$$m (\angle ABC) = 110^{\circ}, m (\angle CBD) = 35^{\circ},$$

$$m (\angle ABE) = 140^{\circ}$$

**Find**:  $m (\angle EBD)$ 



# [5] [a] Draw $\triangle$ ABC in which AB = 5 cm., BC = 3 cm. and AC = 3 cm., then find its image by reflection in $\overrightarrow{AB}$

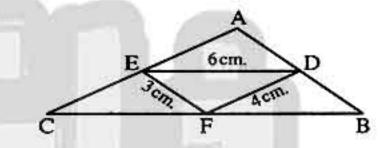
#### [b] In the opposite figure:

Δ ABC in which: D , F and E are midpoints

respectively, such that: DF = 4 cm.,

$$FE = 3 \text{ cm.}$$
,  $DE = 6 \text{ cm.}$ 

Calculate the perimeter of :  $\Delta$  ABC



# Additional question

#### 1 Complete the following:

- (1) The image of the point (-3,5) by reflection in the origin point is ........
- (2) The translation in a plane keeps ......
- (3) The number of axes of symmetry of the rhombus is .......

# 2 In the opposite figure:

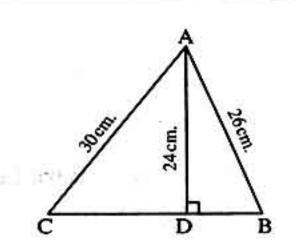
ABC is a triangle in which

$$\overline{AD} \perp \overline{BC}$$
, if  $AD = 24$  cm.

$$AB = 26 \text{ cm.}$$
  $AC = 30 \text{ cm.}$ 

(1) Find: BC

(2) Calculate the area of :  $\triangle$  ABC



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# Cairo Governorate

# **Amal Language Schools**

south teral standard stade DB (TAE = \$C)

#### **Maadi Educational Directorate**

Answer the following questions:

#### Choose the correct answer from those given:

- (1) XYZL is a parallelogram if m ( $\angle X$ ) = 70°, then m ( $\angle Y$ ) = 10.000, qo odt ml [d]
  - (a) 70°
- (b) 90°
- on (c) 20° A daily m (d) 110° at 11 it

Final with proof 1 cent

- - (a) (2, 1)
- (b) (2,-1) (c) (-2,-1) (d) (1,2)
- - (a) 120°
- (b) 135°
- (c) 108° (d) 72°
- (4) The sum of the measures of the interior angles of a triangle is .........
  - (a) 90°
- (b) 150°
- (c) 100°
- (d) 180°
- (5) The measure of the exterior angle of the equilateral triangle = ..........
  - (a) 60°
- (b) 90°
- (c) 120°

I sale to discuss all ter thought all also all the contract which is

(d) 150°

#### 2 Complete:

- (1) The image of the point (3, -5) by rotation about the origin point with an angle of measure 90° is .....
- (2) In the rhombus, the two diagonals are ......... and ........
- (3) The ray drawn from the midpoint of a side of a triangle parallel to another side ........
- (4) A quadrilateral in which only two opposite sides are parallel is called a ......
- (5) The image of the point (1,4) by translation (x,y)

zixu-Z ni mususil za 7d (\* -

#### [a] In the opposite figure : la Rose Dr Lisicux Language

LM // XN // YZ

 $m (\angle L) = 100^{\circ}$ 

 $m (\angle NXZ) = 40^{\circ}$ 

100 (Xscing questions: correct answer from the given ones :

7 110 16

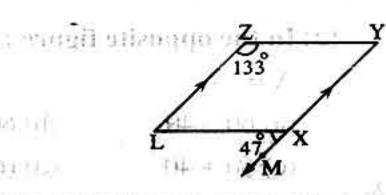
# Find the measures of angles of : $\Delta XYZ$

# [b] In the opposite figure:

LZ//YX, m ( $\angle Z$ ) = 133°

 $m (\angle LXM) = 47^{\circ}$ 

Prove that: XYZL is a parallelogram.



FIFTH SECTION OF

PART (BARRIE)

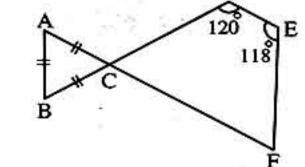
# 4 [a] In the opposite figure:

DEFC is a quadrilateral

 $\Delta$  ABC is an

equilateral triangle where  $\overline{DB} \cap \overline{AF} = \{C\}$ 

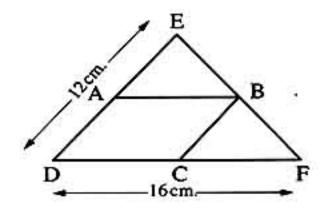
Find with proof:  $m (\angle F)$ 



#### [b] In the opposite figure:

EDF is a triangle in which A, B, C are the midpoints of ED, EF and DF respectively

Find the primeter of the quadrilateral: ABCD



Using the square lattice draw  $\Delta$  LMN in which L = (4,4), M = (4,1), N = (1,1)then find its image by rotation about the origin point with an angle of measure 180°

# Additional question

#### 1 Complete the following:

- (1) In the right-angled triangle, the square of the length of the hypotenuse equals ........
- (2) The number of axes of symmetry of the square is .......
- (3) The point (5, -3) is the image of the point ....... by reflection in the origin point.
- 2 Draw a triangle ABC where AB = BC = 5 cm. and AC = 6 cm. then find its image by reflection in the point B

# Giza Governorate

# **Dokki Educational Directorate**

# La Rose De Lisieux Language

Answer the following questions:

# 1 Choose the correct answer from the given ones:

- (1) The image of the point (-3, 5) by reflection in X-axis is .......
  - (a) (5, -3)
- (b) (3, -5)
- (c)(3,5)
- (d) (-3, -5)

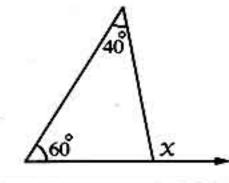
# (2) In the opposite figure:

 $\chi = \cdots \cdots$ 

- (b)  $60 \times 40$
- (c) 60 + 40

(a) 60 - 40

(d)  $(60 \div 40)$ 



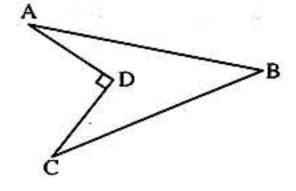
هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلق

- (3) ABCD is called a concave polygon because one of its interior angles is .....
  - (a) acute.

(b) Right.

(c) obtuse.

(d) reflex.



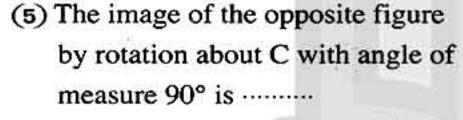
#### (4) In the opposite figure:

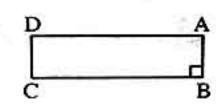
If D, E are the midpoints if AB, AC respectively and the perimeter if  $\Delta AED = 24$  cm. then the perimeter if  $\triangle$  ABC = ......

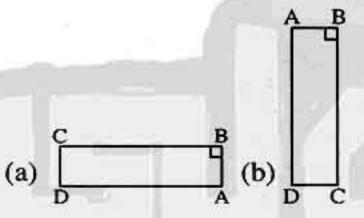


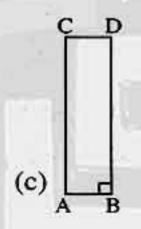
- (b) 18
- (c) 48

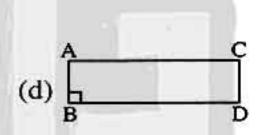
- (d) 24





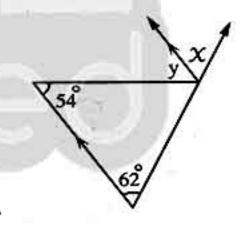






# 2 Complete the following:

- (1) In the opposite figure:  $x + y = \cdots$
- (2) The image of the point (5, -3) by rotation about the origin point with an angle of measure 90° is ......



- (3) The measure of the interior angle of the regular hexagon = .........
- (4) Each two opposite sides of a parallelogram are ........ , and .......
- (5) A square is rectangle in which the two diagonals are ........

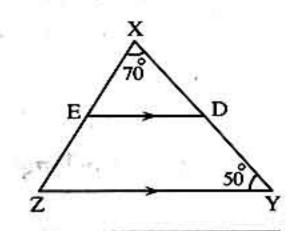
# 3 [a] Using the square lattice draw $\Delta$ ABC in which :

A (5, -2), B (2, 2) and C (1, -3) then find its image by translation (-3, 2)

#### [b] In the opposite figure:

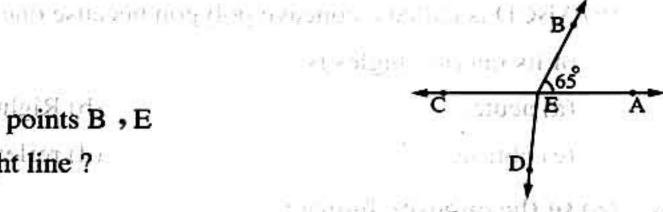
 $\Delta$  XYZ in which m (X) = 70°,  $m(Y) = 50^{\circ} \cdot ED // ZY$ 

Find:  $m (\angle XED)$ 



# [4] [a] $\overrightarrow{AC} \cap \overrightarrow{ED} \cap \overrightarrow{ED} = \{E\}$

- (1) **Find**: m (∠ BEC)
- (2) If m (CED) = 85° are the points B, E and D on the same straight line?



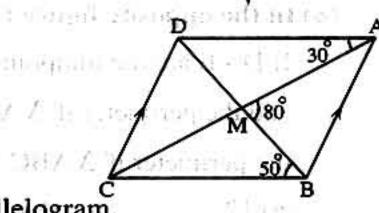
#### [b] In the opposite figure:

$$\overline{AB}//\overline{DC}$$
,  $\overline{AC} \cap \overline{BD} = \{M\}$ ,

 $m (\angle DAC) = 30^{\circ}$ ,  $m (\angle DBC) = 50^{\circ}$ ,

and  $m (\angle AMB) = 80^{\circ}$ 

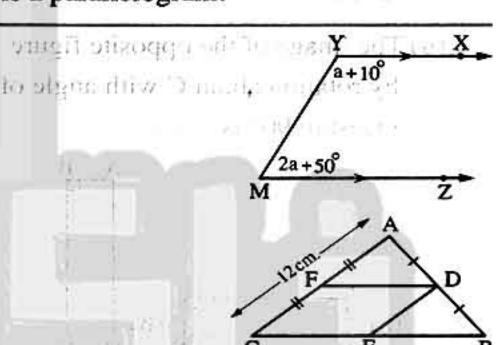
Find: m (\( \subseteq MCB \)) then prove that ABCD is a parallelogram.



# [a] In the opposite figure:

If XY // MZ

Find the value of a

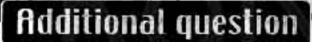


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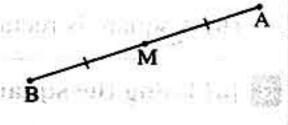
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# [b] In the opposite figure:

ABC is a triangle in which D, E and F are the midpoints of AB, BC, and CA respectively, BC = 16 cm., AC = 12 cm.Find the perimeter of the quadrilateral DECF with proof.



- 1 Complete the following:
  - (1) The length of the diagonal of the rectangle whose dimensions are 8 cm. and 6 cm. equals ..... or the two opposite sides of a translation or a
  - (2) In the opposite figure: zimmognih over odrana was algumina z The image of AB by

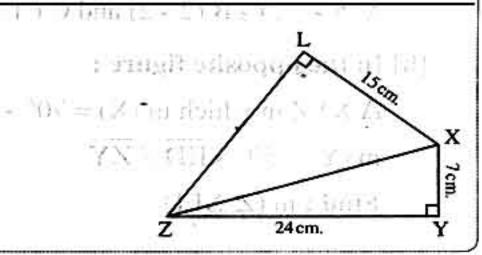


# 2 In the opposite figure:

 $m (\angle XYZ) = m (\angle XLZ) = 90^{\circ}$ XY = 7 cm. YZ = 24 cm.

, and XL = 15 cm.

Find the length of : XZ , LZ



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# Giza Governorate

#### **Boulak Educational Zone**

#### **Queen International School**

Answer the following questions:

- 1 Choose the correct answer from the given ones:
  - (1) The image of the point (2, -3) by reflection in X-axis is ...

(a) (1, 2)

(b) (2,3)

(c)(-3,2)

- (2) The image of the point (-2, 5) by rotation about the origin with an angle of measure 90° is .....

(a) (-2,5)

(b) (-2, -5) (c) (-5, -2) (d) (2, -5)

- (3) The image of the point (-1, -2) by translation of magnitude 3 units in the positive direction of X-axis is ......

(a) (2, -2)

- (4) The measure of the interior angle of the regular hexagon = ......

(a) 102°

(b) 180°

(c) 120°

- (d) 360°
- (5) The identity rotation about any point is with an angle of measure .........

(a) 90°

(b) 180° (c) 270° (d) 360°

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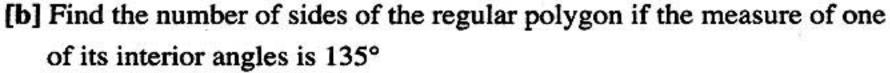
# Complete each of the following:

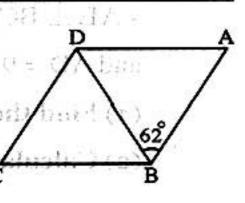
- (1) The point (5, -3) is the image of the point (3, 2) by translation ........
- (2) If the measure of an angle in a triangle equals the sum of measures of the two other angles, then the triangle is ......
- (3) The line segment which joins two midpoints of two sides in a triangle ........
- (4) The square is a ..... one of its angles is right.
- (5) The polygon which has a reflex angle is called ......

# 3 [a] In the opposite figure:

ABCD is a rhombus, BD is a diagonal,

Del : he dissel ed has  $m (\angle ABD) = 62^{\circ}$ U the area of the traperium:  $\Delta W \subseteq U$ Find by proof: m (∠ BAD)





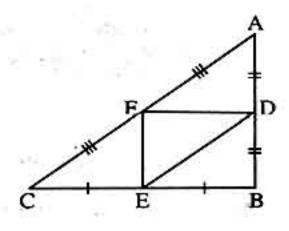
# 4 [a] In the opposite figure:

ABC is a triangle in which: AB = 6 cm.

BC = 8 cm., AC = 10 cm. and D, E, E

are the midpoints of the sides

Calculate the perimeter of the  $\Delta$  DEF

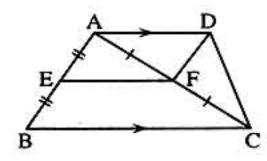


#### [b] In the opposite figure:

AD // BC  $\Rightarrow$  BC = 2 AD  $\Rightarrow$  E is the midpoint of AB

, F is the midpoint of AC

Prove that: AEFD is a parallelogram.



# 5 On a square lattice draw Δ ABC where A (4, 1), B (1, 1) and C (4, 4), then find:

- (1) The image of  $\triangle$  ABC by rotation about O with an angle of measure 90°
- (2) The image of  $\triangle$  ABC by reflection in the X-axis.

# Additional question

# 1 Choose the correct answer from those ones:

- (1) The point whose image by reflection in the origin point is itself is .......
  - (a) (0, 1)
- (b) (1,0)
- (c)(0,0)
- (d)(-1,0)
- (2) ABC is a right-angled triangle at B  $_{9}$  if AB = 3 cm. and AC = 5 cm.
  - , then BC = ..... cm.
  - (a) 16
- (b) 5
- (c) 3
- (d) 4

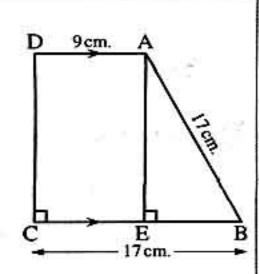
# 2 In the opposite figure:

AD // BC , m ( $\angle$  DCB) = 90°

 $\overline{AE} \perp \overline{BC}$  AB = BC = 17 cm.

and AD = 9 cm.

- (1) Find the length of: DC
- (2) Calculate the area of the trapezium : ABCD



# Alexandria Governorate

#### **East Educational Zone**

#### Al-Thghr E.L.S. for boys

Answer the following questions:

- 1 Choose the correct answer:
  - (1) The point (3, 4) is the image of the point (1, -2) by translation .......
    - (a) (-2, -6) (b) (2, 6)
- (c)(-2,6)
- (d) (2, -6)
- (2) The image of the (2, -1) by reflection in X-axis is .......
  - (a) (2, -1)
- (b) (-2,1) (c) (-2,-1) (d) (2,1)
- (3) The sum of measures of interior angles of a pentagon = .......
  - (a) 108°
- (b) 540°
- (c) 360°
- (d) 180°
- (4) In triangle ABC if m ( $\angle X$ ) + m ( $\angle Y$ ) < m ( $\angle Z$ ) then ( $\angle Z$ ) is ....... angle.
  - (a) acute
- (b) obtuse
- (c) right
- (d) straight
- (5) The measure of one exterior angle of a regular hexagon = .....
  - (a) 30°
- (b) 60°
- (c) 90°
- (d) 120°

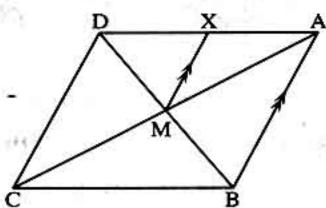
# 2 Complete each of the following to get correct statement:

- (1) The rectangle is a ..... with a right angle.
- (2) The image of point (-1,4) under rotation with an angle of measure 180° about the origin is .....
- (3) The line segment joining two midpoints of two sides of a triangle is ..... to the third side.
- (4) The sum of measures of the accumulative angles at a point is ..........°
- (5) If ABCD is a parallelogram,  $m (\angle A) + m (\angle C) = 130^{\circ}$ , then  $m (\angle B) = \cdots$
- [3] [a] Draw  $\triangle$  ABC where A (-1,2), B (1,3) and C (1,-2) then draw its image by reflection in y-axis.
  - [b] In the opposite figure:

ABCD is a parallelogram,

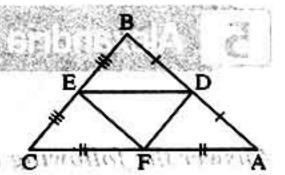
MX // AB

Prove that: X is the midpoint of AD



# [a] In the opposite figure:

AB = 8 cm., BC = 7 cm. and CA = 10 cm.If D, E and F are midpoints of AB, BC, and AC respectively. Find with proof perimeter of  $\Delta$  DEF

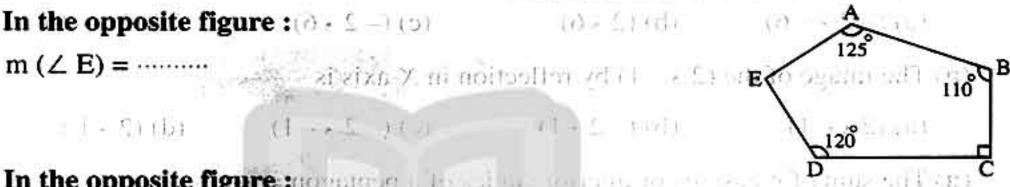


[b] Find the number of sides of a regular polygon if the measure of one of its interior angles is 135° mentioners yet (\$\infty - 1\) minor out the point (\$1 \infty - 2) through \$\infty\$ is \$1.00 \text{out the point (\$1 \infty - 2) through \$\infty\$ is \$1.00 \text{out through \$\infty\$ in \$1.00 \text

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# [a] In the opposite figure: (a) - (b)

$$m (\angle E) = \cdots$$

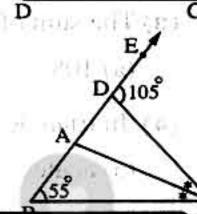


[b] In the opposite figure:

$$m (\angle EDC) = 105^{\circ}, m (\angle B) = 55^{\circ}$$

, AC bisects ∠ DCB

number of summer to some Zathe Find with proof:  $m (\angle CAD)$ 



# Additional question = nogerage uninger a to accompanie to the contract of the

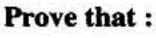
#### 1 Complete the following: 900 (a)

(1) If  $\Delta$  XYZ is a right-angled triangle at Z, then  $(XZ)^2 = \cdots$ 

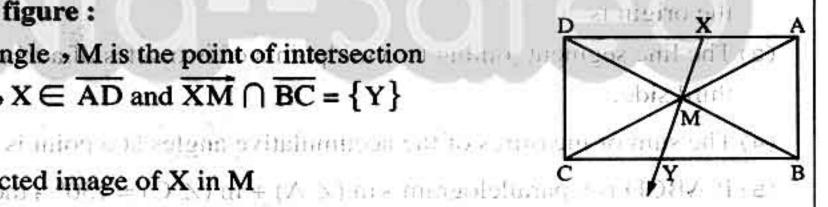
- (2) The image of the point (-4,2) by reflection in the origin point is .......
- (3) The number of axes of symmetry of the isosceles triangle is .......

# 2 In the opposite figure :

ABCD is a rectangle, M is the point of intersection of its diagonals  $X \in \overline{AD}$  and  $\overline{XM} \cap \overline{BC} = \{Y\}$ 



- (1) Y is the reflected image of X in M
- (2) The figure AXCY is a parallelogram.



# Alexandria Governorate

# El Nasr Boys School

#### **Preparatory Department**

Answer the following questions:

# 1 Choose the correct answer:

(1) In 
$$\triangle$$
 ABC if m ( $\angle$  A) = m ( $\angle$  B) = 50°, then m ( $\angle$  C) = .......

(a) 40°

(b) 60°

(c) 80°

(d) 100°

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

H7 - X17

- (2) The image of the point (-3,5) by reflection in y-axis is ........

- (a) (3,-5) (b) (3,5) (c) (-3,-5) (d) (-3,5)
- (3) In  $\triangle$  ABC, if m ( $\angle$  B) = m ( $\angle$  A) + m ( $\angle$  C), then  $\angle$  B is .......
  - (a) acute.
- (b) obtuse.
- (c) right.
- (d) reflex.
- (4) The measure of each interior angle of a regular pentagon = ...........

- (a) 72° (b) 80° (d) 108° (d) 108°
- (5) The image of point (+2,3) by reflection on the X-axis is ......
  - (a)(2,3)
- (b) (-2, -3) (c) (-3, -2)
- (d) (3 , 2)

to the numeral criedlet

#### 2 Complete:

- (1) The quadrilateral in which only two sides are parallel is called .........
- (2) The image of point (4,0) by translation (1,-3) is ......
- (3) In a parallelogram, every two opposite sides are ........ and .......
- (4) In the opposite figure:

 $AB \perp BC$ ,  $D \in BC$ 

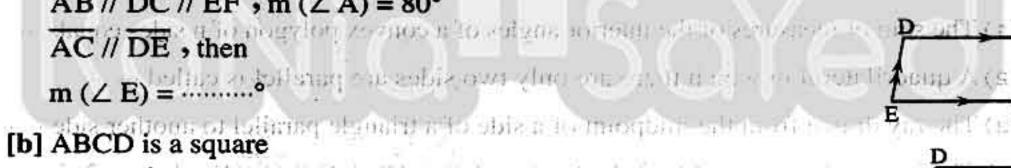
then m (ZA) = 3469 pdrad

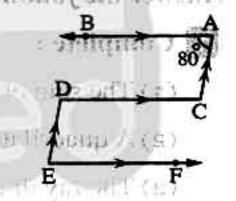
150

- (5) The rotation about the origin point with an angle of measure ..... called the identify rotation.

#### [a] In the opposite figure:

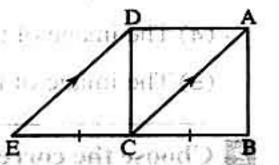
 $AB // DC // EF , m (\angle A) = 80^{\circ}$ 





É∈ BC, and AC // DE . X.) nontalization suit velos, - 1-1 annuques in servicing

- (1) Prove that : ACED is a parallelogram.
- (2) Find : m (∠ ACE)



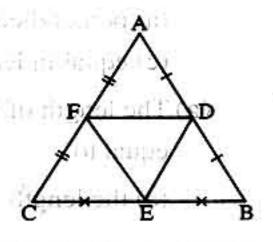
- [a] Calculate the sum of measures of the interior angles of hexagon.
- [b] In the opposite figure:

AB = 5 cm., BC = 8 cm., CA = 7 cm.

D, E and F are the midpoints of

AB, BC, CA respectively

Calculate the perimeter of  $\Delta$  DEF



كراسة المعاصر رياضيات (لغات) / ١ إعدادي / تيرم ٢ (٢ : ١٤)

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- Republishing 1 (81)

On the lattice draw  $\triangle$  ABC, where A (4,3), B (2,0), C (0,2), then draw its image  $\Delta \hat{A} \hat{B} \hat{C}$  by rotation about the origin with an angle of measure 180°

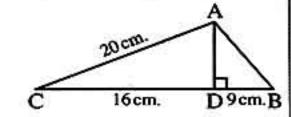
# Additional question

- 1 Complete the following:
  - (1) The image of the point (2, -7) by reflection in the origin point is .......
  - (2) If the axis of symmetry of  $\triangle$  ABC, where A (0, 3) and B (2, -1) is the y-axis , then C (......
- 2 In the opposite figure:

 $\overline{AD} \perp \overline{BC}$ , BD = 9 cm.,

DC = 16 cm., and AC = 20 cm.

Find the length of : AD , AB



# El-Kalyoubia Governorate

#### **Benha Educational Zone**

#### Math inspection

Answer the following questions:

- 1 Complete:
  - (1) The sum of measures of the interior angles of a convex polygon of n sides equals .......
  - (2) A quadrilateral in which there are only two sides are parallel is called ........
  - (3) The ray drawn from the midpoint of a side of a triangle parallel to another side .........
  - (4) The image of the point (4, 3) by the translation  $(x, y) \longrightarrow (x+1, y-2)$  is .......
  - (5) The image of the point (0, -3) by reflection in X-axis is .......
- Choose the correct answer:
  - (1) The two diagonals of the rhombus are ........
    - (a) perpendicular.

(b) parallel.

(c) equal in length.

- (d) perpendicular and equals in length.
- (2) The length of line segment which joins the two midpoints of two sides in a triangle equal to ..... of the third side.
  - (a) the length
- (b)  $\frac{1}{4}$  the length (c) twice the length (d)  $\frac{1}{2}$  the length

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- (3) In the triangle ABC if m ( $\angle$  A) = m ( $\angle$  B) = 50°, then m ( $\angle$  C) = ......
  - (a) 130°
- (b) 100°
- (c) 80°
- (d) 50°
- (4) A rhombus with perimeter 40 cm., then its side length .....
  - (a) 10 cm.
- (b) 5 cm.
- (c) 4 cm.
- (d) 8 cm.
- (5) The image of the point (2, -3) by rotation about the origin point with an angle of measure 90° is .....
  - (a) (-2,3)
- (b) (-2, -3) (c) (2, 3)
- (d)(3,2)
- 3 On an orthogonal Cartesian coordinates plane :

Draw  $\Delta$  LMN where: L(2,4), M(4,2) and N(3,1) then map its image:

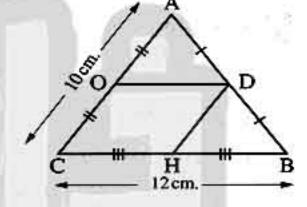
- (1) By reflection in y-axis
- (2) By rotation about the origin point with an angle of measure 180°
- [4] [a] In the opposite figure:

ABC is a triangle in which D, H and O

are the midpoints of AB, BC and CA respectively

 $_{9}$  BC = 12 cm. and AC = 10 cm.

Find the perimeter of the figure DHCO

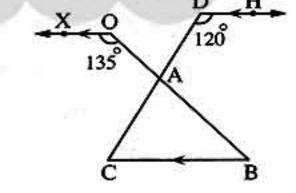


- [b] Find the number of sides of the convex regular polygon if the measure of one of its interior angles is 108°
- 5 [a] In the opposite figure:

$$m (\angle HDC) = 120^{\circ} and$$

$$m (\angle XOB) = 135^{\circ}$$

Find the measures of the angles of the triangle ABC



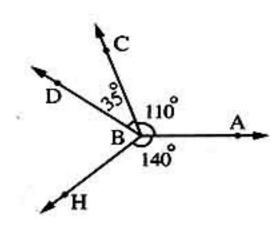
[b] In the opposite figure:

$$m (\angle ABC) = 110^{\circ}$$

$$m (\angle CBD) = 35^{\circ}$$

and m (
$$\angle$$
 ABH) = 140°

Find: m (∠ HBD)



Add	itiona	l aues	tion

- 1 Complete the following:
  - (1) The point (-1, 9) is the image of the point (1, -9) by reflection in ......
- (2) If the lengths of the two diagonals of a rhombus are 6 cm. and 8 cm., then its side length = ......

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2 Draw the square ABCD whose side length is 5 cm., then draw its image by reflection in the point M where M is the point of intersection of its diagonals. What do you observe?

# 8 El-Kalyoubia Governorate

Shebin El-Anater

Math Inspection

Answer the following questions:

- 1 Complete:
  - (1) The measure of the interior angle of the regular hexagon = ........
  - (2) The rhombus which has a right angle is called .......
  - (3) The image of the point (-2, 4) by reflection in X-axis is .......
  - (4) The image of the point (-1, 5) by translation (1, -3) is ......
  - (5) The sum of measures of the interior angles of a triangle = .........°
- 2 Choose the correct answer:
  - (1) If two adjacent sides are equal in a parallelogrm, then the figure is .......
    - (a) square.
- (b) rhombus.
- (c) rectangle.
- (d) trapezium.
- (2) The point (5,3) is the image of the point (-3,5) by rotation about the origin point with an angle of measure .........
  - (a) 90°
- (b)  $-90^{\circ}$
- (c) 180°
- (d) 360°

- (3) ABCD is square m (∠ ACB) = .......
  - (a) 90°
- (b)  $60^{\circ}$
- (c) 45°
- (d) 30°
- (4) The sum of measures of the interior angles of the pentagon = .....
  - (a) 360°
- (b) 450°
- (c) 540°
- (d) 720°
- (5) The ray drawn from the midpoint of a side of a triangle parallel to another side ...... the third side.
  - (a) equals
- (b) parallel
- (c) perpendicular to (d) bisects

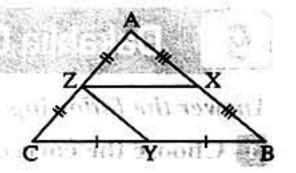
108

مذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى فيخاصونه



# 3 [a] In the opposite figure :

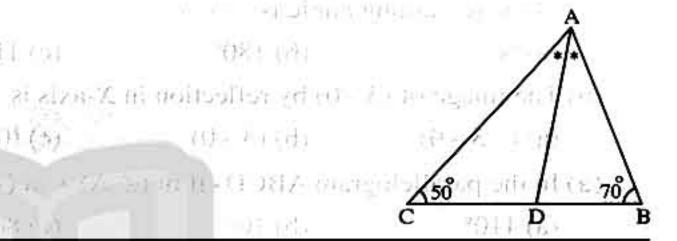
Δ ABC in which X, Y and Z are the midpoint of AB, BC and CA respectively, AB = 8 cm., BC = 10 cm.



Find the perimeter of the figure : XBYZ

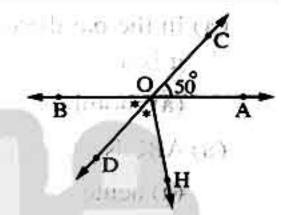
# [b] In the opposite figure:

AD bisects ∠ BAC,  $m (\angle B) = 70^{\circ}$ and m ( $\angle$  C) = 50° Find: m (∠ ADB)



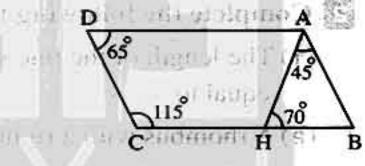
# [a] In the opposite figure :

$$\overrightarrow{AB} \cap \overrightarrow{CD} = \{0\}$$
,  
 $m (\angle AOC) = 50^{\circ}$ ,  
 $\overrightarrow{OD}$  bisects  $\angle HOB$   
Find:  $m (\angle AOH)$ 



#### [b] In the opposite figure:

m (
$$\angle$$
 BAH) = 45°, m ( $\angle$  AHB) = 70°,  
m ( $\angle$  C) = 115° and m ( $\angle$  D) = 65°  
Prove that : ABCD is a parallelogram.



075 J DIE N

Draw on an orthogonal lattice  $\triangle$  ABC where A (4, 2), B (2, 4) and C (1, -2) then find the image of  $\Delta$  ABC by reflection in y-axis. Second the second affice?

# Additional question

# 1 Complete the following:

- (1) In the right-angled triangle, the square of the length of the hypotenuse equals .........
- (2) If  $(2 \times 4)$  is the image of (x-9, -4) by reflection in the origin point, then  $x = \cdots$
- By using geometric instruments, draw the rectangle ABCD, where AB = 3 cm. and BC = 4 cm. locate A as the reflected image of A by reflection in CD and locate C as the reflected image of C by reflection in AB

Prove that : (1) m (
$$\angle \overrightarrow{CAC}$$
) = 2 m ( $\angle CAB$ )  
(2)  $\overrightarrow{AC}$  //  $\overrightarrow{AC}$ 



P. Salina a female

# Dakahlia Governorate

# Fakhr Language School

Answer the following questions:

#### 1 Choose the correct answer:

- (1) The sum of measures of 5 angles of a polygon of 6 sides is 610°, then the measure of the remaining angle is .....
  - (a) 60°
- (b) 180°
- (c) 110°
- (d) 120°
- (2) The image of (3,0) by reflection in X-axis is ........
  - (a) (-3,0)
- (b) (3,0)
- (c) (0, -3)
- (d)(0,3)
- (3) In the parallelogram ABCD, if m ( $\angle$  A) + m ( $\angle$  C) = 160°, then m ( $\angle$  B) = ......
  - (a) 110°
- (b) 100°
- (c) 80°
- (4) In the parallelogram, if the diagonals are orthogonal and equal in length, then it is a ......
  - (a) rhombus.
- (b) rectangle.
- (c) trapezium.
- (d) square.
- (5) ABC is a triangle, m ( $\angle A$ ) =  $2x^{\circ}$ , m ( $\angle C$ ) =  $x^{\circ}$  and m ( $\angle B$ ) =  $3x^{\circ}$ , then  $\angle B$  is .......
  - (a) acute.
- (b) right.
- (c) obtuse.
- (d) straight.

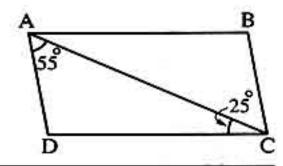
#### 2 Complete the following:

- (1) The length of the line segment joining the midpoints of two sides of a triangle is equal to .....
- (2) A rhombus with a right angle is called a ......
- (3) In the parallelogram, if two adjacent sides are equal in length, then it becomes a .........
- (4) The sum of measures of exterior angles of a triangle equals ...........°
- (5) The image of the point (-2,3) by reflection into the origin is .........
- 3 [a] Draw the image of  $\triangle$  ABC, where A (1,3), B (0,5) and C (-2,4) by reflection in the X-axis.
  - [b] In the opposite figure:

ABCD is a parallelogram,

 $m (\angle CAD) = 55^{\circ} \cdot m (\angle ACD) = 25^{\circ}$ 

Find with proof:  $m (\angle B)$ 

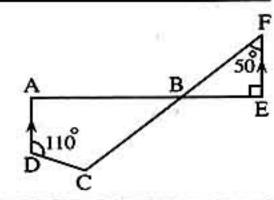


#### 4 [a] In the opposite figure:

AD // EF,  $m (\angle E) = 90^{\circ}$ ,

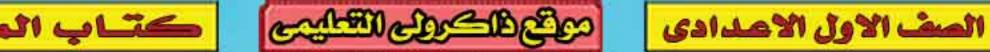
 $m (\angle F) = 50^{\circ} \cdot m (\angle D) = 110^{\circ}$ 

Find:  $m (\angle C)$ 



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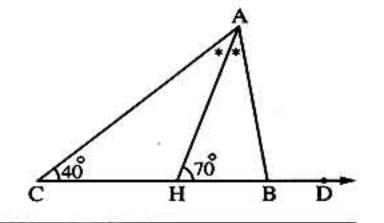
#### [b] In the opposite figure:

AH bisects ∠ BAC, D ∈ CB,

 $m (\angle AHB) = 70^{\circ}$ , and  $m (\angle ACH) = 40^{\circ}$ 

Find: (1) m ( $\angle$  BAC)

(2) m (∠ ABD)



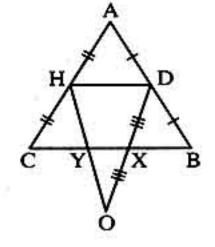
# 5 In the opposite figure:

D is the midpoint of AB, H is the midpoint of

AC and X is the midpoint of DO

Prove that: (1) Y is the midpoint of HO

(2) If: BC = 12 cm., then find XY



# Additional question

#### 1 Complete the following:

- (1) The image of the point (4, -1) by reflection in the origin point is .......
- (2) The number of axes of symmetry of the equilateral triangle is ........

# 2 In the opposite figure:

ABC is a triangle in which

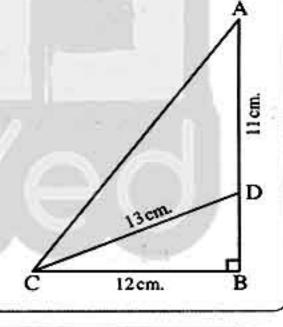
$$m (\angle B) = 90^{\circ}$$

 $D \in AB$ , where AD = 11 cm.

, if BC = 12 cm.

and DC = 13 cm.

Find the length of: BD and AC



# Kafr El-Sheik Governorate

# **Kallin Administration Zone**

# Kallin Exp. Lang. School

Answer the following questions:

#### Choose the correct answer:

- (1) The sum of the measures of the accumulative angles at a point is .........
  - (a) 90°
- (b) 180°
- (c) 270°
- (d) 360°
- (2) (-1, -3) is the image of (3, -1) by rotation about the origin with an angle of measure .....
  - (a) 90°
- (b)  $-90^{\circ}$
- (c) 180°
- $(d) 180^{\circ}$

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

- (3) ABCD is a parallelogram in which m ( $\angle$  B) + m ( $\angle$  D) = 130°, then m ( $\angle$  A) = ......
  - (a) 50°
- (b)  $65^{\circ}$
- (c) 115° (d) 150°
- (4) The measure of the interior angle of the regular hexagon = ......
  - (a) 90°
- (b) 135°
- (c) 120°
- (d) 60°
- (5) A parallelogram which its two diagonals are equal is = .......
- (a) rectangle.
- (b) square.
- (c) a , b together.

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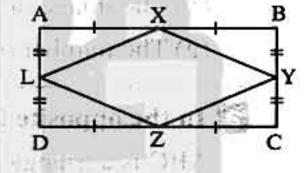
(d) rhombus.

# Complete the following:

- (1) Each two opposite angles of a parallelogram .........
- (3) If the polygon does not have reflex angle then it called ...... polygon.
- (4) The point (2, -1) is the image of the point (-1, 2) by translation  $(\dots, \dots)$ .
- (5) The ray drawn from the midpoint of a side of a triangle parallel to another side ..........
- 3 [a] Find the measure of each interior angle of regular octagon (with 8 sides)
  - [b] In the opposite figure : minorisories of a

ABCD is a rectangle and X, Y, Z and L are the midpoint of AB, BC, CD and DA respectively prove that:

- (1) XYZL is a rhombus.
- (2) The perimeter of the rhombus = 2 BD

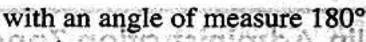


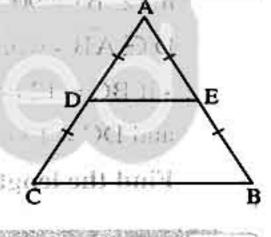
#### 4 [a] In the opposite figure:

ABC is an equilateral triangle of side length 12 cm.

- , then find the perimeter of ADE
- [b] On lattice draw ABC where A (4,0), B (0,3) and C (2,5)

Find the image of  $\triangle$  ABC by rotation around the origin point



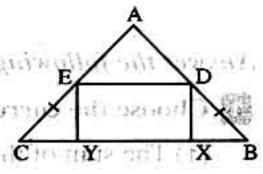


# [a] In the opposite figure :

EC = BD and DXYE

is a rectangle

Prove that :  $m (\angle ADE) = m (\angle AED)$ zi ming a na zolomi oznalnimnose so



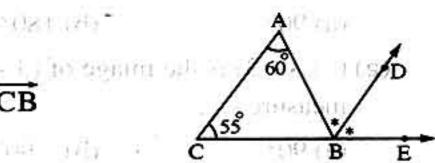
#### [b] In the opposite figure:

ABC is a triangle in which m  $(\angle A) = 60^{\circ}$ 

 $m (\angle C) = 55^{\circ}$ , and BD bisects  $\angle ABE$ ,  $E \in CB$ 

9名115年

Find: m (4 DBE)



بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواق

# **Additional question**

#### 1 Complete the following:

- (1) The image of the point (a , b) by reflection in the origin point is ........
- (2) In the right-angled triangle, the square of the length of the hypotenuse is equal to .....

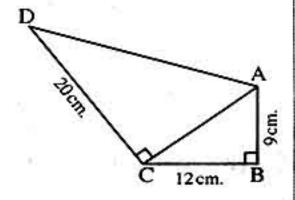
#### 2 In the opposite figure:

$$m (\angle B) = m (\angle ACD) = 90^{\circ}$$

$$AB = 9 \text{ cm.}$$
  $BC = 12 \text{ cm.}$ 

, CD = 20 cm.

Find the perimeter of the figure: ABCD



# El-Gharbia Governorate

#### West Mahalla El Kobra Admin.

#### Salah-Deen Exp. Language School

#### Answer the following questions:

#### 1 Choose the correct answer:

- (1)  $\overrightarrow{A}$  (2, -3) is the image of A by translation (x + 1, y + 1), then A is ......
  - (a)(1,0)
- (b) (1, -4)
- (c) (2, -2)
- (d) (3, -2)
- (2) The point (3, 5) is the image of the point (5, -3) by rotation about origin point with an angle of measure ......
  - (a) 90°
- (b) 180°
- $(c) -90^{\circ}$
- (d) 360°
- (3) ABCD is a parallelogram in which m ( $\angle A$ ) + m ( $\angle C$ ) = 110°, then m ( $\angle B$ ) = ......
  - (a) 50°
- (b) 125°
- (c) 130°
- (d) 45°
- (4) The image of the point (5,0) by reflection in X-axis is .......
  - (a) (5,0)
- (b) (0,5)
- (c) (0, -5)
- (d)(-5,0)
- (5) The sum of measures of interior angles of pentagon is ......
  - (a) 540°
- (b) 720°
- (c) 900°
- (d) 360°

# 2 Complete:

- (2) ABCD is a parallelogram in which m ( $\angle A$ ) = 130°, then m ( $\angle B$ ) = .......°
- (3) The image of point (3, 1) by reflection in y-axis is .........
- (4) The rhombus whose diagonals are equal in length is ........
- (5) The image of the point (3, -5) by rotation of angle 360° about origin point is ........

كراسة المعاصر رياضيات (لغات) / ١ إعدادي / تيرم ٢ (٢: ١٥)

# [3] [a] In the opposite figure:

ABCD is a parallelogram,

AD = 6 cm., DC = 3 cm., AM = 3.5 cm.

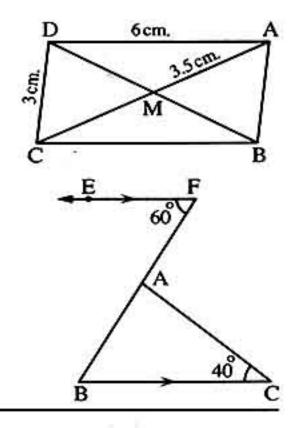
Find perimeter of triangle : ABC



FE // BC, 
$$m (\angle F) = 60^{\circ}$$
,

$$m (\angle C) = 40^{\circ}$$

Find:  $m (\angle BAC)$ 



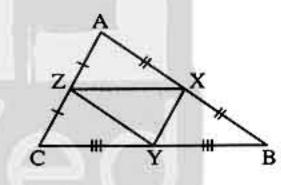
- 4 [a] ABCDE is a pentagon in which m ( $\angle$  A) = 140°,  $m (\angle B) = 130^{\circ} , m (\angle C) = 90^{\circ} , m (\angle D) = 110^{\circ}$ Find:  $m(\angle E)$ 
  - [b] Draw the equilateral triangle ABC of side length 5 cm., find the image of triangle ABC by rotation 60° about C
- [5] [a] Draw on square lattice the triangle ABC where: A(1,3), B(3,5) and C(5,0) Find the image of the triangle ABC by reflection in y-axis.

#### [b] In the opposite figure:

ABC is a triangle in which, X, Y, Z are midpoints of AB, BC and CA,

AB = 7 cm., BC = 9 cm., AC = 6 cm.

Find the perimeter of triangle: XYZ



# **Additional question**

#### 1 Complete the following:

- (1)  $\triangle$  XYZ is a right-angled triangle at Y , if XY = 4 cm. and YZ = 3 cm. , then XZ = .....
- (2) If the reflection in a straight line maps the figure to itself, then this straight line is called ......

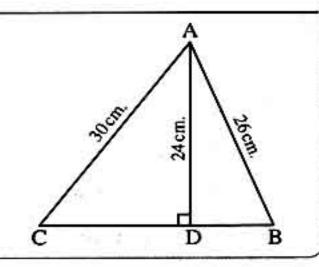
# 2 In the opposite figure :

ABC is a triangle in which AD \( \perp \) BC .

if AD = 24 cm., AB = 26 cm.,

AC = 30 cm.

Calculate the length of : BC



هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

# Damietta Governorate

# Damietta Lang. School

Answer the following questions:

#### Choose the correct answer:

- (1) The sum of measures of the interior angles of a triangle = .........
  - (a) 180°
- (b) 90°
- (c) 270°
- (d) 360°
- (2) ABCD is parallelogram, in which m ( $\angle$  B) = 150°, then m ( $\angle$  A) = ......
  - (a) 30°
- (b) 75°
- (c) 105°
- (d) 210°
- (3) The image of the point (5, -4) by reflection in the y-axis is the point ......
  - (a) (5,4)
- (b) (-5, -4) (c) (4, 5)
- (d)(-4,5)
- (4) The parallelogram whose diagonals are perpendicular and not equal is a ........
  - (a) square.
- (b) rectangle.
- (c) trapezium.
- (d) rhombus.

(5) In the opposite figure:

If B is the midpoint of AC, then the image of AC

by rotation about B with an angle of measure 180° is ......

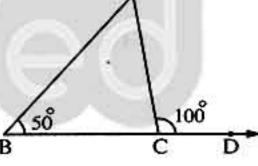
- (a)  $\{B\}$
- (b) AB
- (c) CA
- (d) CB

#### 2 Complete the following:

- (1) If two straight lines intersect, then each two vertically opposite angles are .........
- (2) In the opposite figure:

m (∠ CAB) = ······°

(3) The ray drawn from the midpoint of a side of triangle parallel to another side ..... the third side.



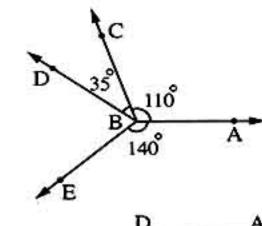
- (4) The measure of the interior angle of the regular hexagon = .....
- (5) The image of the point A (2, -1) is the point  $\widehat{A}(5, 1)$  by translation .......

# 3 [a] In the opposite figure:

 $m (\angle ABC) = 110^{\circ}, m (\angle CBD) = 35^{\circ},$ 

and m ( $\angle$  ABE) = 140°

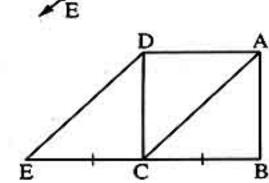
Find by proof: m (∠ EBD)



#### [b] In the opposite figure:

ABCD is a square  $, E \in BC , BC = CE$ 

- (1) Prove that: The figure CED is a parallelogram.
- (2) Find:  $m (\angle E)$



خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخ

# Fayoum Governorate

# Fayoum West Education Adm.

#### Azza Zidan E.L.S

Answer the following questions:

#### 1 Choose the correct answer:

- (1) The sum of measures of accumulative angles at a point is ........
  - (a) 360°
- (b) 180°
- (c) 90°
- (d) 270°
- (2) The image of (-2, 3) by rotation about the origin point with an angle of measure 180° is .....
  - (a) (-3, 2)
- (b) (3,-2) (c) (-3,-2) (d) (2,-3)
- (3) The sum of measures of the interior angles of an octagon = .......
  - (a) 540°
- (b) 720°
- (c) 1080°
- (d) 900°
- (4) If ABCD is a parallelogram in which m ( $\angle A$ ) = 70°, then m ( $\angle B$ ) = ......
  - (a) 70°
- (b) 180°
- (c) 90°
- (d) 110°
- (5) The image of (1, -2) by reflection in X-axis is ......
  - (a)(1,2)
- (b) (-1, -2) (c) (2, -1)
- (d)(-1,2)

#### 2 Complete each of the following:

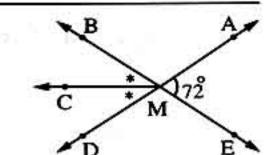
- (1) The line segment which joins two midpoints of two sides of a triangle is ........
- (2) The image of the point (3, 1) by translation (x-2, y-1) is ......
- (3) If the two diagonals of a parallelogram are equal in length and not perpendicular then it is called .....
- (4) The measure of each angle of a regular pentagon = .......

#### [3] [a] In the opposite figure:

 $\overrightarrow{DA} \cap \overrightarrow{EB} = \{M\}, \overrightarrow{MC} \text{ is a bisector}$ 

of ( $\angle$  BMD) and m ( $\angle$  AME) = 72°

Find:  $m (\angle CMD)$ 

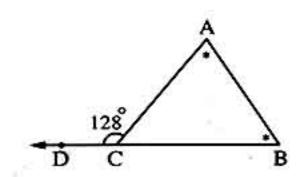


# [b] In the opposite figure:

 $D \in \overrightarrow{BC}, m (\angle ABC) = m (\angle BAC),$ 

and m ( $\angle$  ACD) = 128°

Find:  $m (\angle ABC)$ 



هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى





# 4 [a] In the opposite figure :

XYZ is a triangle in which XZ = 4 cm.

XY = 2.5 cm. and ZY = 3 cm., where

X, Y and Z are the midpoints of AB,

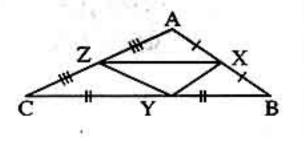
BC and CA

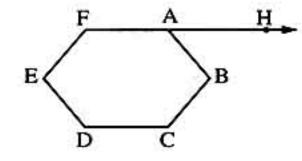
Find the perimeter of :  $\triangle$  ABC

#### [b] In the opposite figure:

ABCDEF is a regular hexagon , H∈FA

Find:  $m (\angle HAB)$ 

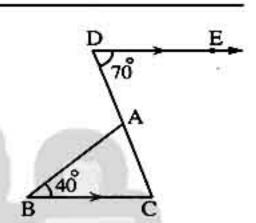




# 5 [a] In the opposite figure:

$$m (\angle D) = 70^{\circ}$$
, and  $m (\angle B) = 40^{\circ}$ 

Find: m (∠ DAB)



#### [b] In an orthogonal coordinates system with two dimensions:

Draw  $\triangle$  ABC in which A (-2,4), B (5,0) and C (3,-3), then find the image of  $\triangle$  ABC by reflection in y-axis.

# **Additional** question

#### 1 Choose the correct answer:

- (1) The point (2, -4) is the image of the point ...... by reflection in the origin point.
  - (a)(2,4)
- (b) (-2,4)
- (c) (-2, -4)
- (d) (2, -4)

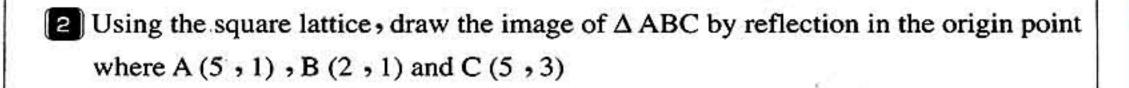
# (2) In the opposite figure:

If the area of  $\triangle$  ABC is 24 cm<sup>2</sup>.

and AB = 6 cm.,

then  $AC = \cdots cm$ .

- (a) 10
- (b) 100
- (c)64
- (d) 8



# 14 Beni Suef Governorate

# Ministry of Education Zone

#### Saad Bn ABe Wakas School

Answer the following questions:

#### 1 Choose the correct answer:

- (1) The sum of measures of the interior angles of a heptagon = .........
  - (a) 540°
- (b) 720°
- (c) 900°
- (d) 1080°
- (2) ABCD is a parallelogram in which :  $m (\angle B) + m (\angle D) = 150^{\circ}$ , then m  $(\angle A) = \cdots$ 
  - (a) 105°
- (b) 210°
- (c) 75°
- (d) 360°
- (3) The point (5, -3) is the image of the point (3, 5) by rotation about the origin point with an angle of measure .....
  - (a) 90°
- $(b) 90^{\circ}$
- (c) 180°
- (d) 360°
- (4)  $\triangle$  XYZ in which E and F and two midpoints of XY and XZ respectively , if YZ = 10 cm., then the length of  $EF = \cdots cm$ .
  - (a) 5
- (b) 10
- (c) 6
- (d) 8
- (5)  $\overrightarrow{A}$  (2, -3) is the image of A by translation (X + 1, Y + 1), then A is ...
  - (a)(1,0)
- (b) (1, -4)
- (c) (2, -2)
- (d) (3, -2)

# 2 Complete:

- (1) If two straight lines intersect, then the measure of each two vertically opposite angles .....
- (2) The image of point (0,4) by reflection in the y-axis is .........
- (3) If two opposite sides in the quadrilateral are parallel, then it is called ..........
- (4) The two diagonals are perpendicular in ...... and .........
- (5) The sum of measures of accumulative angles at a point = .......

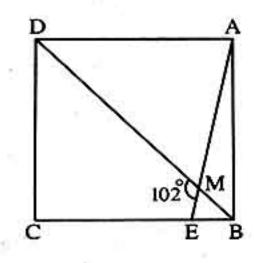
# [3] [a] In the opposite figure:

BD is a diagonal in the square ABCD,

 $m (\angle DME) = 102^{\circ}$ 

Find with proof:  $m (\angle MEC)$ 

[b] Find the number of sides of the regular polygon if the measure of one of its interior angles is 135°



هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى



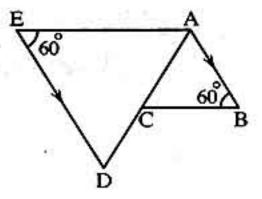


# 4 [a] In the opposite figure:

AB // ED and

$$m (\angle ABC) = m (\angle AED) = 60^{\circ}$$

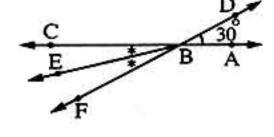
Prove that : BC // AE



#### [b] In the opposite figure:

$$\overrightarrow{AC} \cap \overrightarrow{DF} = \{B\}$$
, m ( $\angle ABD$ ) = 30°,  $\overrightarrow{BE}$  bisects  $\angle CBF$ 

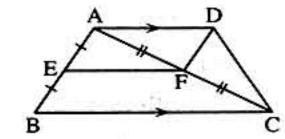
Find:  $m (\angle ABE)$ .



#### 5 [a] In the opposite figure :

 $\overline{AD} // \overline{BC}, BC = 2 AD$ 

Prove that: AEFD is parallelogram.



[b] Use the lattice to find the image of the triangle

LMN by the reflection in X-axis, where L(-4,-1), M(-1,-3), N(0,-1)

# Additional question

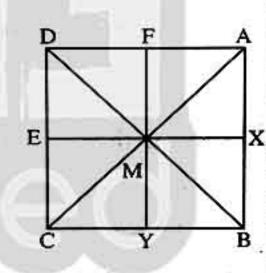
#### 1 In the opposite figure:

ABCD is a square of side length 6 cm.

M is the point of intersection of its diagonals.

X, Y, E and F are the midpoints of AB, BC,

CD and DA respectively.



#### Complete the following:

- (1) The image of the point A by reflection in M is .........
- (2) The image of AB by reflection in M is ......
- (3) The image of Δ AFM by reflection in M is ..........

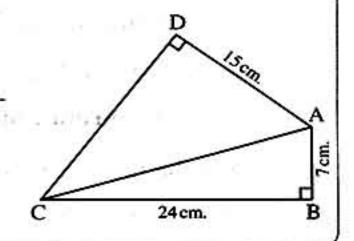
# 2 In the opposite figure :

$$m (\angle B) = m (\angle D) = 90^{\circ}$$

$$AB = 7 \text{ cm.}$$
,  $BC = 24 \text{ cm.}$ 

and AD = 15 cm.

Find the length of: DC



هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

# 15 Souhag Governorate

#### **Juhina Educational Administration**

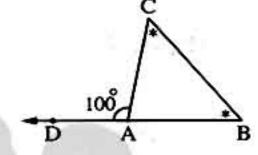
#### **Juhina Experimental Complex for Languages**

Answer the following questions:

#### 1 Complete the following:

- (1) The measure of each interior angle of the regular pentagon is .........°
- (2) If ABCD is a parallelogram and m ( $\angle A$ ) = 70°, then m ( $\angle B$ ) = ......°
- (3) The length of the line segment joining the two midpoints of two sides of a triangle equals ........
- (4) The image of the point (3 , -1) by translation (3 , 2) is .......
- (5) In the opposite figure:

$$D \subseteq BA$$
,  $m (\angle B) = m (\angle C)$ ,  
 $m (\angle CAD) = 100^{\circ}$ , then  $m (\angle C) = \cdots$ 



#### 2 Choose the correct answer:

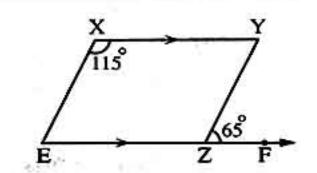
- (1) In  $\triangle$  ABC,  $m(\angle B) = m(\angle A) + m(\angle C)$ , then  $m(\angle B) = \cdots$ 
  - (a) 30°
- (b) 60°
- (c) 90°
- (d) 150°
- (2) The sum of measure of the interior angles of hexagon is .......
  - (a) 180°
- (b) 540°
- (c) 120°
- (d) 720°
- (3) The image of the point (-3,2) by reflection in y-axis is .......
  - (a) (3, -2)
- (b) (-3, -2)
- (c) (3,2)
- (d)(-3,2)
- (4) (-4,5) is the image of (5,4) by rotation in the origin point with an angle of measure ........
  - (a) 90°
- $(b) 90^{\circ}$
- (c) 180°
- (d) 360°
- (5) The sum of measures of the exterior angles of the triangle is ....
  - (a) 360°
- (b) 180°
- (c) 120°
- (d) 100°

# [3] [a] In the opposite figure :

$$\overrightarrow{XY} // \overrightarrow{EZ}$$
, m ( $\angle X$ ) = 115°,

and m ( $\angle$  YZF) = 65°

Prove that: XYZE is a parallelogram.



كراسة المعاصر رياضيات (لغات) / ١ إعدادي / تيرم ٢ (٢: ١٦)

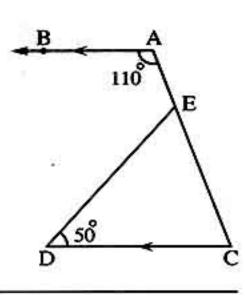
وقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع

#### [b] In the opposite figure:

$$, m (\angle A) = 110^{\circ}$$

$$m (\angle D) = 50^{\circ}$$

Find with proof :  $m (\angle AED)$ 

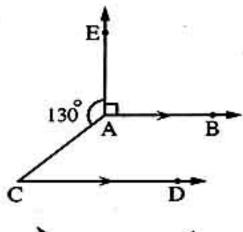


#### [4] [a] In the opposite figure:

$$\overrightarrow{AB} // \overrightarrow{CD}$$
 and m ( $\angle EAC$ ) = 130°,

$$m (\angle EAB) = 90^{\circ}$$

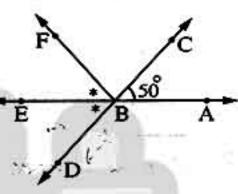
Find:  $m (\angle ACD)$ 



# [b] In the opposite figure : $\overrightarrow{AE} \cap \overrightarrow{CD} = \{B\}$ ,

$$m (\angle ABC) = 50^{\circ}$$
,

Find:  $m (\angle FBC)$ 



#### 5 Draw Δ ABC where A (1,5), B (3,1) and C (5,3), then draw its image

- (1) By reflection in X-axis.
- (2) By rotation about origin point with an angle of measure 180°

# **Additional question**

#### 1 Complete the following:

- (1) The number of axes of symmetry of the rectangle = .........
- (2) If  $(2 \ a \ , 3)$  is the image of  $(8 \ , -3)$  by reflection in the origin point, then  $a = \cdots$
- (3) If the reflection in a straight line maps the figure to itself, then this straight line is called .....

#### 2 In the opposite figure :

ABC is a triangle in which  $m (\angle B) = 90^{\circ}$ ,

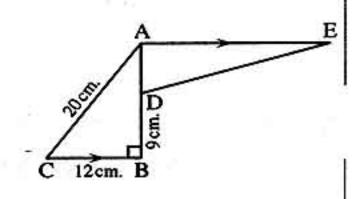
AE // BC

If: BC = 12 cm., AC = 20 cm.

 $D \in \overline{AB}$  where BD = 9 cm.

and AE = 2BC

Find the length of : AD , DE



#### Model Examinations of the School Book

# Model

Answer the following questions:

#### 1 Choose the correct answer from those given:

- (1) The sum of the measure of interior angle of a triangle equals ..........
  - (a) 90°
- (b) 180°
- (c) 270°
- (d) 360°
- (2) The image of the point (-1, 3) by translation (4, -2) is ......
  - (a)(3,1)
- (b) (3,-1)
- (c)(5,1)
- (d) (5, -5)
- (3) The measure of the exterior angle of the equilateral triangle is ..........
  - (a) 30°
- (b) 45°
- (c) 60°
- (d) 120°
- (4) In a parallelogram if the adjacent sides are equal in the length, then the shape is
  - (a) square.
- (b) rhombus.
- (c) rectangle.
- (d) trapezium.
- (5) The number of the diagonals of a pentagon is .........
  - (a) 3
- (b) 5
- (c) 7
- (d) 9

#### 2 Complete the following:

- (1) The image of the point (2, 1) by reflection in X-axis is ........
- (2) The image of the point (2, -1) by rotation about the origin point with an angle of measure 180° is .....
- (3) The square is a rectangle in which ........
- (4) ABCD is a parallelogram in which m (∠ A) = 60°, then m (∠ B) = ········
- (5) The image of the point (5,3) by translation:  $(x,y) \longrightarrow (x+3,y-1)$  is ......

#### [3] [a] In the opposite figure:

$$m (\angle A) = m (\angle B) = 25^{\circ}$$

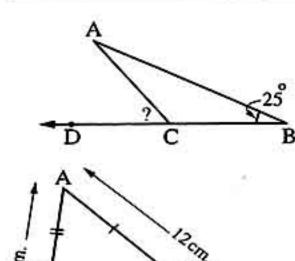
Find: m (∠ ACD)

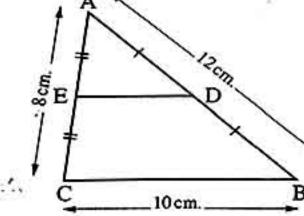
# [b] In the opposite figure:

 $\triangle$  ABC in which: AB = 12 cm.,

BC = 10 cm., AC = 8 cm.

Find the perimeter of :  $\triangle$  ADE





#### [4] [a] In the opposite figure:

$$\overrightarrow{DE} // \overrightarrow{YZ}$$
, m ( $\angle ZDE$ ) = 50°

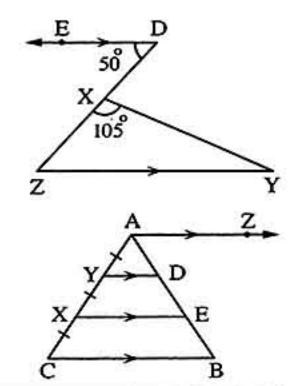
$$m (\angle YXZ) = 105^{\circ}$$

Find: 
$$m (\angle Z) \cdot m (\angle Y) \cdot m (\angle YXD)$$

#### [b] In the opposite figure:

$$AY = YX = XC$$
,  $AB = 18$  cm.,

Find the length of: EB



### [5] [a] In the opposite figure:

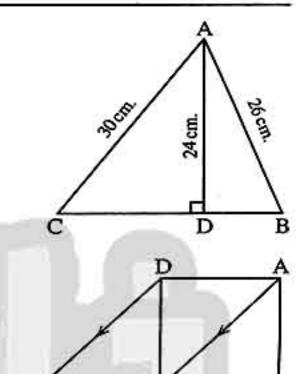
$$\overline{AD} \perp \overline{BC}$$
, if  $AD = 24$  cm.,

$$AB = 26 \text{ cm.}$$
,  $AC = 30 \text{ cm.}$ 

- (1) Find the length of: BC
- (2) Find the area of :  $\triangle$  ABC
- [b] ABCD is a square, E ∈ BC

AC // DE , Prove that

ACED is a parallelogram.

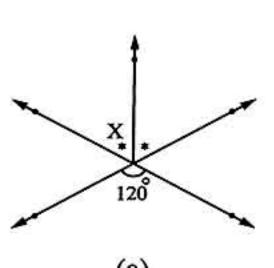


#### Model

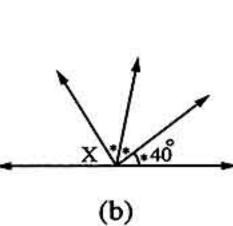
#### Answer the following questions:

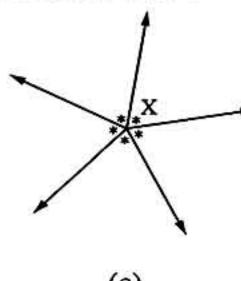
#### 1 Choose the correct answer from those given :

- (1) The image of the point (2, -5) by reflection in  $\mathcal{X}$ -axis is .......
  - (a) (2, -5)
- (b) (2,5)
- (c)(-2,-5)
- (d)(5,2)
- (2) The measure of each angle of regular hexagon equals .....
  - (a) 60°
- (b) 108°
- (c) 120°
- (d) 135°
- (3) The two diagonals are equal in the length and not perpendicular in .........
  - (a) parallelogram. (b) rectangle.
- (c) rhombus.
- (d) square.
- (4) All the following shapes m (\(\angle X\) = 60° except the shape ......

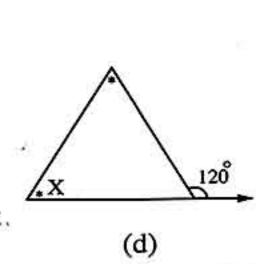


(a)





(c)

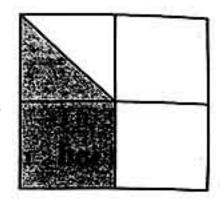


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#### (5) In the opposite figure:

The area of shaded part from the area of all shape equal .....

- (a)  $\frac{1}{8}$
- (b)  $\frac{1}{4}$
- (c)  $\frac{3}{8}$
- (d)  $\frac{3}{4}$

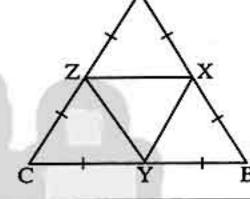


### 2 Complete the following:

- 1) The sum of the measures of the angles of the quadrilateral equals ...........
- (2) The image of the point (2,3) by translation MN, in direction MN, where M (2,-1), N (5 , 1) is .....
- (3) ABCD is parallelogram in which m ( $\angle A$ ) = 60°, then m ( $\angle B$ ) = ......
- (4) The ray drawn parallel to one side of a triangle and passing through the midpoint of another side .....

## (5) In the opposite figure:

The image of the triangle XBY by translation XZ in direction XZ is .....



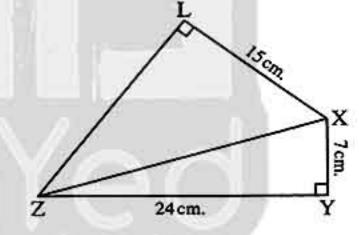
#### 3 [a] In the opposite figure:

XYZL is quadrilateral in which

$$m (\angle Y) = m (\angle L) = 90^{\circ}$$
,  $XY = 7$  cm.,

$$YZ = 24 \text{ cm.}$$
,  $XL = 15 \text{ cm.}$ 

Find the length of each of: XZ, LZ



[b] Using the square lattice, draw AB where

A 
$$(4,3)$$
, B  $(-1,1)$  then find the image of  $\overline{AB}$  by translation  $(x,y) \longrightarrow (x+2,y-1)$ 

[4] [a] Draw the image of triangle ABC where A(1,1), B(3,4), C(5,2) by reflection in X-axis.

#### [b] In the opposite figure:

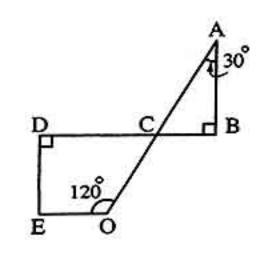
AB and ED, are perpendicular to

$$\overline{BD}$$
,  $\overline{BD} \cap \overline{AO} = \{C\}$ ,

$$m (\angle A) = 30^{\circ}$$

$$, m (\angle EOC) = 120^{\circ},$$

Find:  $m (\angle E)$ 



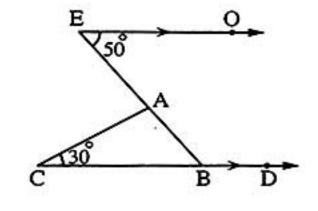
#### [5] [a] In the opposite figure:

$$\overrightarrow{EO} // \overrightarrow{CD}$$
, m ( $\angle E$ ) = 50°

, m (
$$\angle$$
 C) = 30°,

Find the measures of

angles of  $\triangle$  ABC, m ( $\angle$  ABD)



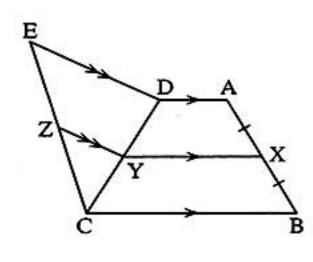
#### [b] In the opposite figure:

X is the midpoint of AB

$$,Y \in \overline{CD}, Z \in \overline{CE}$$

$$\overline{AD} / \overline{XY} / \overline{BC} , \overline{YZ} / \overline{DE}$$

is CZ = ZE? giving reason



#### Model

Answer the following questions:

#### 1 Choose the correct answer from those given:

- 1) The image of the point (3, -5) by reflection in y-axis is .......
  - (a)(3,5)
- (b) (-3, -5)
- (c)(-3,5)
- (d)(-5,3)
- (2) The sum of the measures of interior angles of a pentagon is ........
  - (a) 360°
- (b) 450°
- (c) 540°
- (d) 720°
- (3) The number of diagonals of quadrilateral is .......
  - (a) 2
- (b) 3
- (c) 4
- (d) 5

#### (4) In the opposite figure:

 $\triangle AB \hat{C}$  is the image

of  $\triangle$  ABC by rotation about A and with angle of measure .....

- (a) 30°
- (b) 80°
- (c) 110°
- (d) 140°
- (5) The diagonal of a square divided its vertex angle in two angles of the measure of each of them is .....
  - (a) 30°
- (b) 45°
- (c) 60°
- (d) 90°

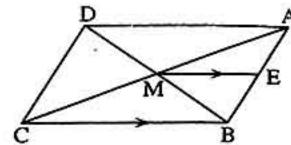
#### 2 Complete the following:

- 1) The rhombus is a parallelogram in which ..........
- (2) Each opposite angles in a parallelogram are .........
- (3) (-3,2) is the image of the point (3,2) by reflection in ......... axis.
- (4) The line segment joining the midpoint of two sides of a triangle is .........
- (5) The image of the point (4,6) by geometric transformation  $(x,y) \longrightarrow (-x,y-7)$ is .....

- [3] [a] Using the lattice, draw Δ ABC where A (1,0), B (0,2) and C (-3,1), then draw its image by reflection in X-axis.
  - [b] In the opposite figure:

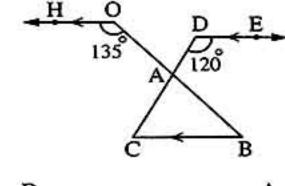
ABCD is a parallelogram, M is the intersection of its diagonals

Draw  $\overrightarrow{ME}$  //  $\overrightarrow{CB}$  is AE = EB? giving reason.



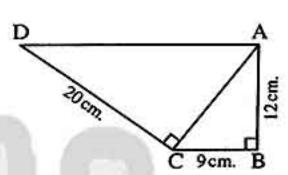
### [4] [a] In the opposite figure:

 $\overrightarrow{DE}$  //  $\overrightarrow{OH}$  //  $\overrightarrow{BC}$ , m ( $\angle$  ADE) = 120°, m ( $\angle$  AOH) = 135°, Calculate the measures of the angles of the triangle ABC



#### [b] In the opposite figure:

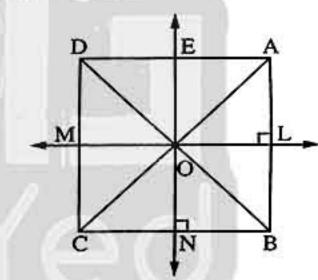
m (
$$\angle$$
 B) = m ( $\angle$  ACD) = 90°,  
AB = 12 cm., BC = 9 cm., CD = 20 cm.  
Find the length of each of:  $\overline{AC}$ ,  $\overline{AD}$ 



#### 5 In the opposite figure :

ABCD is a square of side length 6 cm. and the origin point its center. Find:

- (1) The image of  $\triangle$  AOL by translation 3 cm. in direction  $\overrightarrow{AB}$
- ② The image of Δ AOL by reflection in EN
- (3) The image of  $\Delta$  AOL by rotation about O and with an angle of measure (-90°)



# Model 4

#### Answer the following questions:

- 1 Choose the correct answer from those given :
  - (1) The parallelogram whose diagonals are perpendicular and not equal in length is called .........
    - (a) rhombus.
- (b) square.
- (c) rectangle.
- (d) trapezium.
- (2) The measure of each angle of a fegular pentagon is ......
  - (a) 90°
- (b) 108°
- (c) 120°
- (d) 136°
- (3) The triangle contains at least two ...... angles.
  - (a) acute
- (b) obtuse
- (c) right
- (d) reflex

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- (4) If ABCD is a parallelogram in which BC = 8 cm., CD = 6 cm., then its perimeter = .......
  - (a) 14 cm.
- (b) 28 cm.
- (c) 48 cm.
- (d) 56 cm.
- (5) The image of the point (2, -1) by reflection in X-axis is .......
  - (a) (2, 1)
- (b) (1, 2)
- (c) (-2,-1)
- (d)(-1,2)

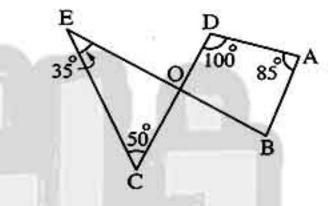
- 2 Complete the following:
  - (1) The line segment joining the midpoint of two sides of a triangle is ........
  - (2) In a parallelogram each opposite angles are .........
  - (3) The quadrilateral is a parallelogram if .........
  - (4) The image of the point (5, -3) by translation 3 units in negative direction of X-axis is ..........
  - (5) The image of the point (3, 2) by rotation with an angle of measure 180° about the origin is ..........
- 3 In the opposite figure :

$$\overline{DC} \cap \overline{BE} = \{O\}, m (\angle A) = 85^{\circ}$$

, m (
$$\angle$$
 D) = 100°, m ( $\angle$  E) = 35°, m ( $\angle$  C) = 50°



- 1) m (\( \text{DOB} \)
- (2) m (\( \precede B \))

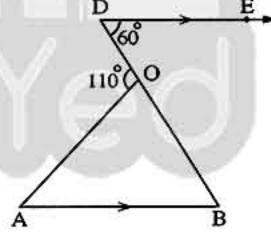


- [a] Find the length of the diagonal of a rectangle whose area 48 cm<sup>2</sup> and of width 6 cm.?
  - [b] In the opposite figure:

$$m (\angle D) = 60^{\circ}$$

$$, m (\angle AOD) = 110^{\circ}$$

Find with proof:  $m (\angle A)$ 

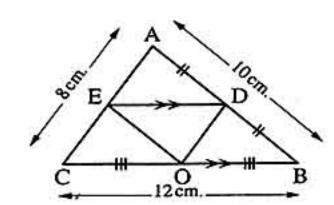


- [a] If the point A is the image of point B (-1,2) by reflection in y-axis, find the image of A by translation (-1,2)
  - [b] In the opposite figure:

ABC is a triangle in which D is the midpoint of  $\overline{AB}$ , O is the midpoint of  $\overline{BC}$ ,  $E \in \overline{AC}$  Such that  $\overline{DE}$  //  $\overline{BC}$ ,

AB = 10 cm., BC = 12 cm., AC = 8 cm.

- (1) Prove that: DBOE is a parallelogram.
- (2) Find the perimeter of :  $\Delta$  EDO



...

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بذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى في المعلقة المعل

# Model

Answer the following questions:

#### 1 Choose the correct answer from those given:

- 1) The image of the point (-3,4) by reflection in y-axis is ..........
  - (a) (3, -4)
- (b) (3,4)
- (c)(-3,-4)
- (d) (4, -3)
- (2) The sum of the measure of the exterior angles of a triangle equals .........
  - (a) 90°
- (b) 108°
- (c) 180°
- (d) 360°
- 3 The diagonals which are equal in the length and perpendicular in ..........
  - (a) square.
- (b) rhombus.
- (c) rectangle.
- (d) parallelogram.
- (4) The image of the point (-3,5) by rotation about the origin and with an angle of measure 90° is .....
  - (a) (5,3)
- (b) (-5,3) (c) (3,5)
- (d) (-5, -3)
- (5) The measure of each angle of regular octagon equals .......
  - (a) 108°
- (b) 120°
- (c) 135°
- (d) 144°

#### 2 Complete the following:

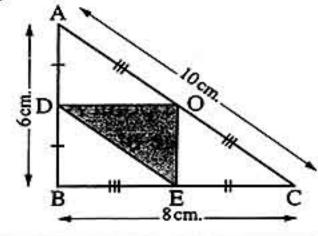
- 1) The parallelogram whose diagonals are perpendicular is ........
- (2) If the measure of an interior angle of a triangle is equal to the sum of the measures of the other two interior angles, then the triangle is ......
- 3 Any triagnle has at least two ..... interior angles.
- 4) The triagnle of the point (2, -4) by reflection in X-axis is .........
- (5) The image of the point (3, -2) by translation  $(x, y) \longrightarrow (x-1, y+6)$  is ......
- [3] [a] Prove that the ray drown parallel to one side of a triangle and passing through the midpoint of another side bisects the third side of the triangle.

#### [b] In the opposite figure:

D, E, O are midpoints of  $\overline{AB}$ ,  $\overline{BC}$ ,  $\overline{AC}$ resectively AB = 6 cm.

BC = 8 cm., AC = 10 cm.

Find the perimeter of :  $\Delta$  DEO

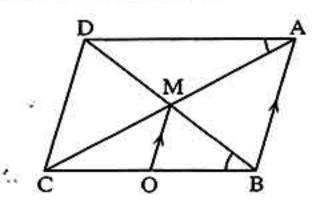


#### [4] [a] In the opposite figure:

ABCD is a parallelogram its diagonals are intersect at M, MO // AB

 $\overline{MO} \cap \overline{BC} = \{0\}$ 

Prove that: BO = OC



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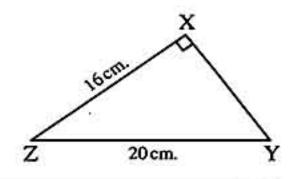
هذا العمل خاص بموقع ذاكرولى التعليمي ولا يسمح بتداوله على مواقع أخرى أفاكم الصف الاول الاعدادي صحيح الكيري التعليمي كالمعاص

#### [b] In the opposite figure:

XYZ is a triangle in which m ( $\angle X$ ) = 90°,

YZ = 20 cm., XZ = 16 cm.

Find the length of: XY

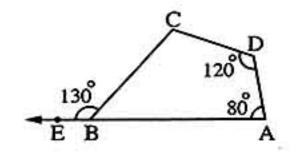


#### [5] [a] In the opposite figure:

$$m (\angle A) = 80^{\circ}, m (\angle D) = 120^{\circ}$$

$$m (\angle CBE) = 130^{\circ}$$

Find:  $m (\angle C)$ 



- [b] On a square lattice, draw the triangle whose vertices are A (4, 4) B (4, 2), C (1, 2) then determine each of the following:
  - 1) The coordinates of the image of  $\triangle$  ABC by translation 2AB in direction AB
  - (2) The image of Δ ABC by rotation about B and with an angle of measure 180°

# Model

#### Answer the following questions:

### 1 Choose the correct answer from those given :

- 1) The measure of each angle of the regular pentagon is ........
  - (a) 90°
- (b) 108°
- (c) 120°
- (d) 144°
- (2) The smallest number of the acute angle in any triangle is .
  - (a) zero
- (b) 1
- (c) 2
- (d) 3
- (3) The rhombus of diagonals are equal in length is ........
  - (a) square.
- (b) rectangle.
- (c) parallelogram.
- (d) trapezium.
- (4) The image of the point (2, -1) by reflection in X-axis is
- (b) (1, 2) (c) (-2, -1)
- (5) The image of the square by rotation about the origin point with an angle of measure 90° is .....
  - (a) rectangle.
- (b) square.
- (c) rhombus.
- (d) trapezium.

كراسة المعاصر رياضيات (لغات) / ١ إعدادي / تيرم ٢ (٢: ١٢)

#### 2 Complete the following:

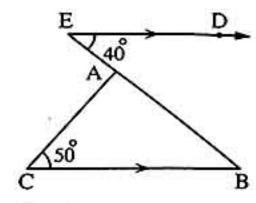
- (1) The measure of the exterior angle of a triangle is .........
- (2) The parallelogram whose diagonals are equal in length and perpendicular is ........
- (3) ABCD is a parallelogram in which m ( $\angle A$ ) = 50°, then m ( $\angle B$ ) = ......
- (4) The image of the point (-4, 5) by translation (2, -3) is ......
- (5)  $\Delta XYZ$ , m ( $\angle Y$ ) = 90°, then  $(XZ)^2 = \cdots$

#### [3] [a] In the opposite figure:

$$\overrightarrow{ED} // \overrightarrow{CB}, m (\angle C) = 50^{\circ}$$

$$m (\angle E) = 40^{\circ}$$

Prove that : 
$$\overline{AC} \perp \overline{BE}$$



[b] Draw  $\triangle$  OBC on a square lattice where O (0,0), B (3,0), C (0,4) then find its image by rotation about the origin point with an angle of measure 180°

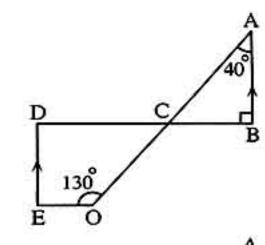
### [4] [a] In the opposite figure:

$$\overline{BD} \cap \overline{AO} = \{C\}, \overline{AB} // \overline{DE},$$

$$m (\angle A) = 40^{\circ}, m (\angle B) = 90^{\circ},$$

$$m (\angle COE) = 130^{\circ}$$

Find: 
$$m (\angle E)$$

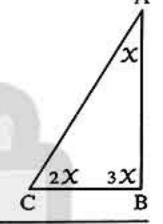


#### [b] In the opposite figure:

Find with proof the

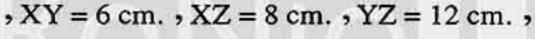
measures of the angles

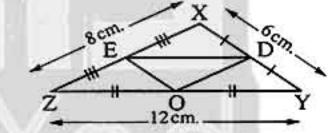
of A ABC



#### [5] [a] In the opposite figure:

XYZ is a triangle in which D, E, O are





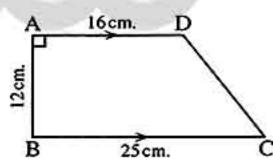
# Find the perimeter of : $\triangle$ DOE

#### [b] In the opposite figure:

ABCD is a trapezium in which AD // BC

$$m (\angle A) = 90^{\circ} AB = 12 \text{ cm.} BC = 25 \text{ cm.} AD = 16 \text{ cm.}$$

Find the length of: DC



#### Model

#### Answer the following questions:

### 1 Choose the correct answer from those given:

- (1) The measure of each angle of the regular hexagon is ........
  - (a) 108°
- (b) 120°
- (c) 136°
- (d) 144°
- (2) Any triangle has at least two ..... interior angles.
  - (a) acute
- (b) right
- (c) obtuse
- (d) straight

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- (3) The diagonals of the rectangle are ......
  - (a) parallel.

(b) perpendicular.

(c) equal in the length.

- (d) equal in length & perpendicular.
- (4) The image of a triangle by rotation about the origin point with an angle of measure 180° is .....
  - (a) triangle.
- (b) line segment.
- (c) point.
- (d) straight line.
- (5) The image of the point (3, -2) by reflection in y-axis ........
  - (a) (3, 2)
- (b) (-3, -2) (c) (-3, 2) (d) (-2, 3)

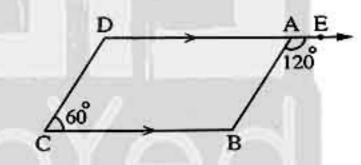
#### 2 Complete the following:

- (1) The sum of the measures of the interior angles of a pentagon equals .........
- (2) The measure of the exterior angle of an equilateral triangle = .......... at one of its vertices.
- (3) The rectangle is a parallelogram in which one of its angles is ........
- (4) The image of the point (-4, 5) by translation (2, -3) is ......
- (5) If the image of the point (-4,0) by rotation about the origin point is (0,-4), then the measure of rotation angle is ......

#### [3] [a] In the opposite figure:

$$E \in DA$$
,  $m (\angle EAB) = 120^{\circ}$   
 $m (\angle C) = 60^{\circ}$ ,  $\overrightarrow{DA} // \overrightarrow{CB}$ 

Prove that: ABCD is a parallelogram.



#### [b] In the opposite figure:

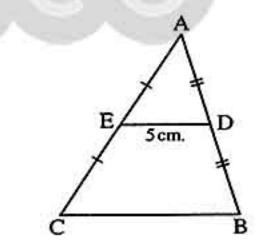
ABC is a triangle in which D

, E are the midpoints

of AB, AC respectively

5DE = 5 cm.

Find the length of : BC



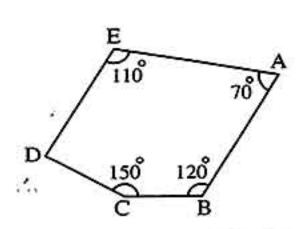
#### [a] In the opposite figure:

ABCDE is a pentagon in which m ( $\angle A$ ) = 70°

$$m (\angle B) = 120^{\circ} m (\angle C) = 150^{\circ}$$

$$m (\angle E) = 110^{\circ}$$

**Find**:  $m (\angle D)$  with proof.



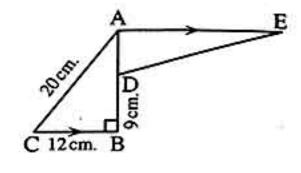
#### [b] In the opposite figure:

 $\triangle$  ABC in which m ( $\angle$  B) = 90°,  $\overline{AE}$  //  $\overline{BC}$ ,

if BC = 12 cm. AC = 20 cm.  $D \in \overline{AB}$ 

such that: BD = 9 cm., AE = 2 BC,

Find the length of each: AD, ED



#### [5] [a] In the opposite figure:

ABCD is a parallelogram in which

 $AB = 5 \text{ cm.}, BC = 8 \text{ cm.}, m (\angle B) = 135^{\circ}$ 

Find:

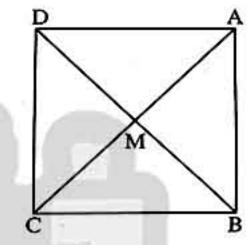
- (1) m (\(\perp C\))
- (2) The perimeter of parallelogram ABCD

#### [b] In the opposite figure:

ABCD is a square, whose diagonals intersect at M.

Find:

- (1) The image of  $\triangle$  ABC by reflection in AC
- (2) The image of  $\Delta$  MAB by rotation about M with measure (-90°)



#### Model 8

#### Answer the following questions:

#### 1 Choose the correct answer from those given :

- (1) The diagonal of square makes angle of measure ...... with any of its sides.
  - (a) 45°
- (b) 60°
- (c) 90°
- (d) 120°

8cm.

- (2) The measure of any of the exterior angle of an equilateral triangle equals ......
  - (a) 60°
- (b) 90°
- (c) 120°
- (d) 180°
- (3) In  $\triangle$  ABC if m ( $\angle$   $\hat{A}$ ) > m ( $\angle$  B) + m ( $\angle$  C) then the angle A is .......
  - (a) acute.
- (b) right.
- (c) obtuse.
- (d) straight.
- (4) The sum of the measures of any two consecutive angles in a parallelogram equals ......
  - (a) 90°
- (b) 180°
- (c) 270°
- (d) 360°
- (5) The image of the point (5, -3) by rotation about the origin point is itself, then the measure of rotation angle is .....
  - (a) 90°
- (b) 180°
- (c) 270°
- : (d) 360°





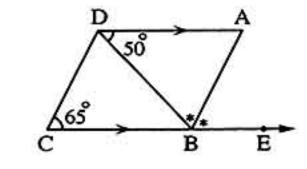
### 2 Complete the following:

- (1) The length of a line segment joining the midpoints of two sides of a triangle equals .........
- (2) The parallelogram whose diagonals are perpendicular and of equal in length is ........
- (3) The parallelogram whose perimeter 24 cm. and the length of one of its sides is 7 cm., then the length of its adjacent side equals ..........
- (4) The image of the point (3, 4) by reflection in the X-axis is .......... and its image by reflection in the y-axis is ..........
- (5) If the image of the point (-1,3) by a translation is (1,4) then the image of the point (3,-2) by the same translation is ........

## [3] [a] In the opposite figure:

$$\overrightarrow{DA}$$
 //  $\overrightarrow{BE}$ ,  $\overrightarrow{BA}$  bisects  $\angle$  DBE,  $\overrightarrow{m}$  ( $\angle$  ADB) = 50°,  $\overrightarrow{m}$  ( $\angle$  C) = 65°

Prove that: ABCD is a parallelogram



[b] Draw the triangle ABC in which AB = AC = 5 cm., BC = 6 cm., then draw its image by rotation about A with an angle of measure  $270^{\circ}$ 

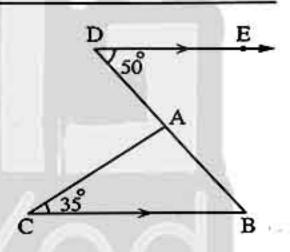
#### 4 [a] In the opposite figure:

$$\overrightarrow{DE} // \overrightarrow{CB}$$
, m ( $\angle D$ ) = 50°

$$m (\angle C) = 35^{\circ}$$

Find:  $\bigcirc$  m ( $\angle$  B)

(2) m (\( \subseteq \text{BAC} \)



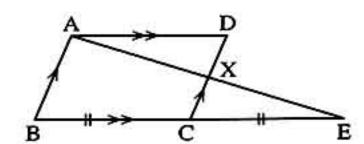
[b] Draw the triangle ABC in which AB = 3 cm., BC = 4 cm., m (∠ ABC) = 90°, then draw its image by reflection in straight line BC

#### [5] [a] In the opposite figure:

ABCD is a parallelogram  $, E \in \overrightarrow{BC}$ 

Such that : 
$$CE = BC \rightarrow \overline{AE} \cap \overline{DC} = \{X\}$$

Prove that : AX = XE



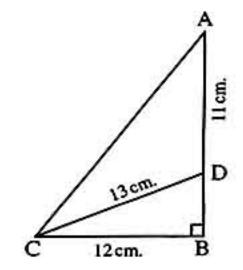
#### [b] In the opposite figure:

ABC is a triangle in which m ( $\angle B$ ) = 90°,  $D \in \overline{AB}$ 

Such that : AD = 11 cm.

, if BC = 12 cm., DC = 13 cm.,

Find the length of each of :  $\overline{BD}$ ,  $\overline{AC}$ 



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#### **School Examinations**

# Cairo Governorate

#### El-Wayli Educational Zone

#### Sakr Koreish (E.L.S)

#### Answer the following questions:

#### 1 Choose the correct answer:

- (1) The sum of the measures of the exterior angles of a polygon = ........
  - (a) 180°
- (b) 360°
- (c) 540°
- (d) 720°
- (2) The sum of the measures of the interior angles of a right-angled triangle = ........
  - (a) 180°
- (b) 90°

- (c) 60°
- (d) 30°
- (3) The image of the point (8, -2) by reflection on X-axis is .......
  - (a) (8, 2)
- (b) (8, -2)
- (c) (-8, -2)
- (d)(-8,2)
- (4) ABCD is a rectangle in which m (∠ BAC) = 40°, then m (∠ DAC) = .......
  - (a) 360°
- (b) 90°

- (c) 50°
- (d) 40°
- (5) In Δ ABC: if X, Y are the midpoints of AC and BC respectively, then XY // .........
  - (a) AB
- (b) BC

- (c) AC
- (d) CY

#### 2 Complete each of the following:

- (1) The image of the point (-5,0) by reflection on X-axis is ........
- (2) If XYZL is a rhombus, then ...... \precedent ......
- (3) Any triangle has at least two ..... interior angles.
- (4) The ray drawn from the midpoint of a side of a triangle parallel to another side ..... the third side.
- (5) The image of the point (7,5) is (5,-7) by rotation about the origin with an angle of measure .....

#### [3] [a] In the opposite figure:

 $\overline{AD} \perp \overline{BC}$  if AD = 24 cm., AB = 26 cm.,

AC = 30 cm., find: the length of BC, then

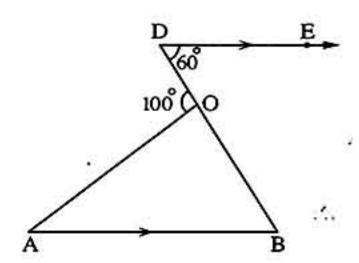
Find: the area of  $\triangle$  ABC

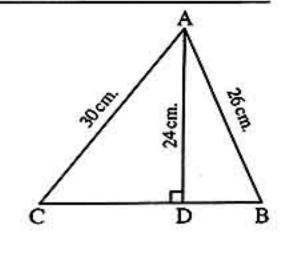
#### [b] In the opposite figure:

 $\overline{AB} // \overline{DE}$ , m ( $\angle D$ ) = 60°

 $, m (\angle AOD) = 100^{\circ}$ 

Find with proof:  $m (\angle A)$ 

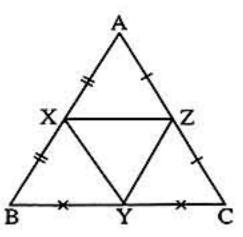




[4] [a] In the opposite figure:

$$XY = 14 \text{ cm.}$$
,  $YZ = 12 \text{ cm.}$  and  $XZ = 10 \text{ cm.}$ ,  $X \cdot Y$  and  $Z$  are the midpoints of  $\overline{AB} \cdot \overline{BC}$  and  $\overline{CA}$ 

respectively. Calculate the perimeter of :  $\triangle$  ABC.



[b] On the lattice. Draw  $\triangle$  ABC where A (-1,3), B (-4,2) and C (-2,5), then draw its image under the translation of magnitude MN in the direction of MN in which M (3, -2) aand N (8, 1)

5 [a] In the opposite figure:

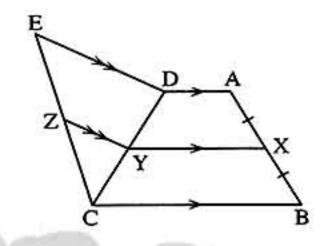
X is the midpoints of AB,

YECD, ZECE,

AD // XY // BC

, YZ // DE

Prove that : CZ = ZE



[b] Draw the square ABCD in which A (1, 1), B (4, 1), C (4, 4), and D (1, 4) Then draw its image by rotation with angle – 90° about the origin.

Cairo Governorate

**El-Nozha Directorate** 

Sunrise Language Schools

Answer the following questions:

1 Choose the correct answer:

(1) The measure of each angle of regular hexagon = ........

(a) 60°

- (b) 108°
- (c) 120°
- (d) 135°
- (2) The image of the point (-3,5) by rotation about the origin and with an angle with measure 90° is .....

(a) (5,3)

- (b)(-5,3)
- (c)(3,5)
- (d)(-5,-3)
- (3) The measure of any of the exterior angle of an equilateral triangle equals ........

(a) 60°

(b) 90°

- (c) 120°
- (d) 180°
- (4) The diagonal of square divided its vertex angle into two angles of the measure of each of them is .....

(a) 30°

(b) 45°

- (c) 60°
- (d) 90°

(5) The sum of the measure of any two consecutive angles in a parallelogram equals .........

(a) 180°

(b) 90°

- (c) 270°
- (d) 360°

# Maths

#### Final Examinations

#### 2 Complete each of the following:

- (1) ABC is a right-angled triangle at B if AB = 5 cm., AC = 13 cm., then BC = ..... cm.
- (2) The image of the point (5,3) by translation  $(x,y) \longrightarrow (x+3,y-1)$  is .......
- (4) (-3,2) is the image of the point (3,2) by reflection in ...... axis.
- (5) The parallelogram whose diagonals are perpendicular and not equal in length is called .....

# [3] [a] In the opposite figure : DE // OH // BC

$$m (\angle ADE) = 120^{\circ}$$

$$m (\angle AOH) = 135^{\circ}$$

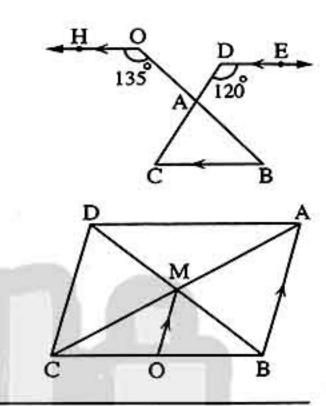
Find the measures of the angles of :  $\triangle$  ABC

#### [b] In the opposite figure:

ABCD is a parallelogram its diagonals are intersect at M,

$$\overline{MO} // \overline{AB}, \overline{MO} \cap \overline{BC} = \{0\}$$

Prove that : BO = OC



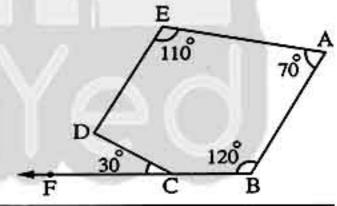
[4] [a] Using the lattice. Draw Δ ABC where A (1,0), B (0,2) and C (-3,1), then draw its image by reflection in X-axis.

### [b] In the opposite figure:

ABCDE is pentagon in which m ( $\angle A$ ) = 70°

$$m (\angle B) = 120^{\circ} m (\angle E) = 110^{\circ} m (\angle DCF) = 30^{\circ}$$

Find with proof:  $m (\angle D)$ 



#### [5] [a] In the opposite figure:

 $\overline{AD} \perp \overline{BC}$ , if AD = 24 cm., AB = 26 cm., AC = 30 cm.

Find: (1) The length of BC

(2) The area of ∆ ABC

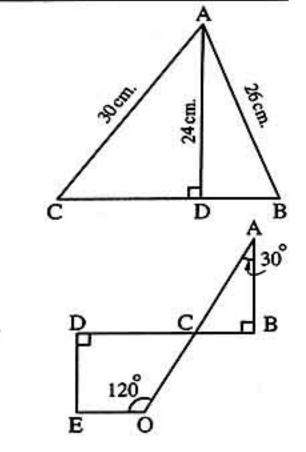
#### [b] In the opposite figure:

AB, ED are perpendicular to BD,

$$\overline{BD} \cap \overline{AO} = \{C\}$$
, m ( $\angle A$ ) = 30°

 $m (\angle EOC) = 120^{\circ}$ 

Find:  $m (\angle E)$ 



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# 3 Cairo Governorate

#### **El-Zawia Educational Zone**

Answer the following questions:

#### 1 Choose the correct answer:

(1) The image of the point (2,-1) by reflection in y-axis is .......

(a)(2,1)

- (b) (1, 2)
- (c) (-2, -1)
- (d) (-1, 2)
- (2) The measure of each angle of regular hexagon equal .....

(a) 108°

- (b) 120°
- (c) 135°
- (d) 144°
- (3) The measure of the exterior angle of the equilateral triangle is .........

(a) 30°

- (b) 45°
- (c) 60°
- (d) 120°

4 In the opposite figure:

 $\triangle AB\hat{C}$  is the image of

Δ ABC by rotation about A

and with angle of measure ......

- (a) 30°
- (b) 80°
- (c) 110°
- (d) 140°
- (5) If ABCD is a square then m ( $\angle$  ACB) = ......
  - (a) 90°
- (b) 60°
- (c) 45°
- (d) 30°

### 2 Complete each of the following:

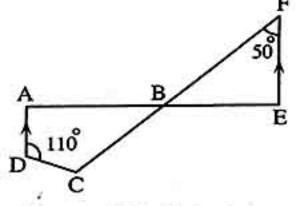
- (1) ABCD is a parallelogram in which m (∠ A) = 50° then m (∠ B) = ········
- ② The image of the point (3, -2) by translation  $(x, y) \longrightarrow (x-1, y+6)$  is .......
- 3 The sum of measures of the interior angles of the triangle = .........
- (4) The ray drawn from the midpoint of a side of triangle parallel to another side ........
- (5) In  $\triangle$  ABC: If m ( $\angle$  A) + m ( $\angle$  C) = m ( $\angle$  B), then m ( $\angle$  B) = ......°

#### 3 [a] In the opposite figure:

$$\overline{AD} // \overline{EF}$$
, m ( $\angle E$ ) = 90°

$$m (\angle F) = 50^{\circ} \cdot m (\angle D) = 110^{\circ}$$

Find:  $m (\angle C)$ 



[b] Find the number of sides of a regular polygon if the measure of one of its interior angles is 135°

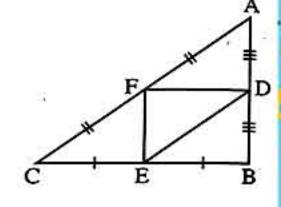
#### [4] [a] In the opposite figure:

ABC is a triangle in which AB = 6 cm.

BC = 8 cm., AC = 10 cm. and  $D \cdot E \cdot F$ 

are the midpoints of AB, CB, AC

Find the perimeter of  $\Delta$  DEF.



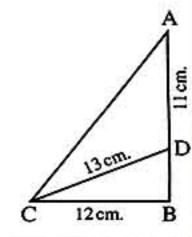
#### [b] In the opposite figure:

ABC is a triangle in which

$$m (\angle B) = 90^{\circ}, D \in \overline{AB}$$
 where  $AD = 11$  cm.,

BC = 12 cm. and DC = 13 cm.

Find the length of: BD and AC



#### 5 Draw Δ ABC where A (1,5), B (3,1) and C (5,3), then draw its image:

- (1) By reflection in X-axis.
- (2) By rotation about origin point with an angle of measure 180°.

# Giza Governorate

## Inspection of Mathematics

#### **Experimental Directory**

#### Answer the following questions:

# 1 Choose the correct answer:

- 1) The sum of measures of accumulative angles at a point is ........
  - (a) 360°
- (b) 180°
- (c) 90°
- (d) 270°
- (2) The image of (-2, 3) by rotation about the origin point with an angle of measure 180° is .....
  - (a) (-3, 2)
- (b) (3, -2) (c) (-3, -2) (d) (2, -3)
- (3) The sum of measures of the interior angles of an octagon = .........
  - (a) 540°
- <sub>~</sub> (b) 720°
- (c) 1080°
- (d) 900°
- (4) If ABCD is a parallelogram in which m ( $\angle A$ ) = 70°, then m ( $\angle B$ ) = ......
  - (a) 70°
- (b) 180°
- (c) 90°
- (d) 110°
- (5) The image of (1, -2) by reflection in X-axis is ......
  - (a)(1,2)
- (b) (-1, -2)
- (c) (2, -1)
- (d)(-1,2)

#### 2 Complete each of the following:

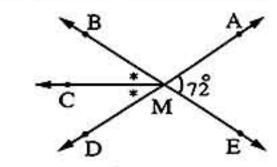
(1) The line segment which joins two midpoints of two sides of a triangle is .........

- (2) The image of the point (3, 1) by translation (x-2, y-1) is .......
- (3) If the two diagonals of a parallelogram are equal in length and not perpendicular, then it is called .....
- (4) The measure of each angle of a regular pentagon = ..........°
- (5) The sum of measures of the interior angles of the triangle = ......°

#### [3] [a] In the opposite figure :

$$\overrightarrow{DA} \cap \overrightarrow{EB} = \{M\}$$
,  $\overrightarrow{MC}$  is a bisector of  $(\angle BMD)$  and m  $(\angle AME) = 72^{\circ}$ 

Find:  $m (\angle CMD)$ 

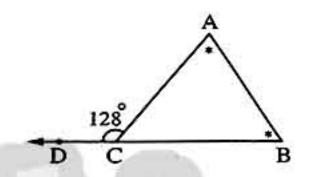


#### [b] In the opposite figure:

$$D \in \overrightarrow{BC}$$
, m ( $\angle ABC$ ) = m ( $\angle BAC$ )

and m ( $\angle$  ACD) = 128°

Find:  $m (\angle ABC)$ 



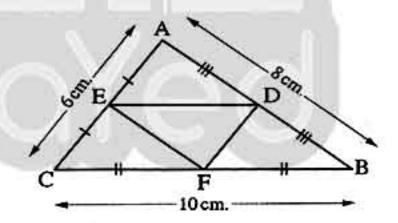
[a] Draw the image of  $\triangle$  XYZ in which XY = 5 cm., YZ = 4 cm. and ZX = 3 cm. by reflection in the straight line YX

#### [b] In the opposite figure:

ABC is a triangle in which D, E and F are midpoints of AB, AC and CB respectively.

If: AB = 8 cm. BC = 10 cm. AC = 6 cm.

Find the perimeter of :  $\triangle$  DEF

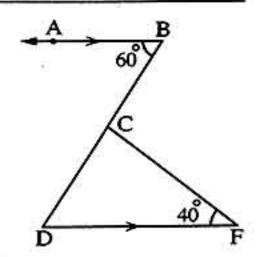


### [5] [a] In the opposite figure:

$$\overrightarrow{BA} // \overrightarrow{FD}$$
, m ( $\angle B$ ) = 60°

and m ( $\angle$  F) = 40°

Find:  $m (\angle DCF)$ 



- [b] Using the square lattice. Draw  $\triangle$  ABC in which A (2, 1)
  - , B (1, 4) and C (3, 3), then find its image by rotation about the origin point with an angle of measure 90°



# Giza Governorate

### Experimental Language Schools

Answer the following questions:

#### 1 Choose the correct answer:

- (1) ABCD is a parallelogram if m ( $\angle A$ ) = 130°, then m ( $\angle B$ ) = ......
  - (a) 130°
- (b) 50°
- (c) 40°
- (d)  $65^{\circ}$
- (2) The image of the point (3, -2) by reflection in X-axis is .......
  - (a) (3, -2)
- (b) (-3, -2)
- (c)(3,2)
- (d)(-3,2)
- (3) The sum of the measures of the interior angles of octagon is .........
  - (a) 720°
- (b) 900°
- (c) 1080°
- (d) 1260°
- (4) The sum of the measures of the exterior angles of pentagon is .......
  - (a) 540°
- (b) 360°
- (c) 180°
- (d) 720°
- (5) The measure of an interior angle of regular hexagon is .......
  - (a) 60°
- (b) 90°
- (c) 120°
- (d) 108°

#### Complete each of the following:

- 2) The image of the point (3, 2) by translation (-1, 3) is .......
- (3) ABC is a triangle,  $m (\angle B) = 90^{\circ}$ , AB = 6 cm, AC = 10 cm, then  $BC = \dots \text{cm}$ .
- (4) In the square, two diagonals are ....... and ........
- (5) A quadrilateral in which only two opposite sides are parallel is called a .........

### [3] [a] Using the square lattice draw $\triangle$ ABC: A = (5, 5), B = (5, 1), C = (1, 1),then find its image by rotation about the origin point with an angle of measure 180°

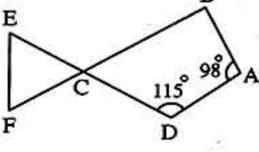
#### [b] In the opposite figure:

ABCD is a quadrilateral,

. 
$$m (∠ D) = 115^{\circ} , m(∠ A) = 98^{\circ}$$

, EC = CF = FE , 
$$\overline{BF} \cap \overline{ED} = \{C\}$$

Find with proof:  $m (\angle B)$ 



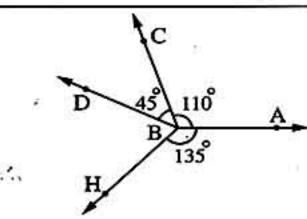
#### [4] [a] In the opposite figure:

$$m (\angle ABC) = 110^{\circ}$$

$$m (\angle CBD) = 45^{\circ}$$

$$m (\angle ABH) = 135^{\circ}$$

Find: m (∠ HBD)



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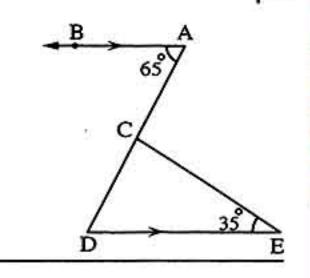
#### [b] In the opposite figure:

$$\overrightarrow{AB} /\!/ \overrightarrow{ED}$$
,

$$m (\angle A) = 65^{\circ}$$
,

$$m (\angle E) = 35^{\circ}$$

Find with proof :  $m (\angle ACE)$ 



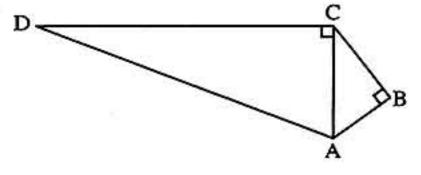
#### [5] [a] In the opposite figure:

$$m (\angle B) = m (\angle ACD) = 90^{\circ}$$

$$AB = 3 \text{ cm.} BC = 4 \text{ cm.}$$

$$CD = 12 cm.$$

Find: AD and perimeter of the figure ABCD

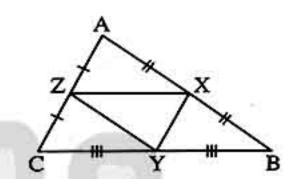


#### [b] In the opposite figure:

$$\overline{BC}$$
 and  $\overline{AC}$ ,  $AB = 10 \text{ cm}$ ,

$$BC = 11 \text{ cm}$$
,  $AC = 9 \text{ cm}$ 

then find the perimeter of  $\Delta XYZ$  with proof.



# Alexandria Governorate

#### Al Montazah Zone

#### Math's Supervision

Answer the following questions:

# Choose the correct answer:

- (1) A parallelogram in which diagonals are equal in length is ........
  - (a) square.
- (b) rectangle.
- (c) rhombus.
- (d) trapezium.
- (2) The image of the point (3,4) by reflection in y-axis is ......
  - (a) (-3, -4)
- (b) (-3,4)
- (c)(-4,3)
- (d) (4, -3)

- (3) (-2,1) Reflection  $\rightarrow$  .....
  - $_{-}(a)(2,1)$
- (b) (2,-1)
- (c) (-2, -1)
- (d) (1, -2)
- (4) The sum of measures of each two consecutive angles in a parallelogram is .......
  - (a) 90°
- (b) 120°
- (c) 180°
- (d) 360°

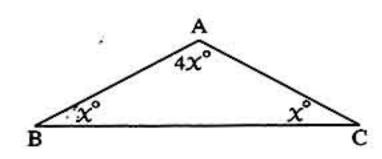
# (5) In the opposite figure:

(a) 20°

 $(b) 30^{\circ}$ 

(c) 60°

(d) 180°



#### 2 Complete each of the following:

- (1) The sum of the measures of the accumulative angles at a point is equal to .........
- (2) If ABCD is a rhombus, then  $\dots$
- (3) The image of the point P (5,4) under translation  $(x,y) \longrightarrow (x+4,y-5)$  is ......
- (4) If ABC is a right-angled triangle at B, then  $(AB)^2 = \cdots \cdots$
- (5) The ray drawn from the midpoint of a side of a triangle parallel to another side ........

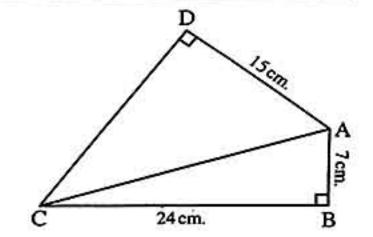
#### [3] [a] In the opposite figure:

$$m (\angle D) = m (\angle B) = 90^{\circ} AB = 7 cm.$$

BC = 24 cm. and AD = 15 cm.

Find with proof: AC and DC.

[b] How many sides does a regular polygon have if the measure of each interior angle of it is 120°?



#### [4] [a] In the opposite figure:

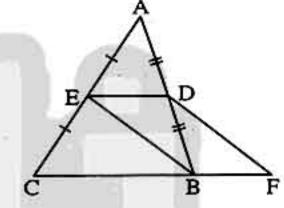
D and E are the midpoints of  $\overline{AB}$  and  $\overline{AC}$  respectively,

 $F \in \overrightarrow{CB}$  where  $BF = \frac{1}{2}BC$ 

Prove that:

BEDF is a parallelogram.

[b] On the lattice, find the image of the trianle ABC Where A (-4, -1), B (-1, -3) and C (0, -1) by reflection on the X-axis.

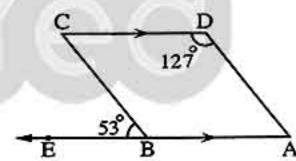


#### [5] [a] In the opposite figure :

 $\overrightarrow{DC} / / \overrightarrow{AB}, E \in \overrightarrow{AB},$ 

$$m (\angle D) = 127^{\circ}, m (\angle CBE) = 53^{\circ}$$

Prove that :  $\overline{AD} // \overline{BC}$ .



[b] On graph paper draw the points A (0,0), B (0,2), C (4,2) and D (4,0). Draw the image formed by rotating the quadrilateral ABCD about the origin through an angle of measure 90°

# 7 Alexandria Governorate

# Central Zone of Education E.G.C.

#### Answer the following questions:

#### 1 Choose the correct answer:

- (1) The sum of the measures of the interior angles of a triangle = the measure of the ...... angle.
  - (a) acute
- (b) right
- (c) obtuse
- (d) straight

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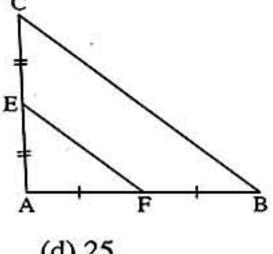
- (2) The rhombus in which its two diagonals are equal in length is called a ......
  - (a) parallelogram.

- (c) rectangle.
- (d) trapezium.

(3) In the opposite figure:

ABC is a triangle in which F and E are the midpoints of AB, AC respectively. If BC = 16 cm., AB = 12 cm. and AC = 10 cm., then the perimeter of  $\triangle$  AFE = ..... cm.

(b) square.



- (a) 24
- (b) 27

- (c) 19
- (d) 25
- (4) The image of the point (-3, 7) by rotation about the origin point with an angle of measure - 90° is .....
  - (a) (-7, -3) (b) (7, -3)
- (c)(7,3)
- (d) (3, -7)
- (5) ABCD is a parallelogram in which m ( $\angle A$ ) = 55°, then m ( $\angle B$ ) = ......
  - (a) 35°
- (b) 125°
- (c) 55°
- (d) 180°

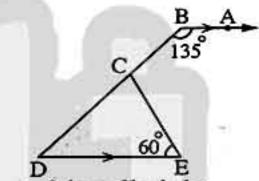
### Complete each of the following:

1 In the opposite figure:

If BA // DE,  $m (\angle DBA) = 135^{\circ}$ 

and m ( $\angle$  CED) = 60°,

then m (∠ DCE) = .....°

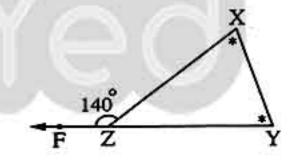


- (2) The rotation about the origin point with an angle of measure ....... is called the neutral rotation.
- 3 The image of the point (4, -2) by reflection in the y-axis is ........
- (4) In the opposite figure:

If  $F \in YZ$ ,  $m(\angle X) = m(\angle Y)$ 

and m ( $\angle XZF$ ) = 140°,

then m ( $\angle X$ ) = .....°



(5) In  $\triangle$  ABC if m ( $\angle$  C) > m ( $\angle$  A) + m ( $\angle$  B), then  $\angle$  C is ...... angle.

### [3] [a] In the opposite figure:

X is the midpoint of AB,

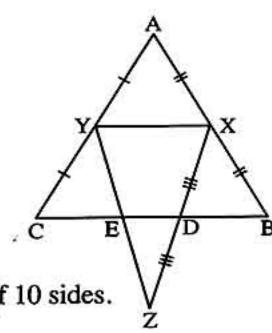
Y is the midpoint of AC

and XD = DZ

#### Prove that:

YE = EZ

[b] Calculate the measure of each interior angle of a regular polygon of 10 sides.





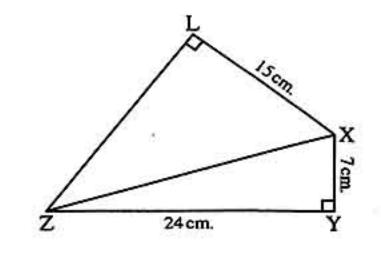
### [4] [a] In the opposite figure:

If m (
$$\angle XYZ$$
) = m ( $\angle XLZ$ ) = 90°,

$$XY = 7 \text{ cm.}$$
,  $YZ = 24 \text{ cm.}$  and  $XL = 15 \text{ cm.}$ 

Find with proof:

The length of XZ and LZ



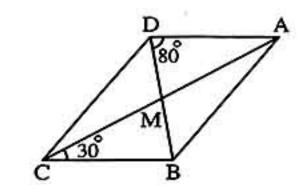
[b] If the point A = (-6, 4) is the image of point A by the translation of LM in the direction of LM where L(2,3) and M(1,5). Find: the point A

### [5] [a] In the opposite figure:

ABCD is a parallelogram,

$$m (\angle BCA) = 30^{\circ}, m (\angle ADB) = 80^{\circ}$$

Find with proof :  $m (\angle CMB)$ 



[b] Triangle ABC whose vertices A (1,5), B (3,1), C (5,3). Draw the triangle and its image by the rotation about the origin point with an angle of measure 180°

# El - Kalyoubia Governorate

#### **Educational Directorate Zone**

Answer the following questions:

#### 1 Choose the correct answer:

- 1) The image of the point (3, -2) by reflection in y-axis is .......
  - (a)(3,2)
- (b) (-3, -2)
- (c)(-3,2)
- (2) The measure of each interior angle of a regular pentagon is ...........°
  - (a) 90
- (b) 120

- (c) 108
- (d) 131
- (3) The measure of any of the exterior angle of an equilateral triangle = ..........°
  - (a) 120
- (b) 60

- (c) 45
- (d) 30
- (4) In  $\triangle$  ABC: if m ( $\angle$  A) > m ( $\angle$  B) + m ( $\angle$  C), then angle A is .......
  - (a) acute.
- (b) right.
- (c) straight.
- (d) obtuse.
- (5) The image of the point (-1,3) by translation (4,-2) is .......
  - (a)(3,1)
- (b) (3,-1)
- (c)(5,1)
- (d) (5, -5)



#### 2 Complete each of the following:

- (1) The rectangle is a parallelogram in which one of its angles is .........
- (2) The line segment joining the midpoints of two sides of a triangle is ........
- (3) The image of the point (3, 2) by rotation with an angle of measure 180° about the origin is .........
- (4) If  $\triangle$  ABC is a right-angled triangle at B, then  $(AC)^2 = \cdots + \cdots$
- (5) If ABCD is a square , then m (∠ ABD) = ······°

#### 3 [a] In the opposite figure: △ ABC in which

AB = 12 cm., BC = 10 cm. and AC = 8 cm.

Find with proof: the perimeter of  $\triangle$  ADE

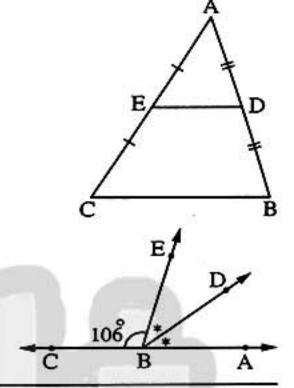
#### [b] In the opposite figure:

$$B \in \overrightarrow{AC}$$
,

 $m (\angle CBE) = 106^{\circ} and$ 

BD bisects ∠ ABE

Find with proof: m (∠ ABD)



[a] Using the lattice, draw Δ ABC where A (1,0), B (0,2) and C (-3,1).

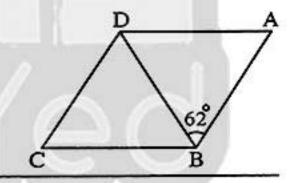
Then draw its image by reflection in Υ axis.

Then draw its image by reflection in X-axis

#### [b] In the opposite figure:

ABCD is a rhombus in which m ( $\angle$  ABD) = 62°

Find with proof:  $m(\angle A)$ 

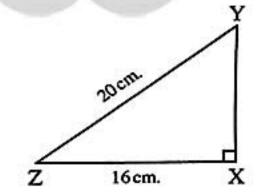


#### 5 [a] In the opposite figure :

XYZ is a triangle in which m ( $\angle X$ ) = 90°,

YZ = 20 cm. and XZ = 16 cm.,

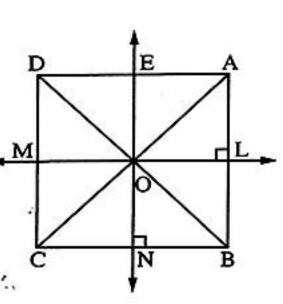
Find with proof: the length of  $\overline{XY}$ 



#### [b] In the opposite figure:

ABCD is a square of side length 6 cm and the origin point its center. Find:

- (1) The image of  $\triangle$  AOE by reflection around point O
- (2) The image of  $\triangle$  AOL by translation 3 cm in direction  $\overrightarrow{AB}$
- 3 The image Δ AOL by rotation about O and with an angle of measure (-90°)



كراسة المعاصر رياضيات (لغات) / ۱ إعدادى / تيرم ۲ (۲: ۱٤)



# El-Sharkia Governorate

#### **Directorate of Education**

#### Mathematics Supervision for E.L.S

Answer the following questions:

### 7 Complete each of the following :

- (1) The sum of measures of the interior angles of a triangle is ...........°,
- (2) If  $\triangle$  ABC is right-angled at B, then  $(AC)^2 = \cdots + \cdots$
- (3) The line segment joining the midpoints of two sides of a triangle is parallel to ........
- (4) Sum of measures of the interior angles of a pentagon = ..........°
- (5) The image of the point (3,5) by the transformation  $(x,y) \longrightarrow (x+1,y-3)$  is ......

#### 2 Choose the correct answer:

- (1) In the opposite figure: XY = ..... BC
  - (a)  $\frac{1}{2}$
- (b) 2

(c)3

- (d)  $\frac{1}{3}$
- (2) The polygon of 6 sides is called ......
  - (a) pentagon.
- (b) hexagon.
- (c) octagon.
- (d) heptagon.

- (3) The rhombus with right angle is called ......
  - (a) square.
- (b) triangle.
- (c) rectangle.
- (d) trapezium.

(4) In the opposite figure : B ∈ AC and

m (
$$\angle$$
 DBF) = 90°, then m ( $\angle$  ABD) = ......

(5) The triangle has at least two ...... angles.

- (a) 180°
- (b) 90°
- (c) 36°

(a) obtuse

(d) 45°

(b) right



- (c) acute
- (d) straight

#### [3] [a] In the opposite figure:

$$\overrightarrow{AB} \cap \overrightarrow{CD} = \{M\}$$
, m ( $\angle AME$ ) = 110°,  $\overrightarrow{MC}$  bisects  $\angle BME$ ,

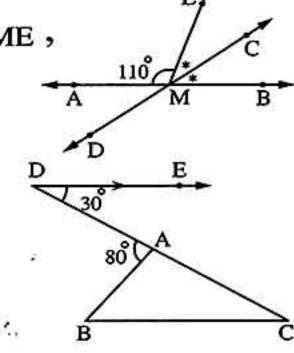
Find with proof:  $m (\angle AMD)$ 

#### [b] In the opposite figure:

$$D \in CA$$
,  $\overline{DE} // BC$ ,

$$m (\angle DAB) = 80^{\circ}$$
  
 $m (\angle D) = 30^{\circ}$ 

Find:  $m (\angle ABC)$ 



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4 [a] Find the measure of each interior angle of regular hexagon.

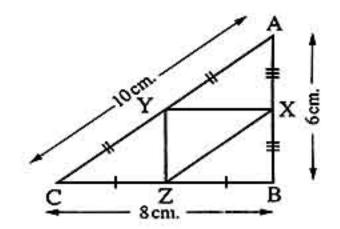
[b] In a coordinates plane. Draw the points A (2, 2), B (5, 2), C (5, 5), then find  $\triangle ABC$  the image of  $\triangle ABC$  by reflection in they y-axis.

#### 5 In the opposite figure :

AB = 6 cm., BC = 8 cm., AC = 10 cm.

X, Y and Z are midpoints of  $\overline{AB}$ ,  $\overline{AC}$  and  $\overline{BC}$ respectively,

**Find:** the perimeter of  $\triangle XYZ$ 



# Suez Governorate

#### **Suez Educational Directorate**

#### Mathematics inspectorate

Answer the following questions:

#### 1 Choose the correct answer:

- (1) In parallelogram if the two adjacent sides are equal in the length, then the shape is ...
  - (a) square.
- (b) rhombus.
- (c) rectangle.
- (d) trapezium.
- (2) The measure of any of exterior angles of an equilateral triangle equals .
  - (a) 60°
- (b) 180°
- (c) 120°
- (d) 90°
- (3) Any triangle has at least two ..... interior angles.
  - (a) acute
- (b) right
- (c) obtuse
- (d) straight
- (4) The measures of each angle of regular hexagon equals ......
  - (a) 60°
- (b) 108°
- (c) 120°
- (d) 135°
- (5) The image of the point (2, -5) by reflection in y-axis is .........
  - (a) (2, -5)
- (b) (2,5)
- (c) (-2, -5) (d) (5, 2)

#### 2 Complete each of the following:

- (1) The length of a line segment joining the midpoints of two sides of a triangle equals .........
- (2) If the image of the point (-1,3) by translation is (1,4), then the image of the point (3, -2) by the same translation is ......
- (3) The sum of the measure of interior angles of a triangle equals ......
- (4) The parallelogram whose diagonals are equal in length and perpendicular is .........
- (5) The image of the point (3, 2) by rotation with an angle of measure 180° about the origin is .....

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# Maths

Final Examinations

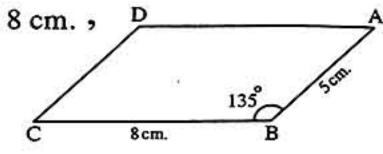
### [3] [a] In the opposite figure:

ABCD is parallelogram in which AB = 5 cm., BC = 8 cm.,

$$m (\angle B) = 135^{\circ}$$

Find:  $\bigcirc$  m ( $\angle$  C)

(2) The perimeter of parallelogram ABCD



[b] Draw  $\triangle$  OBC on a square lattice where O (0,0), B (3,0), C (0,4), then find its image by rotation about the origin point with an angle of measure 180°

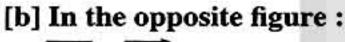
#### [4] [a] In the opposite figure:

D, E and O, are midpoint of

AB, BC and AC respectively AB = 6 cm.,

$$BC = 8 \text{ cm.}$$
  $AC = 10 \text{ cm.}$ 

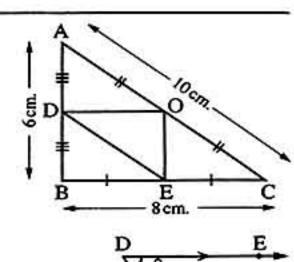
Find the perimeter of :  $\triangle$  DEO

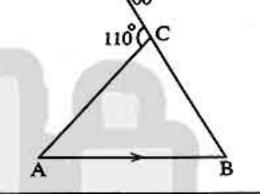


$$m (\angle D) = 60^{\circ}$$

$$m (\angle ACD) = 110^{\circ}$$

Find with proof :  $m (\angle A)$ 



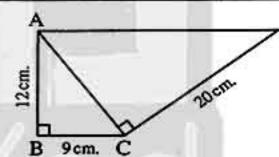


#### [5] [a] In the opposite figure:

$$m (\angle B) = m (\angle ACD) = 90^{\circ}, AB = 12 cm.$$

BC = 9 cm., CD = 20 cm.

Find the length of: AC, AD

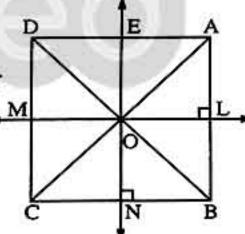


#### [b] In the opposite figure:

ABCD is square of side length 6 cm. and origin point its center

#### Find:

- (1) The image of  $\triangle$  AOL by translation 3 cm. in direction AB
- ② The image of Δ AOL by reflection in EN



# El-Beheira Governorate

**Bandar Kafr El-Dawar Educational** 

**Mathematics inspectorate** 

Answer the following questions:

#### 1 Choose the correct answer:

(1) ABCD is a parallelogram in which m ( $\angle A$ ) = 70°, then m ( $\angle B$ ) = ......

(a) 70°

(b) 110°

(c) 140°

(d) 210°

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# Maths

Final Examinations

- (2) The measure of the interior angle of regular pentagon = ........
  - (a) 108°
- (b) 120°
- (c) 135°
- (d) 540°
- (3) If two adjacent sides are equal in length in a parallelogram, then the figure is a ..........
  - (a) square.
- (b) rhombus.
- (c) rectangle.
- (d) trapezium.
- (4) The sum of the measure of the exterior angles of a triangle = ........
  - (a) 90°
- (b) 180°
- (c) 360°
- (d) 720°

- (5) The triangle contain two ..... angles at least.
  - (a) acute
- (b) obtuse
- (c) right
- (d) reflex

#### 2 Complete each of the following:

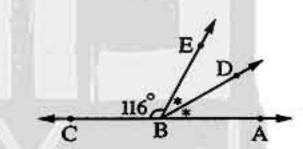
- 1 The line segment joining the midpoints of two sides of a triangle is ...... the third side.
- (2) In  $\triangle$  ABC: If  $(AB)^2 = (BC)^2 + (AC)^2$ , then m  $(\angle \dots) = 90^\circ$
- (3) The image of the point (-3, 2) by reflection in y-axis is ..........
- (4) The image of the point (-3, -4) by the translation (x-4, y+1) is .......
- (5) The image of the point (-4,2) by rotation around the origin point with an anlge of measure 90° is .....

#### 3 [a] In the opposite figure:

$$B \in \overrightarrow{AC}$$
, m ( $\angle$  CBE) = 116°

and BD bisects ∠ ABE

Find:  $m (\angle ABD)$ 



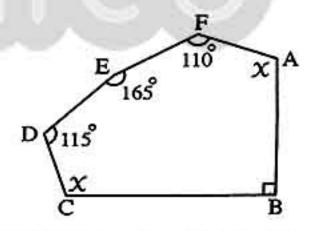
#### [b] In the opposite figure:

ABCDEF is a hexagon, 
$$m (\angle B) = 90^{\circ}$$
,

$$m (\angle F) = 110^{\circ}$$
,  $m (\angle E) = 165^{\circ}$ ,  $m (\angle D) = 115^{\circ}$ ,

$$m (\angle FAB) = m (\angle DCB) = X$$

-Find: the value of  $X^*$ 



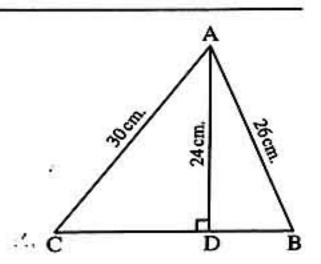
#### 4 [a] In the opposite figure:

ABC is a triangle in which  $\overline{AD} \perp \overline{BC}$ ,

If AD = 24 cm., AB = 26 cm.

, AC = 30 cm.

Find the length of: BC



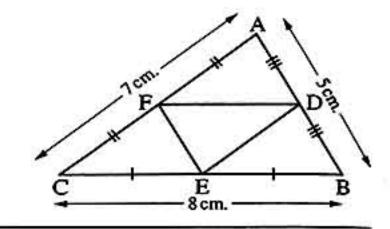
#### [b] In the opposite figure:

AB = 5 cm., BC = 8 cm.,

AC = 7 cm., D, E and F are

the midpoints of AB, BC and CA respectively.

Calculate the perimeter of :  $\Delta$  DEF



- 5 Draw the triangle ABC in which A (1, -1), B (2, 3) and C (0, 4) then find:
  - (1) The image of  $\triangle$  ABC by reflection in the origon point.
  - (2) The image of  $\triangle$  ABC by rotation R (0  $\rightarrow$  90°)

# Beni Suef Governorate Directorate of Experimental Language

#### **Education Administration**

#### Answer the following questions:

#### 1 Choose the correct answer:

- (1) A quadrilateral in which only two opposite sides are parallel is called a .........
  - (a) parallelogram.
- (b) rhombus.
- (c) trapezium.
- (d) square.
- (2) The parallelogram whose diagonals are equal in length and not perpendicular is called .....
  - (a) square.
- (b) rectangle.
- (c) rhombus.
- (d) trapezium.
- (3) The sum of the measures of the interior angles of a triangle is ........
  - (a) 90°

- (b) 180°
- (c) 270°
- (d) 360°
- (4) The image of the point (-4, 5) by translation (2, -3) is ......
  - (a) (-6, -8)
- (b) (-2, 2)
- (c) (-2, -2)
- (d) (2, -2)
- (5) The image of the point (5, -3) by rotation about the origin point with an angle of measure 90° is .....
  - (a) (-5, -3)
- (b) (5,3)
- (c)(3,5)
- (d)(-3,5)

## 2 Complete each of the following:

- (1) A square is a ..... with a right angle.
- (2) The line segment joining the midpoints of two sides of a triangle is .........
- (3) The ray drawn from the midpoint of a side of a triangle parallel to another side .........
- (4) The image of the point (4,6) by geometric transformation  $(x,y) \longrightarrow (-x,y-7)$ is ......
- (5) The measure of the exterior angle of the equilateral triangle at any one of its vertices equals .....°

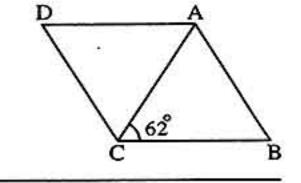
3 [a] Calculate the sum of the measures of the interior angles of a hexagon.

#### [b] In the opposite figure:

ABCD is a rhombus in which,

$$m (\angle ACB) = 62^{\circ}$$
,

Find with proof :  $m (\angle B)$ 

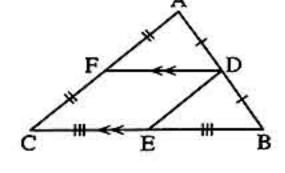


#### 4 [a] In the opposite figure:

ABC is a triangle in which,

D, E and F are the midpoints of AB, BC and AC respectively. BC = 12 cm., AC = 10 cm.

Find the perimeter of the quadrilateral DECF

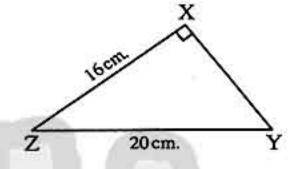


#### [b] In the opposite figure:

XYZ is a triangle in which,

$$m (\angle X) = 90^{\circ}, YZ = 20 \text{ cm.}, XZ = 16 \text{ cm.}$$

Find the length of XY



- 5 On a square lattice, draw Δ XYZ where: X (2, 4), Y (4, 2) and Z (1, 1), then draw:
  - (1) The image of the  $\triangle$  XYZ by reflection in the X-axis.
  - (2) The image of the  $\triangle$  XYZ by rotation about the origin point with an angle of measure 180°

# El - Menia Governorate

#### El-Menia Educational Directorate

Answer the following questions:

#### 1 Choose the correct answer:

- (1) The measure of each interior angle of the regular hexagon = .........
  - ~(a) 108°
- (b) 120°
- (c) 136°
- (d) 114°
- (2) ABCD is a parallelogram in which m ( $\angle A$ ) = 60°, then angle m ( $\angle C$ ) = ......
  - (a) 60°

- (b) 180°
- (c) 120°
- (d) 90°
- (3) The image of the point (3, -5) by reflection in the y-axis is .......
  - (a)(3,5)
- (b) (-3, -5)
- (c)(-3,5)
- (d) (-5,3)
- (4) In  $\triangle$  ABC, m ( $\angle$  A) = m ( $\angle$  B) + m ( $\angle$  C), then m ( $\angle$  A) = .......
  - (a) 30°

(b) 90°

(c) 60°

(d) 150°

- (5) The image of the point (3, 2) by rotation about the origin point with an angle of 180° is .....
  - (a) (-3, -2)
- (b) (-2,3)
- (c) (2, -3)
- (d)(3,2)

### 2 Complete each of the following:

- (1) The parallelogram whose diagonals are perpendicular and not equal in length is a .........
- (2) The image of the point (5,3) by translation  $(x,y) \longrightarrow (x+3,y-1)$  is ......
- (3) The measure of the exterior angle of equilateral triangle is .........
- (4) The sum of measures of the interior angles of a triangle = ..........°
- (5) The ray drawn from the midpoint of a side of a triangle parallel to another side ........
- [3] [a] In the opposite figure :

DE // BC,  $m (\angle D) = 60^{\circ}$ ,

 $m (\angle DAC) = 100^{\circ}$ 

Find:  $m (\angle C)$ 

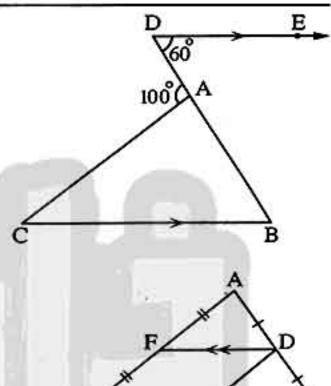


ABC, D, E and F are the midpoints of

AB, BC and CA respectively, BC = 12 cm.

, AC = 10 cm.,

Find: the perimeter of the quadrilateral DECF

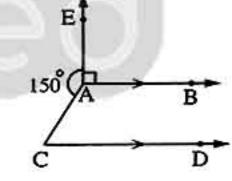


[4] [a] In the opposite figure:

AB // CD,  $m (\angle EAC) = 150^{\circ}$ 

 $\overrightarrow{AE} \perp \overrightarrow{AB}$ 

Find:  $m (\angle BAC) \cdot m (\angle C)$ 



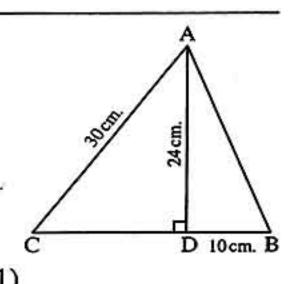
- [b] On a square lattic. Draw  $\triangle$  ABC where A(1,1), B(4,1), C(4,4)
- then draw its image by reflection in X-axis.
- 5 [a] In the opposite figure:

 $\triangle$  ABC,  $\overrightarrow{AD} \perp \overrightarrow{BC}$ ,  $\overrightarrow{AD} = 24$  cm.

, BD = 10 cm. , AC = 30 cm.

Find: the length of BC and the area of  $\triangle$  ABC

[b] On a square lattice. Draw  $\overline{AB}$  where A (4,3), B (-1,1), then draw its image by translation  $(x, y) \longrightarrow (x + 2, y - 1)$ 



# 14. Aswan Governorate

#### **Aswan Educational Directorate**

Answer the following questions:

#### 1 Choose the correct answer:

- (1) The measure of each interior angle of a regular pentagon = ........
  - (a) 90°

- (b) 120°
- (c) 108°
- (d) 135°

(2) In the opposite figure:

If 
$$BC = 10 \text{ cm.}$$
,

then  $DE = \cdots cm$ .

(a) 5

(b) 10

(c) 20

- (d) 40
- (3) The image of the point (3,0) by reflection in origin point is .........
  - (a) (-3,0)
- (b) (0,3)
- (c) (0, -3)
- (d)(3,0)

10cm.

- (4) ABCD is a parallelogram in which m ( $\angle$  A) + m ( $\angle$  C) = 110° then m ( $\angle$  B) = ......°
  - (a) 77

(b) 55

- (c) 180
- (d) 125
- (5) The sum of the measures of interior angles of a triangle = .........°
  - (a) 360

(b) 180

- (c) 120
- (d) 60

#### 2 Complete each of the following:

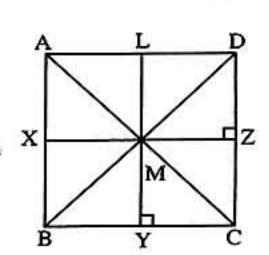
- 1) The image of the point (-1,2) by translation (1,3) is ........
- ② If ABCD is a square, then m (∠ BAC) = ······°
- (4) The sum of the measure of the accumulative angles at a point = .........°
- (5) The measure of the exterior angle of the equilateral triangle = .........°

#### [a] In the opposite figure :

ABCD is a square, where M is the intersection of its diagonals X, Y, Z, L are midpoints of its sides.

Find: 1 The image of the point A by reflecting in LY

(2) The image of  $\triangle$  ALM by reflection in XZ



كراسة المعاصر رياضيات (لغات) / ١ إعدادي / تيرم ٢ (٢: ١٥)

#### [b] In the opposite figure:

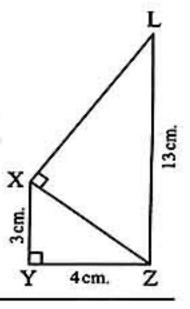
XYZL is quadrilateral

where m (
$$\angle XYZ$$
) = m ( $\angle LXZ$ ) = 90°

$$XY = 3 \text{ cm.}$$
,  $YZ = 4 \text{ cm.}$ 

$$LZ = 13$$
 cm.

Find: the length of each XZ, XL



#### [4] [a] If the ratio between the measure of angles of a quadrilateral is 2:3:3:4, then find the measure of the smallest angle.

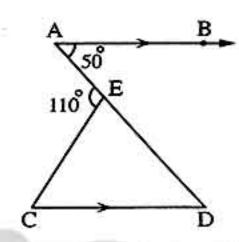
#### [b] In the opposite figure:

$$\overrightarrow{AB} // \overrightarrow{CD}, m (\angle A) = 50^{\circ},$$

$$m (\angle AEC) = 110^{\circ}$$

Find with proof: the measures of

interior angles in the  $\Delta$  EDC



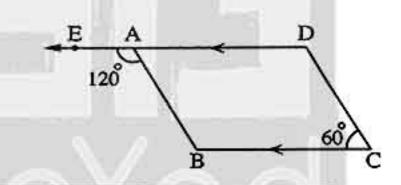
[a] Using the lattice. draw Δ ABC where: A (2,3), B (4,2), C (1,2), then draw its image by rotation about the origin point with an angle of measure 180°

#### [b] In the opposite figure:

$$E \in DA$$
,  $m (\angle EAB) = 120^{\circ}$ 

, m (
$$\angle$$
 C) = 60°,  $\overrightarrow{DA}$  //  $\overrightarrow{CB}$ 

Prove that: ABCD is a parallelogram.



# Southern Sinai Governorate

#### Directorate of Education

#### Tur Sinai Educational Idara

#### Answer the following questions:

# 1 Choose the correct answer:

- (1) The sum of the measures of the accumulative angles at a point is equal to .........°
  - (a) 360

- (b) 270
- (c) 180
- (d) 90
- (2) The measure of each angle of a regular pentagon = ..........°
  - (a) 90

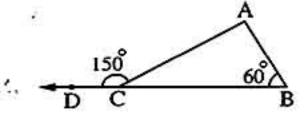
- (b) 108
- (c) 120
- (d) 180

- (3) In the opposite figure:  $m (\angle A) = \dots \circ$ 
  - (a) 30

(b) 60

(c) 90

(d) 150



- (4) Any triangle has two ..... angles at least.
  - (a) straight
- (b) obtuse
- (c) right
- (d) acute
- (5) The image of the point (4, -2) by translation (-3, 3) ......
  - (a) (1, -5)
- (b) (7,1)
- (c) (7, -5) (d) (1, 1)

## Complete each of the following :

- (1) The rectangle is ..... but its angles are right angles.
- (2) The line segment joining between the two midpoints of two sides of a triangle ..... the third side.
- (3) The image of the point (3, 2) by reflection in an origin is ..........
- (4) In the right-angled triangle the area of the square on ..... equals the sum of areas of the squares on the other two sides.
- (5) If the image of the point (-2,0) by rotation at origin is (0,-2), then the measure of the angle of rotation = ......
- [3] [a] If the measure of the angle of a regular polygon is 135°,

Find: the number of sides of this polygon.

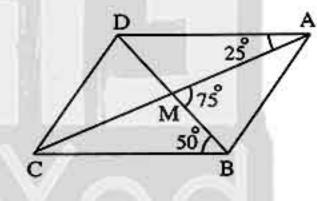
#### [b] In the opposite figure:

$$\overline{AB} / \overline{DC}, \overline{AC} \cap \overline{BD} = \{M\},$$

$$m (\angle DBC) = 50^{\circ}, m (\angle DAC) = 25^{\circ},$$

$$m (\angle AMB) = 75^{\circ}$$

Prove that: ABCD is a parallelogram.

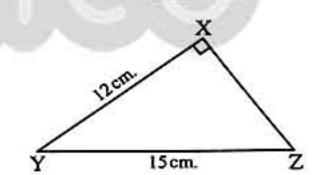


#### 4 [a] In the opposite figure:

XYZ is a triangle such that

$$m (\angle X) = 90^{\circ} , XY = 12 cm. , YZ = 15 cm.$$

Find: the length of XZ



#### [b] In the opposite figure:

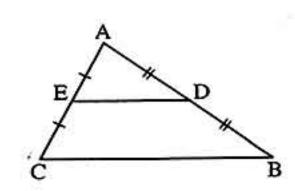
ABC is a triangle such that

D is the midpoint of AB,

E is the midpoint of AC,

AB = 12 cm., AC = 8 cm., BC = 10 cm.

**Find:** the perimeter of  $\triangle$  ADE



...

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#### 5 In the opposite figure:

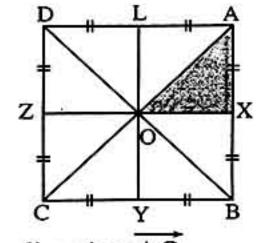
ABCD is a square  $\overline{AC} \cap \overline{BD} = \{O\}$ 

X,Y,Z and L are midpoints of

 $\overline{AB}$ ,  $\overline{BC}$ ,  $\overline{CD}$ ,  $\overline{DA}$  respectively.

**Find**: 1 The image of  $\triangle$  AXO by reflection in  $\overrightarrow{AO}$ 

- (2) The image of  $\triangle$  AXO by translation of magnitude AO in direction  $\overrightarrow{AO}$
- (3) The image of  $\triangle$  AXO by rotation R (0, 180°)





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## Answers of school book models in geometry

## Model

- 1 (1) (b)
- (2) (a)
- (3)(d)
- (4)(b)
- (5) (b)

- (1)(2,-1)
- (2)(-2,1)
- (3) its two diagonals are perpendicular
- (4) 120°
- (5)(8,2)

- [a] : m ( $\angle$  A) = m ( $\angle$  B) = 25°
  - → ∠ ACD is an exterior angle of △ ABC
  - $m (\angle ACD) = 25^{\circ} + 25^{\circ} = 50^{\circ}$
- (The req.)
- [b] : D is the midpoint AB
- $\therefore AD = \frac{1}{2}AB$
- $\therefore AD = \frac{1}{2} \times 12 = 6 \text{ cm}.$ , ∵ E is the midpoint AC
- $\therefore AE = \frac{1}{2}AC$
- $\therefore AE = \frac{1}{2} \times 8 = 4 \text{ cm}.$
- . . D is the midpoint AB . E is the midpoint AC (3)
- : ED =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 10 = 5 cm.
- :. From (1) , (2) , (3):

The perimeter of  $\triangle$  ADE = 6 + 4 + 5 = 15 cm.

(The req.)

- [a] : DE // YZ , ZD is a transversal
  - $\therefore$  m ( $\angle$  Z) = m ( $\angle$  D) = 50° (alternate angles)
  - In A XYZ:
  - $m (\angle Z) + m (\angle ZXY) + m (\angle Y) = 180^{\circ}$
  - $m (\angle Y) = 180^{\circ} (105^{\circ} + 50^{\circ}) = 25^{\circ}$
  - $, : X \in \overline{DZ}$
  - $m (\angle YXD) = 180^{\circ} 105^{\circ} = 75^{\circ}$ (The req.)
- $[b] : \overline{AZ} // \overline{YD} // \overline{XE} // \overline{CB}$ 
  - AY = YX = XC
  - $\therefore$  AD = DE = EB
- ∴ EB =  $\frac{18}{3}$  = 6 cm.

- In  $\triangle$  ABD:  $\because$  m ( $\angle$  ADB) = 90°
- $(BD)^2 = (AB)^2 (AD)^2 = 676 576 = 100$
- ∴ BD =  $\sqrt{100}$  = 10 cm.

- In  $\triangle$  ADC:  $\therefore$  m ( $\angle$  ADC) = 90°
- $(CD)^2 = (AC)^2 (AD)^2 = 900 576 = 324$
- :. CD =  $\sqrt{324}$  = 18 cm.
- ∴ BC = 10 + 18 = 28 cm.
- ... The area of  $\triangle ABC = \frac{1}{2} BC \times AD$ 
  - $=\frac{1}{2} \times 28 \times 24 = 336$  cm<sup>2</sup>

## (The req.)

## Model

(1) (b)

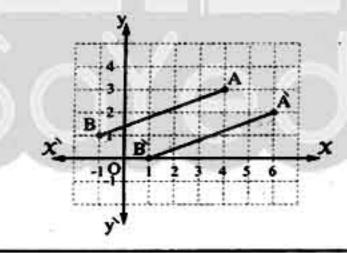
- (2)(c)
- (3) (b)
- (4)(c)
- (5) (c)

### 2

- (1) 360°
- (2) (5,5)
- (a) 120°
- (4) bisects the third side.
- (5) ZYC

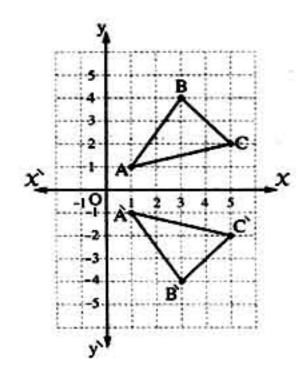
- [a]  $\ln \Delta XYZ : m (\angle Y) = 90^{\circ}$ 
  - $(XZ)^2 = (XY)^2 + (YZ)^2 = 49 + 576 = 625$
  - $XZ = \sqrt{625} = 25 \text{ cm}.$
  - In  $\Delta$  LXZ: m ( $\angle$  L) = 90°
  - $\therefore (LZ)^2 = (XZ)^2 (LX)^2 = 625 225 = 400$
  - :. LZ =  $\sqrt{400}$  = 20 cm.
- (The req.)

[b]



#### 4

[a]



**[b]** In  $\triangle$  ABC: m ( $\angle$  ACB) = 180° - (90° + 30°) = 60°

$$\cdot : BD \cap AO = \{C\}$$

$$\therefore m (\angle ACB) = m (\angle OCD) = 60^{\circ} \qquad (V.O.A)$$

$$\therefore$$
 m ( $\angle$  E) = 360° - (60° + 120° + 90°) = 90°

5

[a] : EO // CD , EB is a transversal

$$\therefore$$
 m ( $\angle$  CBA) = m ( $\angle$  E) = 50° (alternate angles)

From AABC:

$$m (\angle BAC) = 180^{\circ} - (50^{\circ} + 30^{\circ}) = 100^{\circ}$$

: 
$$m (\angle ABD) = 30^{\circ} + 100^{\circ} = 130^{\circ}$$
 (The req.)

[b] 
$$\therefore \overrightarrow{AD} // \overrightarrow{XY} // \overrightarrow{BC} \rightarrow \therefore AX = XB$$

$$\therefore$$
 CZ = ZE

(Q.E.D.)

Model

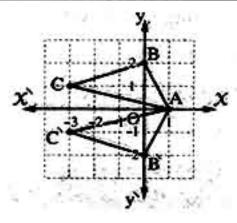
5

(1) two adjacent sides are equal in length

- (2) equal in measure
- (3) y-axis
- (4) parallel to the third side
- (5)(-4,-1)

3

[a]



[b] : ABCD is a parallelogram , M is the intersection point of its diagonals.

.. M is the midpoint of AC

In △ ABC : .: M is the midpoint of AC , ME // BC

.. E is the midpoint of AB

$$\therefore AE = EB$$

(Q.E.D.)

4

[a] : OH // BC , OB is a transversal to them

$$\therefore$$
 m ( $\angle$  B) + m ( $\angle$ O) = 180°

(two interior angles in the same side of the transversal)

$$m (\angle B) = 180^{\circ} - 135^{\circ} = 45^{\circ}$$

$$\therefore m (\angle C) + m (\angle D) = 180^{\circ}$$

(two interior angles in the same side of the transversal)

$$\therefore$$
 m ( $\angle$  C) = 180° - 120° = 60°

∴ In ∆ ABC:

$$m (\angle BAC) = 180^{\circ} - (45^{\circ} + 60^{\circ}) = 75^{\circ} (The req.)$$

[b] In  $\triangle$  ABC: m ( $\angle$  B) = 90°

$$\therefore (AC)^2 = (AB)^2 + (BC)^2 = 144 + 81 = 225$$

∴ AC = 
$$\sqrt{225}$$
 = 15 cm.

In 
$$\triangle$$
 ACD: m ( $\angle$  ACD) = 90°

$$\therefore$$
 (AD)<sup>2</sup> = (AC)<sup>2</sup> + (DC)<sup>2</sup> = 225 + 400 = 625

∴ AD = 
$$\sqrt{625}$$
 = 25 cm.

(The req.)

5

(1) A LNB

(2) A DOM

(3) **A BON** 

Model 4

1

(1) (a)

(5) (p)

(3) (a)

(4) (b)

(5) (a)

ä

2

(1) parallel to the third side

(2) equal in measure

(3) each two opposite sides are parallel (there are another solution).

$$(4)(2,-3)$$

$$(5)(-3,-2)$$

3

In  $\triangle$  CEO: m ( $\angle$  COE) = 180° - (35° + 50°) = 95°

$$, \because \overrightarrow{DC} \cap \overrightarrow{BE} = \{0\}$$

$$\therefore$$
 m ( $\angle$  DOB) = m ( $\angle$  COE) = 95° (V.O.A) (First req.)

From the quadrilateral ABOD

$$m (\angle B) = 360^{\circ} - (95^{\circ} + 100^{\circ} + 85^{\circ}) = 80^{\circ}$$

(Second req.)

4

[a] : The length =  $\frac{48}{6}$  = 8 cm.

 $\therefore$  The length of the diagonal =  $\sqrt{8^2 + 6^2} = 10$  cm.

- [b] : AB // DE , BD is a transversal
  - $\therefore$  m ( $\angle$  B) = m ( $\angle$  D) = 60° (alternate angles)
  - → ∴ ∠ AOD is an exterior angle of Δ ABO
  - $\therefore m (\angle AOD) = m (\angle B) + m (\angle A)$
  - $m (\angle A) = 110^{\circ} 60^{\circ} = 50^{\circ}$

(The req.)

- [a] The point A = (1, 2)
  - .. The image of the point A (1 , 2) by translation (-1,2) is (0,4)
- [b] In  $\triangle$  ABC:  $\therefore$   $\overrightarrow{DE}$  //  $\overrightarrow{BC}$  > D is the midpoint of  $\overrightarrow{AB}$ 
  - .. E is the midpoint of AC
- $\therefore$  DE =  $\frac{1}{2}$  BC
- . . O is the midpoint of BC
- $\therefore BO = \frac{1}{2} BC$
- .: DE = BO
- · · · DE // BC
- .. DBOE is a parallelogram

(First req.)

- : ED =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 12 = 6 cm.
- . .. D is the midpoint of AB . O is the midpoint of BC
- ∴ DO =  $\frac{1}{2}$  AC =  $\frac{1}{2}$  × 8 = 4 cm.
- . E is the midpoint of AC , O is the midpoint of BC
- $EO = \frac{1}{2} AB = \frac{1}{2} \times 10 = 5 \text{ cm}.$
- $\therefore$  The perimeter of  $\triangle$  EDO = 6 + 4 + 5 = 15 cm.

(Second req.)

# Model

1

- (1) (b)
- (b) (s)
- (3) (a)
- (d)
- (5) (c)

- (1) The rhombus
- (2) right-angled

- (3) acute
- (4) (2,4)
- (5) (2,4)

- [a] Theoretical
- [b] : D is the midpoint of AB , O is the midpoint of AC
  - $\therefore$  DO =  $\frac{1}{2}$  BC
- .: DO = 4 cm.
- . . O is the midpoint of AC . E is the midpoint of BC
- $\therefore$  OE =  $\frac{1}{2}$  AB
- $\therefore$  OE = 3 cm.
- . .: E is the midpoint of BC . D is the midpoint of AB
- $\therefore$  ED =  $\frac{1}{2}$  AC
- $\therefore$  ED = 5 cm.
- $\therefore$  The perimeter of  $\triangle$  DEO = 4 + 3 + 5 = 12 cm.
  - (The req.)

- [a] : ABCD is a parallelogram . M is the intersection point of its diagonals.
  - .. M is the midpoint of AC
  - In A ABC : MO // AB
  - , M is the midpoint of AC
  - .. O is the midpoint of BC
  - ∴ BO = OC

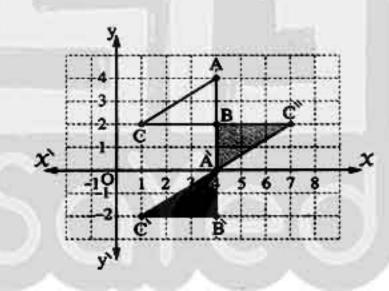
- (Q.E.D.)
- [b] In  $\triangle$  XYZ:  $\cdots$  m ( $\angle$  X) = 90°
  - $(XY)^2 = (YZ)^2 (XZ)^2 = 400 256 = 144$
  - ∴ XY =  $\sqrt{144}$  = 12 cm.
- (The req.)

- $[a] : B \in \overline{AE}$ 
  - $\therefore$  m ( $\angle$  ABC) = 180° 130° = 50°
  - :. From the quadrilateral ABCD :
  - $m (\angle C) = 360^{\circ} (50^{\circ} + 80^{\circ} + 120^{\circ})$

 $= 360^{\circ} - 250^{\circ} = 110^{\circ}$ 

(The req.)

[b]



- (1)  $\triangle ABC$  is the image of  $\triangle ABC$  by translation 2 AB in direction AB
- (2)  $\triangle ABC$  is the image of  $\triangle ABC$  by rotation about B with an angle of measure 180°

# Model

1

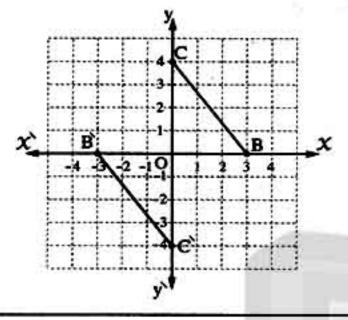
- ① (b)
- (c)
- (3) (a)
- (4) (a)
- (5) (b)

- 2
- (1) equal to the sum of the measures of its non adjacent interior angles
- (2) square
- (3) 130°
- (4) (-2,2)

- [a] : ED // CB , BE is a transversal
  - $\therefore$  m ( $\angle$  B) = m ( $\angle$  E) = 40° (alternate angles)
  - :. In  $\triangle$  ABC: m ( $\angle$  BAC) = 180° (50° + 40°) = 90°
  - ∴ AC ⊥ BE

(Q.E.D.)

[b]



4

In  $\triangle$  ABC: m ( $\angle$  ACB) = 180° - (90° + 40°) = 50°

- $, :: BD \cap AO = \{C\}$
- $\therefore$  m ( $\angle$  DCO) = m ( $\angle$  ACB) = 50°
- (V.O.A.)
- : AB // DE , BD is a transversal
- $\therefore$  m ( $\angle$  B) = m ( $\angle$  D) = 90° (alternate angles)

From the quadrilateral CDEO

 $\therefore$  m ( $\angle$  E) = 360° - (90° + 50° + 130°) = 90° (The req.)

5

- [a] In A XYZ:
  - .. D is the midpoint of XY , E is the midpoint of XZ
  - ∴ DE =  $\frac{1}{2}$  ZY =  $\frac{1}{2}$  × 12 = 6 cm.
  - E is the midpoint of X Z O is the midpoint of ZY
  - $\therefore EO = \frac{1}{2} \times XY = \frac{1}{2} \times 6 = 3 \text{ cm}.$
  - $\bullet$  O is the midpoint of  $\overline{ZY}$   $\bullet$  D is the midpoint of  $\overline{XY}$
  - $\therefore OD = \frac{1}{2} \times XZ = \frac{1}{2} \times 8 = 4 \text{ cm}.$
  - $\therefore$  The perimeter of  $\triangle$  DOE = 6 + 3 + 4 = 13 cm.

(The req.)

16cm.

[b] Construction : Draw DE ⊥ BC

Proof: ABED is a rectangle

- ∴ DE = AB = 12 cm.
- AD = BE = 16 cm.
- $\therefore$  EC = 25 16 = 9 cm.
- → ∵ m (∠ DEC) = 90°
- $\therefore$  (DC)<sup>2</sup> = (DE)<sup>2</sup> + (EC)<sup>2</sup> = 144 + 81 = 225
- :. DC =  $\sqrt{225}$  = 15 cm.

(The req.)

Model

- (1) (b)
- (2) (a)
- (3)(c)
- (4) (a)
- (5) (b)

2

- (1) 540° (2) 120° (3) right (4) (-2,2) (5) 90°

- [a] : DE // BC , AB is a transversal
  - $\therefore$  m ( $\angle$  B) = m ( $\angle$  EAB) = 120° (alternate angles)
  - :  $m (\angle B) + m (\angle C) = 120^{\circ} + 60^{\circ} = 180^{\circ}$ and they are interior angles on the same side of
  - :. AB // CD

the transversal

- , : DA // CB
- .: ABCD is a parallelogram
- (Q.E.D.)

- [b] In  $\triangle$  ABC:
  - .. D is the midpoint of AB , E is the midpoint of AC
  - $\therefore$  ED =  $\frac{1}{2}$  BC
- ∴ BC = 2 ED
- $\therefore$  BC = 2 × 5 = 10 cm.

(The req.)

- [a] : The sum of measures of the interior angles of the pentagon =  $(5-2) \times 180^\circ = 540^\circ$ 
  - $\therefore$  m ( $\angle$  D) = 540° (110° + 70° + 120° + 150°)
    - = 90°

(The req.)

- [b] In  $\triangle$  ABC : :: m ( $\angle$  B) = 90°
  - $(AB)^2 = (AC)^2 (BC)^2 = 400 144 = 256$
  - :. AB = 16 cm.
  - ∴ AD = AB DB = 16 9 = 7 cm.
  - $\cdot : AE = 2BC$
- $AE = 2 \times 12 = 24$
- , : AE // BC , AB is a transversal
- $\therefore$  m ( $\angle$  A) = m ( $\angle$  B) = 90° (alternate angles)
- $(ED)^2 = (AD)^2 + (AE)^2 = 49 + 576 = 625$
- :. ED =  $\sqrt{625}$  = 25

(The req.)

5

- [a] : ABCD is a parallelogram
  - $\therefore m (\angle B) + m (\angle C) = 180^{\circ}$
  - $m (\angle C) = 180^{\circ} 135^{\circ} = 45^{\circ}$

(First req.)

- . . ABCD is a parallelogram
- $\therefore$  AB = CD = 5 cm.  $\Rightarrow$  AD = BC = 8 cm.

.. The perimeter of parallelogram ABCD

= 5 + 8 + 5 + 8 = 26 cm. (Second req.)

[b] (1) ∆ ADC

(2)  $\Delta$  MBC

## Model

- (1) (a)
- (5)(c)
- (3)(c)
- (4)(b)
- (5) (d)

- (1) half the length of the third side.
- (2) square

- (3) 5 cm.
- (4)(3,-4),(-3,4) (5)(5,-1)

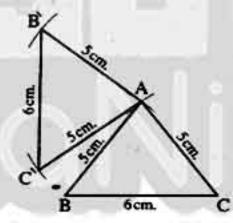
- [a] : DA // BE , BD is a transversal
  - $\therefore$  m ( $\angle$  CBD) = m ( $\angle$  ADB) = 50° (alternate angles)
  - $m (\angle DBE) = 180^{\circ} 50^{\circ} = 130^{\circ}$
  - , : BA bisects ∠ DBE
  - ∴ m ( $\angle$  ABE) =  $\frac{130^{\circ}}{2}$  = 65°
  - $\rightarrow$  :: m ( $\angle$  C) = m ( $\angle$  ABE) = 65°

and they are corresponding angles

- : AB // CD
- , : AD // BC
- .. ABCD is a parallelogram.

(Q.E.D.)

[b]



- [a] : DE // CB , BD is a transversal
  - $\therefore$  m ( $\angle$  B) = m ( $\angle$  D) = 50° (alternate angles)

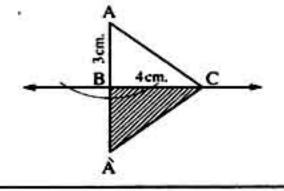
(First req.)

From  $\triangle$  ABC:

$$m (\angle BAC) = 180^{\circ} - (35^{\circ} + 50^{\circ}) = 95^{\circ}$$

(Second req.)

[b]



- [a] : ABCD is a parallelogram
  - : AB // DC
- :. XC // AB

In △ ABE : .: C is the midpoint of BE

- ,XC // AB
- .. X is the midpoint of AE
- :. AX = XE

(Q.E.D.)

- [b] In  $\triangle$  BCD:  $\therefore$  m ( $\angle$  B) = 90°
  - $(BD)^2 = (DC)^2 (BC)^2 = 169 144 = 25$
  - ∴ BD =  $\sqrt{25}$  = 5 cm.
  - AB = 5 + 11 = 16 cm.
  - In  $\triangle$  ABC:  $\cdots$  m ( $\angle$  B) = 90°
  - $(AC)^2 = (AB)^2 + (BC)^2 = 256 + 144 = 400$
  - :. AC =  $\sqrt{400}$  = 20 cm.

(The req.)

## **Answers of school examinations** in Geometry

# Cairo

- (1) (b)
- (5)(q)
- (3)(c)
- (4) (a)
- (5) (a)

- (1) half the length of the third side
- (2) equal in measure
- (3) The rectangle
- (4) 180°
- (5)(0,5)

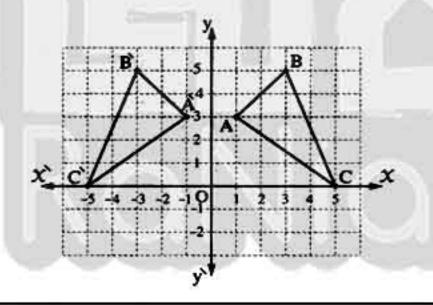
- [a] : ABCDE is a pentagon
  - .. The sum of measures of its interior angles  $= (5-2) \times 180^{\circ} = 540^{\circ}$

$$\therefore$$
 m ( $\angle$  E) = 540° - (140° + 130° + 90° + 110°)

= 70°

(The req.)

[b]



- [a]  $:: \angle DAB$  is an exterior angle of  $\triangle ABC$ 
  - $m (\angle C) = 120^{\circ} 50^{\circ} = 70^{\circ}$
  - , .: DE // CB , CD is a transversal
  - $\therefore$  m ( $\angle$  C) + m ( $\angle$  D) = 180°

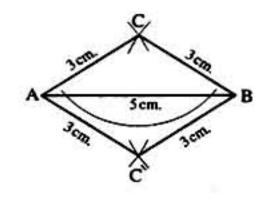
(interior angles in the same side of the transversal)

- $\therefore$  m ( $\angle$  D) = 180° 70° = 110°
- (The req.)
- [b] : m ( $\angle$  ABC) + m ( $\angle$  CBD) + m ( $\angle$  DBE)
  - + m ( $\angle$  EBA) = 360° (acumulative angles at B)
  - $\therefore$  m ( $\angle$  DBE) = 360° (110° + 35° + 140°) = 75°

(The req.)

### 5

[a]



#### [b] In Δ ABC :

- .. D is the midpoint of AB , E is the midpoint of AC
- $\therefore$  ED =  $\frac{1}{2}$  BC
- ∴ BC = 12 cm.
- . .. D is the midpoint of AB . F is the midpoint of BC
- $\therefore DF = \frac{1}{2}AC$
- :. AC = 8 cm.
- . : E is the midpoint of AC . F is the midpoint of BC
- $\therefore EF = \frac{1}{2}AB$
- $\therefore$  AB = 6 cm.
- ∴ The perimeter of ∆ ABC
  - = 6 + 12 + 8 = 26 cm.

(The req.)

### Additional question

- 1 (1) (3,-5)
  - (2) the lengths of line segments.
    - , the measures of angles.
    - , the parallelism , betweeness
  - (3) two
- In  $\triangle$  ABD: : m ( $\angle$  ADB) = 90°
  - $\therefore (DB)^2 = (AB)^2 (AD)^2 = 676 576 = 100$
  - :. DB =  $\sqrt{100}$  = 10 cm.
  - In  $\triangle$  ACD:  $m (\angle ADC) = 90^{\circ}$
  - $\therefore$  (CD)<sup>2</sup> = (AC)<sup>2</sup> (AD)<sup>2</sup> = 900 576 = 324
  - $\therefore$  CD =  $\sqrt{324}$  = 18 cm.
  - $\therefore$  BC = 10 + 18 = 28

(First req.)

- $\therefore$  The area of  $\triangle$  ABC =  $\frac{1}{2} \times 28 \times 24$ 
  - = 336 cm. (Second req.)

## Cairo

- 1 (1) (d)
- (2) (a)
- (3) (b)
- (4) (d) (5) (c)
- 2 (1) (5,3) (2) perpendicular, bisect each other
  - (3) bisects the third side
- (4) trapezium

(5) (0,2)

ا المادي / ديم / المادي ا المادي / 13 مادي / 1

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى في المعلقة

[a] LM // YZ , LY is a transversal

$$\therefore m (\angle L) + m (\angle Y) = 180^{\circ}$$

(interior angles in the same side of the transversal)

$$\therefore$$
 m ( $\angle$  Y) = 180° - 100° = 80°

$$\rightarrow : \overline{XN} / \overline{YZ} \rightarrow \overline{XZ}$$
 is a transversal

$$\therefore$$
 m ( $\angle$  Z) = m ( $\angle$  ZXN) = 40° (alternate angles)

: In 
$$\triangle$$
 XZY: m ( $\angle$  YXZ) = 180° - (80° + 40°) = 60°

(The req.)

[b] : LZ // YX , LX is a transversal

$$\therefore$$
 m ( $\angle$  L) = m ( $\angle$  MXL) = 47° (alternate angles)

$$m (\angle L) + m (\angle Z) = 47^{\circ} + 133^{\circ} = 180^{\circ}$$

and they are interior angles in the same side of the transversal

[a] ∴ ∆ ABC is an equilateral triangle

∴ m (
$$\angle$$
 ACB) =  $\frac{180^{\circ}}{3}$  = 60°

$$\cdots \overline{AF} \cap \overline{BD} = \{C\}$$

$$\therefore m (\angle DCF) = m (\angle ACB) = 60^{\circ} (V.O.A.)$$

.. From the quadrilateral CDEF:

$$m (\angle F) = 360^{\circ} - (60^{\circ} + 120^{\circ} + 110^{\circ}) = 70^{\circ}$$

(The req.)

[b] In ∆ EDF :

: A is the midpoint of ED , B is the midpoint of EF

$$\therefore AB = \frac{1}{2}DF = DC = 8 \text{ cm}.$$

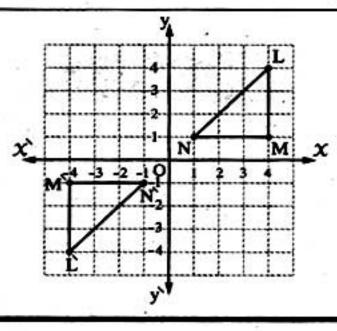
, ... B is the midpoint of EF, C is the midpoint of DF

$$\therefore BC = \frac{1}{2} DE = DA = 6 cm.$$

.. The perimeter of the quadrilateral ABCD

$$= 8 + 6 + 8 + 6 = 28$$
 cm.

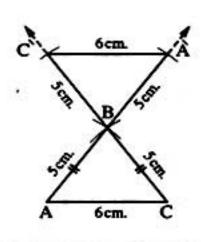
(The req.)



### Additional question

1 (1) the sum of the squares of the lengths of the other two sides.

**2**4



## Giza

1 (d)

(2) (c)

(3) (d)

(5) (b) (4) (c)

2 (1) 116°

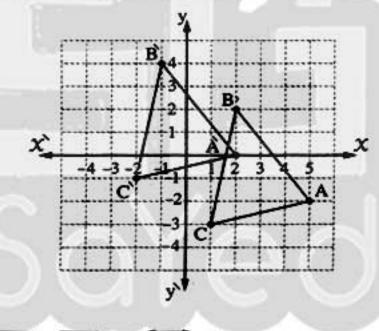
(2)(3,5)

(3) 120°

(4) parallel , equal in length

(5) perpendicular

3 [a]



[b]  $: \overline{ED} / / \overline{ZY}$  and  $\overline{DY}$  is a transversal.

 $\therefore$  m ( $\angle$  XDE) = m ( $\angle$  Y) = 50° (corresponding angles)

In  $\triangle$  XDE:

 $m (\angle XED) = 180^{\circ} - (70^{\circ} + 50^{\circ}) = 60^{\circ}$ 

(The req.)

{a] ∵ E ∈ AC

 $m (\angle BEC) = 180^{\circ} - 65^{\circ} = 115^{\circ}$ (First req.)

 $m (\angle BEC) + m (\angle CED) = 115^{\circ} + 85^{\circ} = 200^{\circ}$ 

.. The points B , E and D are not on the same straight line. (Second req.)

### [b] $\therefore$ $\angle$ AMB is an exterior angle of $\triangle$ MBC

$$\therefore$$
 m ( $\angle$  BCM) = 80° - 50° = 30°

$$\therefore$$
 m ( $\angle$  BCM) = m ( $\angle$  DAC)

$$\therefore a + 10^{\circ} + 2 a + 50^{\circ} = 180^{\circ}$$

(interior angles in the same side of the transversal)

$$\therefore 3 a + 60^{\circ} = 180^{\circ}$$
.

(The req.)

#### [b] In ∆ ABC :

$$\therefore FD = \frac{1}{2} CB = EC = 8 cm.$$

$$\therefore DE = \frac{1}{2} AC = CF = 6 cm.$$

$$= 6 + 8 + 6 + 8 = 28$$
 cm.

(The req.)

### Additional question

- 1 (1) 10 cm. (2) BA
- 2 In  $\triangle$  XYZ:  $\cdots$  m ( $\angle$  XYZ) = 90°

$$\therefore (XZ)^2 = (XY)^2 + (YZ)^2 = 49 + 576 = 625$$

∴ XZ = 
$$\sqrt{625}$$
 = 25 cm.

In 
$$\triangle$$
 XLZ:  $\cdots$  m ( $\angle$  XLZ) = 90°

$$\therefore (LZ)^2 = (XZ)^2 - (XL)^2 = 625 - 225 = 400$$

∴ LZ = 
$$\sqrt{400}$$
 = 20 cm.

(The req.)

(5) (d)

## Giza

- 1 (b)
- (c)
- (3) (a)
- (c)

- 2 (1) (2, -5)
- (2) right angled
- (3) is parallel to the third side
- (4) rhombus
- (5) concave

- [a] : ABCD is a rhombus , BD is a diagonal in it.
  - ∴ BD bisects ∠ ABC
  - , ∵ m (∠ ABD) = 62°
  - $\therefore$  m ( $\angle$  ABC) = 2 m ( $\angle$  ABD) = 2 × 62° = 124°
  - $m (\angle BAD) = 180^{\circ} 124^{\circ} = 56^{\circ}$
- **(b)** The number of sides =  $\frac{360^{\circ}}{180^{\circ} 135^{\circ}} = 8$

- [a] : D is the midpoint of AB , F is the midpoint of AC
  - $\therefore DF = \frac{1}{2} BC$
- $\therefore$  DF = 4 cm.
- : F is the midpoint of  $\overline{AC}$  E is the midpoint of  $\overline{BC}$
- $\therefore FE = \frac{1}{2}AB$
- $\therefore$  FE = 3 cm.
- E is the midpoint of  $\overline{BC}$  D is the midpoint of  $\overline{AB}$
- $\therefore$  ED =  $\frac{1}{2}$  AC
- ∴ ED = 5 cm.
- $\therefore$  The perimeter of  $\triangle$  DEF = 4 + 3 + 5 = 12 cm.

(The req.)

#### [b] In A ABC:

- : E is the midpoint of BA , F is the midpoint of CA
- : EF // BC
- , .: AD // BC
- : EF // AD
- (1)

- $EF = \frac{1}{2}BC$
- $\Rightarrow$  : AD =  $\frac{1}{2}$  BC
- : EF = AD
- (2)

- From (1) and (2):
- .. AEFD is a parallelogram.
- (Q.E.D.)

- (1)  $\triangle ABC$  is the image of  $\triangle ABC$  by rotation about O with an angle of measure 90°
- (2)  $\triangle ABC$  is the image of  $\triangle ABC$  by reflection in X-axis.

### Additional question

- 1 (1) (c)

- The figure AECD is a rectangle
  - ∴ EC = AD = 9 cm.
  - $\therefore BE = 17 9 = 8 \text{ cm}.$
  - $\therefore$  In  $\triangle$  AEB :  $\because$  m ( $\angle$  AEB) = 90°
  - $(AE)^2 = (AB)^2 (BE)^2 = 289 64 = 225$
  - ∴ AE =  $\sqrt{225}$  = 15 cm.
  - ∴ DC = AE = 15 cm.

(First req.)

The area of the trapezium ABCD

- = The area of  $\triangle$  ABE + The area of the rectangle AECD
- $=\frac{1}{2} \times 8 \times 15 + 9 \times 15 = 195 \text{ cm}^2$  (Second req.)

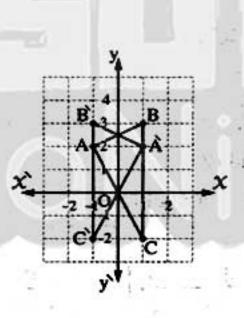
# Alexandria

- 1 (1) (b)
- (b) (s)
- (3) (b)
- (4) (b) (5) (b)
- 2 (1) parallelogram (2) (1 > -4)
- (3) parallel

- (4) 360°
- (5) 115°

3

[a]



- [b] : ABCD is a parallelogram , M is the intersection point of its diagonals
  - .. M is the midpoint of BD

In A ABD:

- .. M is the midpoint of BD , MX // AB
- .. X is the midpoint of AD
- (Q.E.D.)

- [a] . D is the midpoint of AB , F is the midpoint of AC
  - $\therefore$  DF =  $\frac{1}{2}$  BC
- $\therefore$  DF = 3.5 cm.
- , .. F is the midpoint of AC , E is the midpoint of BC

- $\therefore FE = \frac{1}{2}AB$
- $\therefore$  FE = 4 cm.
- . .: E is the midpoint of BC . D is the midpoint of AB
- $\therefore$  ED =  $\frac{1}{2}$  AC
- $\therefore$  ED = 5 cm.
- $\therefore$  The perimeter of  $\triangle$  DEF = 4 + 3.5 + 5 = 12.5 cm.

(The req.)

**[b]** The number of sides =  $\frac{360^{\circ}}{180^{\circ} - 135^{\circ}}$  = 8 sides



- [a] 95°
- [b]  $\therefore$   $\angle$  EDC is an exterior angle of  $\triangle$  BCD
  - $\therefore$  m ( $\angle$  EDC) = m ( $\angle$  B) + m ( $\angle$  C)
  - $m (\angle C) = 105^{\circ} 55^{\circ} = 50^{\circ}$
  - : CA bisects  $\angle$  C : m ( $\angle$  ACB) =  $\frac{50^{\circ}}{2}$  = 25°
  - :  $\angle$  CAD is an exterior angle of  $\triangle$  ABC
  - $m (\angle CAD) = m (\angle B) + m (\angle ACB)$ 
    - $=55^{\circ} + 25^{\circ} = 80^{\circ}$ (The req.)

### Additional question

- 1 (1)  $(XY)^2 (YZ)^2$  (2) (4, -2)
- 2 : ABCD is a rectangle
  - :. AD // BC
  - ∴ m (∠ XAM)
    - $= m (\angle YCM)$

(alternate angles)

- $\Delta\Delta$  AMX , CMY in them :  $m (\angle XAM) = m (\angle YCM)$
- $m (\angle AMX) = m (\angle CMY) (V.O.A.)$
- AM = CM
- $\triangle AMX \equiv \triangle CMY$ , then we deduce that XM = MY
- $Y \in XM$
- .. Y is the image of X by reflection in the point M (Q.E.D. 1)
- ∴ AM = CM , MX = MY
- .. The figure AXCY is a parallelogram. (Q.E.D.2)

# Alexandria

- 1 (1) (c)
- (a) (p)
- (3)(c)
- (4) (d)

(5) (b)

- 2 (1) trapezium
- (2)(5,-3)
- (3) parallel , equal in length
- (4) 60°
- (5) 360°

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

موقع والكروال التعليم

الصف الاول الاعدادي

[a] 80°

[b] In the square ABCD:

- $\therefore \overline{AD} / \overline{BC}, E \in \overline{BC}$ :. AD // CE
- , :: AC // DE
- .. ACED is a parallelogram.

(First req.)

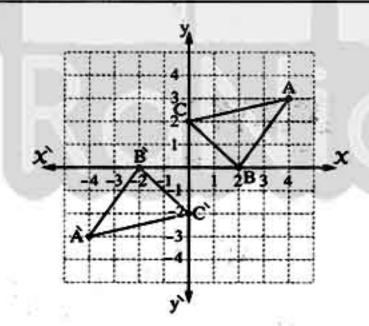
- ·· CA bisects ∠ BCD
- ∴ m (∠ ACB) = 45°
- $m (\angle ACE) + m (\angle ACB) = 180^{\circ}$

(Supplementary angles)

:. m ( $\angle$  ACE) = 180° - 45° = 135° (Second req.)

- [a] The sum of measures of the interior angles of hexagon =  $(6-2) \times 180^{\circ} = 720^{\circ}$
- [b] : D is the midpoint of AB , F is the midpoint of AC
  - $\therefore$  DF =  $\frac{1}{2}$  BC
- $\therefore$  DF = 4 cm.
- . F is the midpoint of AC . E is the midpoint of BC
- $\therefore FE = \frac{1}{2}AB$
- $\therefore$  FE = 2.5 cm.
- . .: E is the midpoint of BC . D is the midpoint of AB
- $\therefore$  ED =  $\frac{1}{2}$  AC
- $\therefore$  ED = 3.5 cm.
- $\therefore$  The perimeter of  $\triangle$  DEF = 4 + 2.5 + 3.5 = 10 cm.

(The req.)



### Additional question

- 1 (1)(-2,7) (2)(-2,-1)
- In ∆ ADC : ∵ AD ⊥ BC
  - ∴ m (∠ ADC) = 90°
  - $(AD)^2 = (AC)^2 (DC)^2 = 400 256 = 144$
  - :. AD =  $\sqrt{144}$  = 12 cm.

In  $\triangle$  ADB :  $\cdots$  m ( $\angle$  ADB) = 90°

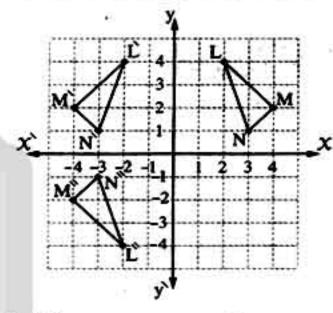
- $(AB)^2 = (AD)^2 + (DB)^2 = 144 + 81 = 225$
- ∴ AB =  $\sqrt{225}$  = 15 cm.

(The req.)

# El-Kalyoubia

- 1 (1)  $(n-2) \times 180^{\circ}$
- (2) trapezium
- (3) bisects the third side
- (4) (5,1)
- (5)(0,3)
- 2 (1) (a)
- (b) (c)
- (3)(c)
- (4) (a)
- (5) (d)

3



- (1)  $\triangle$  LMN is the image of  $\triangle$  LMN by reflection in y-axis.
- (2)  $\Delta LMN$  is the image of  $\Delta LMN$  by rotation about the origin with an angle of measure 180°

- [a] In A ABC:
  - : D is the midpoint of AB
  - O is the midpoint of AC
  - $\therefore OD = \frac{1}{2} CB = HC = 6 cm.$
  - : D is the midpoint of AB
  - , H is the midpoint of BC
  - $\therefore DH = \frac{1}{2} AC = CO = 5 cm.$
  - .. The perimeter of the quadrilateral DHCO
    - = 6 + 5 + 6 + 5 = 22 cm.

(The req.)

**[b]** The number of sides =  $\frac{360^{\circ}}{180^{\circ} - 108} = 5$  sides

5

- [a] : OX // BC , OB is a transversal to them
  - $\therefore$  m ( $\angle$  B) + m ( $\angle$  O) = 180°

(two interior angles in the same side of the transversal)

- $\therefore$  m ( $\angle$  B) = 180° 135° = 45°
- .. DH // BC and DC is a transversal to them
- $\therefore m (\angle C) + m (\angle D) = 180^{\circ}$

(two interior angles in the same side of the transversal)

 $m (\angle C) = 180^{\circ} - 120^{\circ} = 60^{\circ}$ 

∴ In AABC:

$$m (\angle BAC) = 180^{\circ} - (45^{\circ} + 60^{\circ}) = 75^{\circ} \text{ (The req.)}$$

[b] : m ( $\angle$  ABC) + m ( $\angle$  CBD) + m ( $\angle$  DBH)

+ m ( $\angle$  HBA) = 360° (accumulative angles at B)

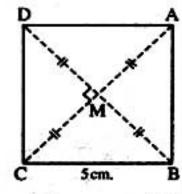
 $\therefore$  m ( $\angle$  HBD) = 360° - (110° + 35° + 140°) = 75°

(The req.)

### Additional question

1 (1) The origin point

(2) 5 cm.



The image of the square ABCD by reflection in the point M is the square CDAB We notice that we got the same square.

# El-Kalyoubia

(1) 120°

(2) square

(3)(-2,-4)

(4)(0,2)

(5) 180°

(1) (b)

(5) (p)

(3)(c)

(4)(c)

(5) (d)

#### [a] In A ABC:

.. X is the midpoint of AB, Z is the midpoint of AC

 $\therefore XZ = \frac{1}{2}BC = BY = 5 cm.$ 

.. Z is the midpoint of AC , Y is the midpoint of BC

 $\therefore ZY = \frac{1}{2} AB = BX = 4 cm.$ 

.. The perimeter of the figure XBYZ

= 5 + 4 + 5 + 4 = 18 cm.

(The req.)

#### [b] In \( \Delta \) ABC :

$$m (\angle BAC) = 180^{\circ} - (70^{\circ} + 50^{\circ}) = 60^{\circ}$$

, ∵ AD bisects ∠ BAC

 $\therefore$  m ( $\angle$  BAD) =  $\frac{60^{\circ}}{5}$  = 30°

∴ From ∆ ABD :

 $m (\angle ADB) = 180^{\circ} - (70^{\circ} + 30^{\circ}) = 80^{\circ}$ 

[a]  $: AB \cap CD = \{0\}$ 

 $\therefore$  m ( $\angle$  BOD) = m ( $\angle$  AOC) = 50° (V.O.A.)

, ∵ OD bisects ∠ BOH

 $\therefore$  m ( $\angle$  BOH) = 2 × 50° = 100°

 $, : O \in AB$ 

 $\therefore$  m ( $\angle$  AOH) = 180° - 100° = 80° (The req.)

### $[b] : H \in BC$

 $\therefore$  m ( $\angle$  AHC) = 180° - 70° = 110°

, : AHCD is a quadrilateral.

 $m (\angle HAD) = 360^{\circ} - (110^{\circ} + 115^{\circ} + 65^{\circ}) = 70^{\circ}$ 

 $\therefore$  m ( $\angle$  BAD) = 70° + 45° = 115°

 $\therefore$  m ( $\angle$  BAD) = m ( $\angle$  C) (1)

 $_{9}$  In  $\triangle$  ABH ::: m ( $\angle$  B) = 180° - (45° + 70°) = 65°

 $\therefore$  m ( $\angle$  B) = m ( $\angle$  D)

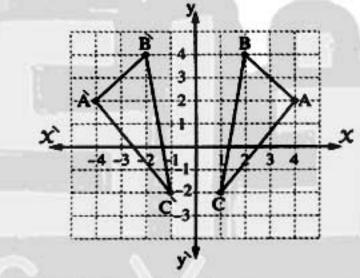
(2)

From (1) and (2):

5

.. ABCD is a parallelogram.

(Q.E.D.)



### Additional question

1 (1) The sum of the squares of the lengths of the other two sides (2) 3

A is the image of itself by reflection in AB

, B is the image of itself by reflection in AB

∴ ∆ ABC is the image of ∆ ABC by reflection in AB

 $\therefore$  m ( $\angle$  CAB) = m ( $\angle$  CAB)

 $\therefore m (\angle CAC) = 2 m (\angle CAB) (Q.E.D. 1) (1)$ 

Similarly we can prove that:

 $m (\angle ACA) = 2 m (\angle ACD)$ 

: ABCD is a rectangle

∴ AB // CD

 $\therefore$  m ( $\angle$  BAC) = m ( $\angle$  ACD) (alternate angles) (3)

From (1)  $\Rightarrow$  (2)  $\Rightarrow$  (3) :  $\therefore$  m ( $\angle$  CAC) = m ( $\angle$  ACA) but they are alternate angles

:. AC // AC

(Q.E.D. 2)

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

# El-Dakahlia



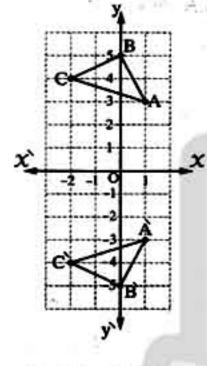
- (1)(c)
- (a) (p)
- (3) (b)
- (4) (d) (5) (b)

- (1) half the length of the third side.
- (2) square

- (3) rhombus
- (4) 360°
- (5)(2,-3)

### 3

[a]



- [b] In  $\triangle$  ACD: m ( $\angle$  D) = 180° (55° + 25°) = 100°
  - : ABCD is a parallelogram
  - $\therefore$  m ( $\angle$  B) = m ( $\angle$  D) = 100°
- (The req.)

- [a] From  $\triangle$  BEF: m ( $\angle$  EBF) = 180° (90° + 50°) = 40°
  - $: \overline{CF} \cap \overline{AE} = \{B\}$
  - $\therefore$  m ( $\angle$  ABC) = m ( $\angle$  EBF) = 40° (V.O.A.)
  - , : AD // EF , AE is a transversal
  - $\therefore m (\angle A) = m (\angle E) = 90^{\circ}$ (alternate angles)
  - .. from the quadrilateral ABCD
  - $m (\angle C) = 360^{\circ} (40^{\circ} + 90^{\circ} + 110^{\circ}) = 120^{\circ} (The req.)$
- [b] ∵ ∠ AHB is an exterior angle of ∆ ACH
  - $\therefore$  m ( $\angle$  HAC) = 70° 40° = 30°
  - ∵ AH bisects ∠ BAC
  - $\therefore$  m ( $\angle$  BAC) = 2 × 30° = 60°
- (First req.)
- $\bullet$  :  $\angle$  ABC is an exterior angle of  $\triangle$  ABC
- :.  $m (\angle ABD) = 40^{\circ} + 60^{\circ} = 100^{\circ}$  (Second req.)

#### In A ABC:

- : D is the midpoint of AB
- H is the midpoint of AC
- $\therefore \overline{DH} // \overline{BC} \cdot DH = \frac{1}{2} BC$

- , ∵ X is the midpoint of DO, XY // DH
- .. Y is the midpoint of HO
- (First req.)
- $XY = \frac{1}{2} HD$
- $\cdot : DH = \frac{1}{2} BC$
- $\therefore XY = \frac{1}{2} \times \frac{1}{2} BC = \frac{1}{4} BC$
- $\therefore XY = \frac{1}{4} \times 12 = 3 \text{ cm}.$
- (Second req.)

### Additional question

- 1 (1) (-4,1)
- (2) Three
- In  $\triangle$  BCD:  $m (\angle B) = 90^{\circ}$ 
  - $\therefore$  (BD)<sup>2</sup> = (CD)<sup>2</sup> (CB)<sup>2</sup> = 169 144 = 25
  - :. BD =  $\sqrt{25}$  = 5 cm.
  - In  $\triangle$  ABC:  $\because$  m ( $\angle$  B) = 90°
  - AB = 11 + 5 = 16 cm.
  - $(AC)^2 = (AB)^2 + (BC)^2 = 256 + 144 = 400$
  - ∴ AC =  $\sqrt{400}$  = 20 cm.
- (The req.)

#### Kafr El-Sheikh 10

- (1) (d)
- (a) (p)
- (3)(c)
- (4)(c)
- (5) (a)

- (1) are equal in measure
- (2) a rhombus , a square
- (3) convex
- (4)(3,-3)
- (5) bisects the third side

- [a] The measure of each interior angle of the regular octagon =  $\frac{(8-2) \times 180^{\circ}}{9}$  = 135°
- [b] Construction:
  - Draw BD and AC
  - Proof: In A ABD
- : X is the midpoint of AB
- , L is the midpont of AD
- $\therefore \overline{XL} // \overline{BD} \rightarrow XL = \frac{1}{2} BD$
- (1)

- , In A DBC :
- .. Y is the midpoint of BC , Z is the midpoint of DC
- $\therefore \overline{YZ} // \overline{BD}, YZ = \frac{1}{2} BD$
- (2)

From (1), (2):  $\overline{XL} // \overline{YZ}$ , XL = YZ

- ∴ XYZL is a parallelogram → From ∆ ABC :
- .. X is the midpoint of AB
- , Y is the midpoint of BC

$$\therefore XY = \frac{1}{2}AC$$

(3)

From  $(1) \cdot (3)$ :

- The two diagonals of the rectangle are equal in length
- $\therefore LX = XY$
- ∴ XYZL is a rhombus
- (Q.E.D. 1)
- , the perimeter of the rhombus

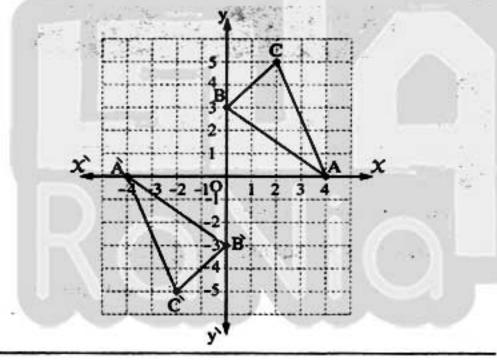
$$= 4 \text{ XL} = 4 \times \frac{1}{2} \text{ BD} = 2 \text{ BD}$$

(Q.E.D. 2)

- [a] : E is the midpoint of AB
  - D is the midpoint of AC
  - $\therefore DE = \frac{1}{2} BC = 6 cm.$
  - :. The perimeter of  $\triangle$  ADE = 6 + 6 + 6 = 18 cm.

(The req.)

[b]



[a]  $\Delta\Delta$  DXB , EYC in them :

$$DB = EC$$

$$DX = EY$$

$$m (\angle DXB) = m (\angle EYC) = 90^{\circ}$$

 $\therefore \Delta DXB \equiv \Delta EYC$ , Then we deduce that:

$$m (\angle B) = m (\angle C)$$

·· BC // DE and AB is a transversal to them

$$\therefore m (\angle ADE) = m (\angle B) \tag{2}$$

(Corresponding angles)

Similarly:  $m (\angle AED) = m (\angle C)$ (3)

(Corresponding angles)

From (1), (2) and (3):

$$\therefore$$
 m ( $\angle$  ADE) = m ( $\angle$  AED)

(Q.E.D.)

- [b]  $\therefore$   $\angle$  ABE is an exterior angle of  $\triangle$  ABC
  - $\therefore$  m ( $\angle$  ABE) = 60° + 55° = 115°
  - , ∵ BD bisects ∠ ABE
  - ∴ m ( $\angle$  DBE) =  $\frac{115^{\circ}}{2}$  = 57.5°

(The req.)

### Additional question

- (1)(-a,b)
  - (2) The sum of the squares of the lengths of the other two sides.
- 2 In  $\triangle$  ABC: m ( $\angle$  B) = 90°

$$(AC)^2 = (AB)^2 + (BC)^2 = 81 + 144 = 225$$

:. AC =  $\sqrt{255}$  = 15 cm.

In  $\triangle$  ACD:  $\cdots$  m ( $\angle$  ACD) = 90°

$$(AD)^2 = (AC)^2 + (DC)^2 = 225 + 400 = 625$$

- $\therefore$  AD =  $\sqrt{625}$  = 25 cm.
- .. The perimeter of the figure ABCD = 9 + 12 + 20 + 25 = 66 cm.

## El-Gharbia

1

- (1) (b)
- (2) (a)
- (3) (b)
- (4) (a)
- (5) (a)

- (1) parallel to the third side , its length is half the length of the third side.
- (2) 50°
- (3) (-3,1) (4) square (5) (3,-5)

3

- [a] : ABCD is a parallelogram.
  - .. M is the midpoint of AC
  - ∴ AC = 2 MA
- ∴ AC = 7 cm.
- $\Rightarrow$ : AB = DC = 3 cm.  $\Rightarrow$  BC = AD = 6 cm.
- $\therefore$  The perimeter of  $\triangle$  ABC = 3 + 6 + 7 = 16 cm.

(The req.)

- [b] : FE // BC , FB is a transversal.
  - $\therefore$  m ( $\angle$  EFB) = m ( $\angle$  CBF) = 60°

(alternate angles)

In  $\triangle$  ABC:

 $\therefore$  m ( $\angle$  BAC) = 180° - (60° + 40°) = 80° (The req.)

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

(1)

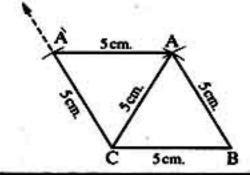
### [a] In the pentagon ABCDE:

$$m (\angle A) + m (\angle B) + m (\angle C) + m (\angle D)$$
$$+ m (\angle E) = 540^{\circ}$$

$$m (\angle E) = 540^{\circ} - (140^{\circ} + 130^{\circ} + 90^{\circ} + 110^{\circ}) = 70^{\circ}$$

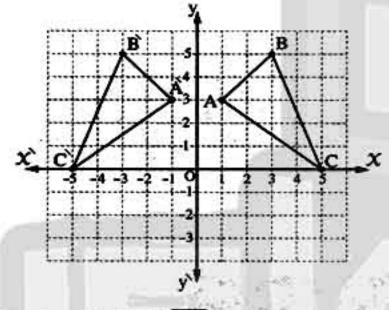
(The req.)

[b]



5

[a]



### [b] : X is the midpoint of AB , Y is the midpoint of BC

$$\therefore XY = \frac{1}{2}AC$$

$$\therefore$$
 XY = 3 cm.

$$\therefore YZ = \frac{1}{2} AB$$

$$\therefore$$
 YZ = 3.5 cm.

$$\therefore$$
 Z is the midpoint of  $\overline{AC}$ , X is the midpoint of  $\overline{AB}$ 

$$\therefore ZX = \frac{1}{2} BC$$

$$\therefore$$
 ZX = 4.5 cm.

$$\therefore$$
 The perimeter of  $\triangle$  XYZ = 3 + 3.5 + 4.5 = 11 cm.

(The req.)

### Additional question

- 1 (1) 5 cm. (2) axis of symmetry

## $2 \ln \Delta ADB : : m (\angle ADB) = 90^{\circ}$

$$\therefore (BD)^2 = (AB)^2 - (AD)^2 = 676 - 576 = 100$$

∴ BD = 
$$\sqrt{100}$$
 = 10 cm.

In 
$$\triangle$$
 ADC:  $\cdots$  m ( $\angle$  ADC) = 90°

$$\therefore$$
 (CD)<sup>2</sup> = (AC)<sup>2</sup> - (AD)<sup>2</sup> = 900 - 576 = 324

∴ CD = 
$$\sqrt{324}$$
 = 18 cm.

$$\therefore$$
 BC = 18 + 10 = 28·cm.

(The req.)

# Damietta

1

- (1) (a)
- (2) (a)
- (3) (b)
- (4)(d)
- (5) (c)

[2]

- (1) equal in measure
- (2) 50°
- (3) bisects

- (4) 120°
- (5)(3,2)

[a]  $: m (\angle ABC) + m (\angle CBD) + m (\angle DBE)$ 

+ m (
$$\angle$$
 EBA) = 360° (accumulative angles at B)

 $\therefore$  m ( $\angle$  EBD) = 360° - (110° + 35° + 140°) = 75°

(The req.)

- [b] In the square ABCD:
  - : AD = BC , BC = CE
- ∴ AD = CE (1)
- : AD // BC , E ∈ BC
- :. AD // CE (2)

From (1) and (2):

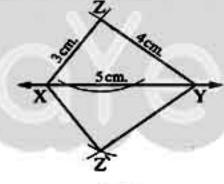
- .. The figure ACED is a parallelogram. (First req.)
- : AC bisects ∠ BAD
- ∴ m (∠ CAD) = 45°
- $\therefore$  m ( $\angle$  E) = 45°

(properties of parallelogram)

(Second req.)

4

[a]



[b] : D is the midpoint of AB , E is the midpoint of AC

$$\therefore DE = \frac{1}{2} BC$$

$$\therefore$$
 DE = 5 cm.

, : E is the midpoint of AC , F is the midpoint of BC

$$\therefore FE = \frac{1}{2}AB$$

$$\therefore$$
 FE = 4 cm.

, .. F if the midpoint of BC , D is the midpoint of AB

$$\therefore FD = \frac{1}{2}AC$$

$$\therefore$$
 ED = 3 cm.

 $\therefore$  The perimeter of  $\triangle$  DEF = 4 + 3 + 5 = 12 cm.

(The req.)

[5]

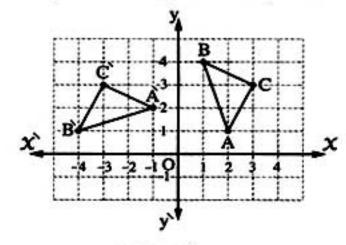
- [a] : BA // DF , BD is a transversal
  - $\therefore$  m ( $\angle$  D) = m ( $\angle$  B) = 60°

(alternate angles)

In  $\triangle$  CDF:

$$m (\angle DCF) = 180^{\circ} - (60^{\circ} + 40^{\circ}) = 80^{\circ} \text{ (The req.)}$$

[b]



### Additional question

- 1 (1) (c)
- (2)(b)
- In  $\triangle$  ABD:  $m (\angle ADB) = 90^{\circ}$ 
  - $(AD)^2 = (AB)^2 (BD)^2 = 169 25 = 144$
  - $\therefore$  AD =  $\sqrt{144}$  = 12 cm.
  - In  $\triangle$  ADC:  $m (\angle ADC) = 90^{\circ}$
  - $(AC)^2 = (AD)^2 + (DC)^2 = 144 + 256 = 400$
  - ∴ AC =  $\sqrt{400}$  = 20 cm.
- (The req.)

# El-Fayoum

- (1) (a)
- (b) (s)
- (3) (c)
- (d) (d)
- (5) (a)

- (1) parallel to the third side.
- (2)(1,0)
- (3) a rectangle
- (4) 108°

- [a]  $: \overline{DA} \cap \overline{EB} = \{M\}$ 
  - $\therefore$  m ( $\angle$  BMD) = m ( $\angle$  AME) = 72°
- (V.O.A.)

(5) 180°

- , ∵ MC bisects ∠ BMD
- $\therefore m (\angle CMD) = \frac{72^{\circ}}{2} = 36^{\circ}$
- (The req.)
- [b]  $: m (\angle BAC) = m (\angle ABC)$ 
  - $\bullet$   $\angle$  ACD is an exterior angle of  $\triangle$  ABC
  - ∴ m ( $\angle$  ABC) =  $\frac{128^{\circ}}{2}$  = 64°
- (The req.)

#### [a] In Δ ABC:

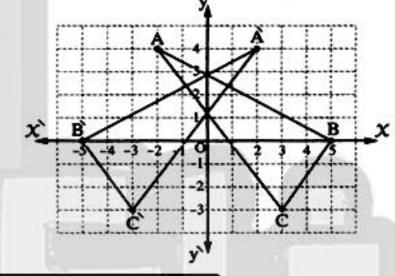
- .. X is the midpoint of AB , Z is the midpoint of AC
- $\therefore XZ = \frac{1}{2}BC$
- ∴ BC = 8 cm.
- . . X is the midpoint of AB, Y is the midpoint of BC
- $\therefore XY = \frac{1}{2}AC$
- $\therefore$  AC = 5 cm.

- , .. Y is the midpoint of BC, Z is the midpoint of AC
- $\therefore YZ = \frac{1}{2}AB$
- $\therefore$  AB = 6 cm.
- $\therefore$  The perimeter of  $\triangle$  ABC = 8 + 5 + 6 = 19 cm.
- [b] : ABCDEF is a regular hexagon
  - .. The measure of each exterior angle of the regular
    - hexagon =  $\frac{360^{\circ}}{6}$  =  $60^{\circ}$

- [a] : DE // BC , DC is a transversal
  - $\therefore$  m ( $\angle$  C) = m ( $\angle$  D) = 70°
- (alternate angles)
- $\therefore$   $\angle$  DAB is an exterior angle of  $\triangle$  ABC
- $\therefore$  m ( $\angle$  DAB) = 40° + 70° = 110°
- (The req.)

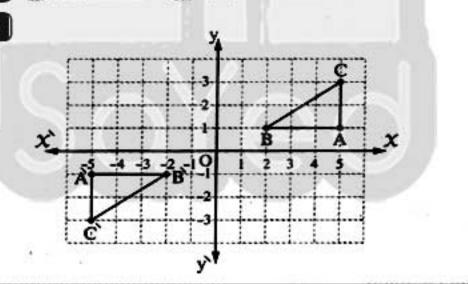
(The req.)

[b]



### Additional question

- 1 (b)
- (2) (a)



# Beni Suef

- 1 (1) (c)
  - (2) (a)
- (3) (b)
- (4) (a)
- (5) (b)
- 2 (1) equal in measure
- (2)(0,4)
- (3) trapezium
- (4) a rhombus , a square
- (5) 360°

3

- [a] : ABCD is a square and BD is a diagonal in it.
  - $\therefore$  m ( $\angle$  C) = 90° and m ( $\angle$  BDC) = 45°

In the quadrilateral CDME:

$$\therefore$$
 m ( $\angle$  MEC) = 360° - (90° + 45° + 102°) = 123°

(The req.)

**[b]** The number of sides = 
$$\frac{360^{\circ}}{180^{\circ} - 135^{\circ}} = 8$$
 sides

$$\therefore$$
 m ( $\angle$  BAE) + m ( $\angle$  E) = 180°

(interior angles in the same side of the transversal)

$$\therefore$$
 m ( $\angle$  BAE) = 180° - 60° = 120°

$$\therefore$$
 m ( $\angle$  BAE) + m ( $\angle$  B) = 180°

but they are interior angles in the same side of AB

(Q.E.D.)

[b] 
$$\therefore \overrightarrow{AC} \cap \overrightarrow{DF} = \{B\}$$

$$\therefore m (\angle CBF) = m (\angle ABD) = 30^{\circ} \qquad (V.O.A.)$$

$$\therefore m (\angle CBE) = m (\angle EBF) = \frac{30^{\circ}}{2} = 15^{\circ}$$

$$\therefore$$
 m ( $\angle$  ABF) = 180° - 30° = 150°

$$\therefore m (\angle ABE) = m (\angle ABF) + m (\angle EBF)$$

$$= 150^{\circ} + 15^{\circ} = 165^{\circ}$$
 (The req.)

### 5

#### [a] In $\triangle$ ABC:

- : E is the midpoint of AB , F is the midpoint of AC
- : EF // BC

(1)

EF = 
$$\frac{1}{2}$$
 BC

$$\therefore$$
 BC = 2 EF

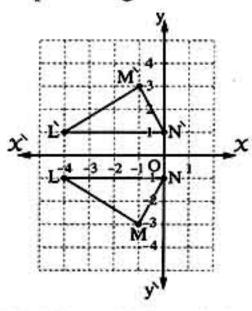
$$\therefore$$
 EF = AD

(2)

#### From (1) , (2):

(Q.E.D.)

#### [b]



### Additional question

- 1 (1) The point C
- (2) CD
- (3) ∆ CYM

2 In 
$$\triangle$$
 ABC:  $\because$  m ( $\angle$  B) = 90°

$$(AC)^2 = (AB)^2 + (BC)^2 = 49 + 576 = 625$$

∴ AC = 
$$\sqrt{625}$$
 = 25 cm.

In 
$$\triangle$$
 ADC:  $m (\angle D) = 90^{\circ}$ 

$$\therefore$$
 (CD)<sup>2</sup> = (AC)<sup>2</sup> - (AD)<sup>2</sup> = 625 - 225 = 400

∴ DC = 
$$\sqrt{400}$$
 = 20 cm.

(The req.)

#### Souhag 15

- 1 (1) 108°
- (2) 110°
- (3) half the length of the third side.
- (4) (6,1)
- (5) 50°
- 2 (1) (c)
- (2) (d)
- (3) (c) (4) (a)
- (5) (a)

- [a] : XY // EZ , XE is a transversal
  - $\therefore m (\angle X) + m (\angle E) = 180^{\circ}$

(interior angles in the same side of the transversal)

$$\therefore$$
 m ( $\angle$  E) = 180° - 115° = 65°

$$\therefore$$
 m ( $\angle$  E) = m ( $\angle$  YZF) = 65°

but they are corresponding angles

(Q.E.D.)

$$\therefore m (\angle C) + m (\angle A) = 180^{\circ}$$

(interior angles and in the same side of the transversal)

$$\therefore$$
 m ( $\angle$  C) = 180° - 110° = 70°

 $\therefore$   $\angle$  AED is an exterior angle of  $\triangle$  CDE

$$\therefore$$
 m ( $\angle$  AED) = 50° + 70° = 120°

(The req.)

#### 4

[a] :  $m (\angle BAE) + m (\angle EAC) + m (\angle CAB) = 360^{\circ}$ (accumulative angles at A)

$$\therefore$$
 m ( $\angle$  CAB) = 360° - (130° + 90°) = 140°

$$\therefore$$
 m ( $\angle$  CAB) + m ( $\angle$  C) = 180°

(interior angles in the same side of the transversal)

$$\therefore$$
 m ( $\angle$  C) = 180° - 140° = 40°

(The req.)

[b] 
$$: \overrightarrow{AE} \cap \overrightarrow{CD} = \{B\}$$

$$\therefore$$
 m ( $\angle$  DBE) = m ( $\angle$  ABC) = 50° (V.O.A.)

$$\therefore$$
 m ( $\angle$  EBF) = m ( $\angle$  DBE) = 50°

$$\therefore$$
 m ( $\angle$  FBC) = 180° - (50° + 50°) = 80°

(Q.E.D.)

- ① Δ ABC is the image of Δ ABC by reflection in x-axis.
- (2) Δ ABC is the image of Δ ABC by rotation about origin point with an angle of measure 180°

#### Additional question

- 1 (1) two (2) -4 (3) axis of symmetry
- 2 In  $\triangle$  ABC:  $\cdots$  m ( $\angle$  B) = 90°

$$(AB)^2 = (AC)^2 - (BC)^2 = 400 - 144 = 256$$

∴ AB = 
$$\sqrt{256}$$
 = 16 cm.

$$\therefore AD = AB - BD = 16 - 9 = 7 \text{ cm}.$$

$$AE = 2 BC$$
  $\therefore AE = 2 \times 12 = 24 cm.$ 

$$\therefore$$
 m ( $\angle$  A) = m ( $\angle$  B) = 90° (alternate angles)

In 
$$\triangle$$
 ADE:  $\cdots$  m ( $\angle$  A) = 90°

$$\therefore$$
 (DE)<sup>2</sup> = (AE)<sup>2</sup> + (AD)<sup>2</sup> = 576 + 49 = 625

∴ DE = 
$$\sqrt{625}$$
 = 25 cm. (T

(The req.)

## Answers of school book models in geometry and measurement

# Model

- 1 (1) (b)
- (2) (a)
- (3) (d)
- (4) (b)
- (5) (b)

### 2

- (1)(2,-1)
- (2)(-2,1)
- (3) its two diagonals are perpendicular
- (4) 120°
- (5) (8,2)

- [a]  $\therefore$  m ( $\angle$  A) = m ( $\angle$  B) = 25°
  - , ∠ ACD is an exterior angle of △ ABC
  - $m (\angle ACD) = 25^{\circ} + 25^{\circ} = 50^{\circ}$
- (The req.)
- [b] : D is the midpoint AB
- $\therefore AD = \frac{1}{2}AB$
- $\therefore AD = \frac{1}{2} \times 12 = 6 \text{ cm}.$ . . E is the midpoint AC
- $\therefore AE = \frac{1}{2}AC$
- $\therefore AE = \frac{1}{2} \times 8 = 4 \text{ cm}.$
- , .. D is the midpoint AB, E is the midpoint AC
- ∴ ED =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 10 = 5 cm.

:. From (1), (2), (3):

The perimeter of  $\triangle$  ADE = 6 + 4 + 5 = 15 cm.

(The req.)

- [a] : DE // YZ , ZD is a transversal
  - $\therefore$  m ( $\angle$  Z) = m ( $\angle$  D) = 50° (alternate angles)

In A XYZ:

- $m (\angle Z) + m (\angle ZXY) + m (\angle Y) = 180^{\circ}$
- $m (\angle Y) = 180^{\circ} (105^{\circ} + 50^{\circ}) = 25^{\circ}$
- $, :: X \in \overline{DZ}$
- $m (\angle YXD) = 180^{\circ} 105^{\circ} = 75^{\circ}$

(The req.)

- [b] : AZ // YD // XE // CB
  - AY = YX = XC
  - $\therefore AD = DE = EB$
- ∴ EB =  $\frac{18}{3}$  = 6 cm.

### 5

- [a] In  $\triangle$  ABD:  $\cdots$  m ( $\angle$  ADB) = 90°
  - $(BD)^2 = (AB)^2 (AD)^2 = 676 576 = 100$
  - :. BD =  $\sqrt{100}$  = 10 cm.
  - In  $\triangle$  ADC:  $\cdots$  m ( $\angle$  ADC) = 90°
  - $(CD)^2 = (AC)^2 (AD)^2 = 900 576 = 324$

- $\therefore$  CD =  $\sqrt{324}$  = 18 cm.
- $\therefore$  BC = 10 + 18 = 28 cm.
- $\therefore$  The area of  $\triangle$  ABC =  $\frac{1}{2}$  BC  $\times$  AD

$$=\frac{1}{2} \times 28 \times 24 = 336 \text{ cm}^2$$
. (The req.)

(The req.)

- [b] : ABCD is a squre
  - $\therefore \overline{AD} / \overline{BC}$
- , ∵ E∈BC
- ∴ AD // EC
- · ·· AC // DE
- .. ACED is a parallelogram
- (Q.E.D.)

# Model

### [1]

- (1) (b)
- (c)
- (3) (b)
- (4)(c)
- (5) (c)

# 2

- (1) 360°
- (2) (5,5)
- 3 120°
- (4) bisects the third side.
- (5) ZYC

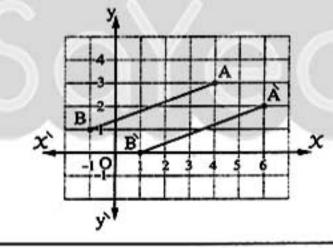
### 3

- [a] In  $\triangle$  XYZ: m ( $\angle$  Y) = 90°
  - $(XZ)^2 = (XY)^2 + (YZ)^2 = 49 + 576 = 625$
  - $\therefore XZ = \sqrt{625} = 25 \text{ cm}.$

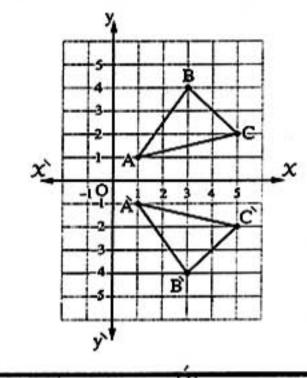
In  $\triangle$  LXZ: m ( $\angle$  L) = 90°

- $\therefore (LZ)^2 = (XZ)^2 (LX)^2 = 625 225 = 400$
- ∴ LZ =  $\sqrt{400}$  = 20 cm.
- (The req.)

[b]



- 4
- [a]



- **[b]** In  $\triangle$  ABC : m ( $\angle$  ACB) = 180° (90° + 30°) = 60°
  - $\rightarrow :: \overline{BD} \cap \overline{AO} = \{C\}$
  - $\therefore m (\angle ACB) = m (\angle OCD) = 60^{\circ} \qquad (V.O.A)$
  - $\therefore$  m ( $\angle$  E) = 360° (60° + 120° + 90°) = 90°

(The req.)

### 5

- [a] : EO // CD , EB is a transversal
  - $\therefore$  m ( $\angle$  CBA) = m ( $\angle$  E) = 50° (alternate angles)

From  $\triangle$  ABC:

- $m (\angle BAC) = 180^{\circ} (50^{\circ} + 30^{\circ}) = 100^{\circ}$
- ∴ ∠ ABD is an exterior angle of △ ABC
- $\therefore$  m ( $\angle$  ABD) = 30° + 100° = 130°
- (The req.)
- $[b] :: \overline{AD} / / \overline{XY} / / \overline{BC}$
- $\cdot : AX = XB$
- $\therefore$  DY = YC
- $\therefore$  Y is the midpoint of  $\overline{CD}$

In  $\triangle$  CDE:  $\therefore$   $\overrightarrow{ZY}$  //  $\overrightarrow{DE}$ 

- , Y is the midpoint of CD
- .. Z is the midpoint of CE
- $\therefore$  CZ = ZE

(Q.E.D.)

## Model

[1]

- (1) (b)
- (5) (c)
- (3) (a)
- (4) (c)
- (5) (b)

### 2

- (1) two adjacent sides are equal in length
- (2) equal in measure
- (3) y-axis
- (4) parallel to the third side
- (5)(-4,-1)

### 3

[a]

- X G 1 A X
- [b] : ABCD is a parallelogram M is the intersection point of its diagonals.
  - $\therefore$  M is the midpoint of  $\overline{AC}$

In  $\triangle$  ABC :  $\cdots$  M is the midpoint of  $\overline{AC}$ ,  $\overline{ME}$  //  $\overline{BC}$ 

- ∴ E is the midpoint of AB
- $\therefore AE = EB$

(Q.E.D.)

#### 4

- [a] : OH // BC , OB is a transversal to them
  - $\therefore m (\angle B) + m (\angle O) = 180^{\circ}$

(two interior angles in the same side of the transversal)

- $\therefore$  m ( $\angle$  B) = 180° 135° = 45°
- : DE // BC and DC is a transversal to them
- $\therefore$  m ( $\angle$  C) + m ( $\angle$  D) = 180°

(two interior angles in the same side of the transversal)

- $m (\angle C) = 180^{\circ} 120^{\circ} = 60^{\circ}$
- ∴ In ∆ ABC:
- $m (\angle BAC) = 180^{\circ} (45^{\circ} + 60^{\circ}) = 75^{\circ} (The req.)$
- [b] In  $\triangle$  ABC: m ( $\angle$  B) = 90°
  - $(AC)^2 = (AB)^2 + (BC)^2 = 144 + 81 = 225$
  - ∴ AC =  $\sqrt{225}$  = 15 cm.

In  $\triangle$  ACD: m ( $\angle$  ACD) = 90°

- $(AD)^2 = (AC)^2 + (DC)^2 = 225 + 400 = 625$
- :. AD =  $\sqrt{625}$  = 25 cm.

(The req.)

#### [5]

- (1)  $\Delta$  LNB
- (S)  $\nabla$  DOM
- (3) ∆ BON

# Model 4

### [1]

- (1) (a)
- (s) (p)
- (3) (a)
- (4) (b)
- (5) (a)

### 2

- (1) parallel to the third side
- (2) equal in measure
- (3) each two opposite sides are parallel (there are another solution).
- (4) (2,-3)
- (5)(-3,-2)

### 3

In  $\triangle$  CEO: m ( $\angle$  COE) = 180° - (35° + 50°) = 95°

- $\cdots \overline{DC} \cap \overline{BE} = \{0\}$
- $\therefore$  m ( $\angle$  DOB) = m ( $\angle$  COE) = 95° (V.O.A) (First req.)

From the quadrilateral ABOD

 $m (\angle B) = 360^{\circ} - (95^{\circ} + 100^{\circ} + 85^{\circ}) = 80^{\circ}$ 

(Second req.)

### 4

- [a] : The length =  $\frac{48}{6}$  = 8 cm.
  - $\therefore$  The length of the diagonal =  $\sqrt{8^2 + 6^2} = 10$  cm.

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### [b] : AB // DE , BD is a transversal

- $\therefore$  m ( $\angle$  B) = m ( $\angle$  D) = 60° (alternate angles)
- → ∴ ∠ AOD is an exterior angle of △ ABO
- $\therefore m (\angle AOD) = m (\angle B) + m (\angle A)$
- $m (\angle A) = 110^{\circ} 60^{\circ} = 50^{\circ}$

#### 5

- [a] The point A = (1, 2)
  - .. The image of the point A (1, 2) by translation (-1, 2) is (0, 4)
- [b] In △ ABC: : DE // BC , D is the midpoint of AB
  - .. E is the midpoint of AC
- $\therefore DE = \frac{1}{2} BC$
- → ∵ O is the midpoint of BC
- $\therefore BO = \frac{1}{2} BC$
- $\therefore$  DE = BO
- → ∵ DE // BC
- .. DBOE is a parallelogram

(First req.)

(The req.)

- : ED =  $\frac{1}{2}$  BC =  $\frac{1}{2} \times 12 = 6$  cm.
- . . D is the midpoint of AB . O is the midpoint of BC
- :. DO =  $\frac{1}{2}$  AC =  $\frac{1}{2}$  × 8 = 4 cm.
- . E is the midpoint of AC . O is the midpoint of BC
- $EO = \frac{1}{2} AB = \frac{1}{2} \times 10 = 5 \text{ cm}.$
- $\therefore$  The perimeter of  $\triangle$  EDO = 6 + 4 + 5 = 15 cm.

(Second req.)

## Model 5

#### 1

- (1) (b)
- (a) (d)
- (3) (a)
- (4) (d)
- (5) (c)

### 2

- 1) The rhombus
- (2) right-angled

- (3) acute
- (4) (2,4)
- (5)(2,4)

### 3

- [a] Theoretical
- [b] : D is the midpoint of  $\overline{AB}$   $\to$  O is the midpoint of  $\overline{AC}$ 
  - $\therefore$  DO =  $\frac{1}{2}$  BC
- $\therefore$  DO = 4 cm.
- , .. O is the midpoint of AC, E is the midpoint of BC
- $\therefore$  OE =  $\frac{1}{2}$  AB
- $\therefore$  OE = 3 cm.
- . E is the midpoint of BC . D is the midpoint of AB
- $\therefore$  ED =  $\frac{1}{2}$  AC
- $\therefore$  ED = 5 cm.
- $\therefore$  The perimeter of  $\triangle$  DEO = 4 + 3 + 5 = 12 cm.

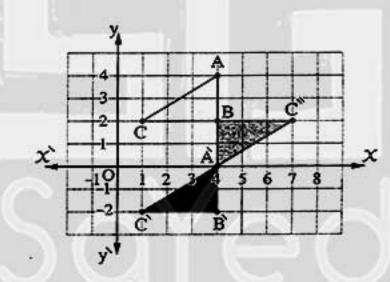
(The req.)

- 4
- [a] : ABCD is a parallelogram > M is the intersection point of its diagonals.
  - .. M is the midpoint of AC
  - In  $\triangle$  ABC :  $\overrightarrow{MO}$  //  $\overrightarrow{AB}$
  - , M is the midpoint of AC
  - .. O is the midpoint of BC
  - ∴ BO = OC
- (Q.E.D.)
- **[b]** In  $\triangle$  XYZ:  $\cdots$  m ( $\angle$  X) = 90°
  - $(XY)^2 = (YZ)^2 (XZ)^2 = 400 256 = 144$
  - $\therefore XY = \sqrt{144} = 12 \text{ cm}.$
- (The req.)

### 5

- $[a] : B \in \overline{AE}$ 
  - $m (\angle ABC) = 180^{\circ} 130^{\circ} = 50^{\circ}$
  - .. From the quadrilateral ABCD :
  - $m (\angle C) = 360^{\circ} (50^{\circ} + 80^{\circ} + 120^{\circ})$ 
    - $=360^{\circ} 250^{\circ} = 110^{\circ}$
- (The req.)

[b]



- (1)  $\triangle \overrightarrow{ABC}$  is the image of  $\triangle ABC$  by translation 2 AB in direction  $\overrightarrow{AB}$
- (2) Δ ABC is the image of Δ ABC by rotation about B with an angle of measure 180°

# Model 6

## [1]

- ① (b)
- (b) (2) (c)
- (3) (a)
- (4) (a)
- (5) (b)

- [2]
- (1) equal to the sum of the measures of its non adjacent interior angles
- (2) square
- (3) 130°
- (4)(-2,2)
- (5)  $(XY)^2 + (YZ)^2$

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# Maths

16cm.

### Answers of final examinations

3

[a] : ED // CB , BE is a transversal

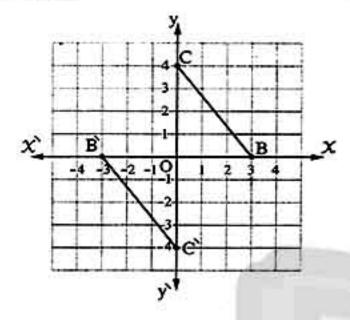
 $\therefore$  m ( $\angle$  B) = m ( $\angle$  E) = 40° (alternate angles)

:. In  $\triangle$  ABC: m ( $\angle$  BAC) = 180° - (50° + 40°) = 90°

∴ AC ⊥ BE

(Q.E.D.)

[b]



[4]

[a] In  $\triangle$  ABC: m ( $\angle$  ACB) = 180° - (90° + 40°) = 50°

 $, :: \overline{BD} \cap \overline{AO} = \{C\}$ 

 $\therefore m (\angle DCO) = m (\angle ACB) = 50^{\circ} \qquad (V.O.A.)$ 

: AB // DE , BD is a transversal

 $\therefore$  m ( $\angle$  B) = m ( $\angle$  D) = 90° (alternate angles)

From the quadrilateral CDEO

 $\therefore$  m ( $\angle$  E) = 360° - (90° + 50° + 130°) = 90°

(The req.)

[b] : The sum of measures of the interior angles of the triangle = 180°

 $x + 3x + 2x = 180^{\circ}$ 

 $\therefore 6 x = 180^{\circ}$ 

 $\therefore x = \frac{180^{\circ}}{6} = 30^{\circ}$ 

 $\therefore$  m ( $\angle$  A) =  $X = 30^{\circ}$   $\Rightarrow$  m ( $\angle$  B) = 3  $X = 90^{\circ}$ 

 $m (\angle C) = 2 X = 60^{\circ}$ 

(The req.)

#### 5

[a] In  $\triangle$  XYZ:

: D is the midpoint of XY > E is the midpoint of XZ

: DE =  $\frac{1}{2}$  ZY =  $\frac{1}{2}$  × 12 = 6 cm.

• E is the midpoint of X Z • O is the midpoint of ZY

 $\therefore EO = \frac{1}{2} \times XY = \frac{1}{2} \times 6 = 3 \text{ cm}.$ 

, O is the midpoint of  $\overline{ZY}$ , D is the midpoint of  $\overline{XY}$ 

 $\therefore OD = \frac{1}{2} \times XZ = \frac{1}{2} \times 8 = 4 \text{ cm}.$ 

 $\therefore$  The perimeter of  $\triangle$  DOE = 6 + 3 + 4 = 13 cm.

(The req.)

[b] Construction : Draw DE ⊥ BC

Proof: ABED is a rectangle

 $\therefore$  DE = AB = 12 cm.

AD = BE = 16 cm.

 $\therefore$  EC = 25 - 16 = 9 cm.

, ∵ m (∠ DEC) = 90°

 $\therefore$  (DC)<sup>2</sup> = (DE)<sup>2</sup> + (EC)<sup>2</sup> = 144 + 81 = 225

:. DC =  $\sqrt{225}$  = 15 cm.

(The req.)

## Model

1

(1) (b) (2) (a)

(3) (c)

(4) (a)

(3) right (4) (-2,2) (5) 90°

(5) (b)

2

(1) 540°

[a] : DE // BC → AB is a transversal

(2) 120°

 $\therefore$  m ( $\angle$  B) = m ( $\angle$  EAB) = 120° (alternate angles)

 $\rightarrow :: m (\angle B) + m (\angle C) = 120^{\circ} + 60^{\circ} = 180^{\circ}$ 

and they are interior angles on the same side of the transversal

: AB // CD

, ∵ DA // CB

.. ABCD is a parallelogram

(Q.E.D.)

[b] In  $\triangle$  ABC:

.. D is the midpoint of AB , E is the midpoint of AC

 $\therefore$  ED =  $\frac{1}{2}$  BC

∴ BC = 2 ED

 $\therefore BC = 2 \times 5 = 10 \text{ cm}.$ 

(The req.)

4

[a] : The sum of measures of the interior angles of the pentagon = (5 - 2) × 180° = 540°

 $m (\angle D) = 540^{\circ} - (110^{\circ} + 70^{\circ} + 120^{\circ} + 150^{\circ})$ = 90° (The req.)

[b] In  $\triangle$  ABC:  $\because$  m ( $\angle$  B) = 90°

 $\therefore$  (AB)<sup>2</sup> = (AC)<sup>2</sup> - (BC)<sup>2</sup> = 400 - 144 = 256

∴ AB = 16 cm.

 $\therefore$  AD = AB - DB = 16 - 9 = 7 cm.

 $\rightarrow$ : AE = 2 BC

 $AE = 2 \times 12 = 24$ 

, : AE // BC , AB is a transversal

 $\therefore$  m ( $\angle$  A) = m ( $\angle$  B) = 90° (alternate angles)

 $(ED)^2 = (AD)^2 + (AE)^2 = 49 + 576 = 625$ 

∴ ED =  $\sqrt{625}$  = 25

(The req.)

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[a] : ABCD is a parallelogram

$$\therefore m (\angle B) + m (\angle C) = 180^{\circ}$$

$$\therefore$$
 m ( $\angle$  C) = 180° - 135° = 45°

, ∵ ABCD is a parallelogram

$$\therefore$$
 AB = CD = 5 cm.  $\Rightarrow$  AD = BC = 8 cm.

[b] (1) A ADC

(2) ∆ MBC

### Model

1

(1) (a)

(2) (c)

(3) (c)

(4) (b)

8

(5) (d)

[2]

(1) half the length of the third side.

(2) square

(3) 5 cm.

(4)(3,-4),(-3,4) (5) (5,-1)

(3)

[a] : DA // BE , BD is a transversal

$$\therefore$$
 m ( $\angle$  CBD) = m ( $\angle$  ADB) = 50° (alternate angles)

:. 
$$m (\angle DBE) = 180^{\circ} - 50^{\circ} = 130^{\circ}$$

, ∵ BA bisects ∠ DBE

∴ m (
$$\angle$$
 ABE) =  $\frac{130^{\circ}}{2}$  = 65°

$$\rightarrow$$
: m ( $\angle$  C) = m ( $\angle$  ABE) = 65°

and they are corresponding angles

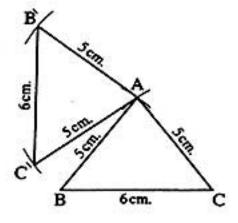
: AB // CD

, : AD // BC

.. ABCD is a parallelogram.

(Q.E.D.)

[b]



[a] : DE // CB , BD is a transversal

$$\therefore$$
 m ( $\angle$  B) = m ( $\angle$  D) = 50° (alternate angles)

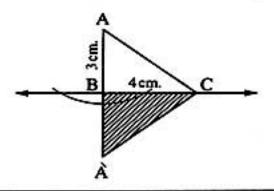
(First req.)

From  $\triangle$  ABC:

$$m (\angle BAC) = 180^{\circ} - (35^{\circ} + 50^{\circ}) = 95^{\circ}$$

(Second req.)

[b]



[5]

[a] : ABCD is a parallelogram

: AB // DC

:. XC // AB

In △ ABE: ... C is the midpoint of BE

,XC // AB

.. X is the midpoint of AE

$$\therefore AX = XE$$

(Q.E.D.)

[b] In  $\triangle$  BCD:  $\therefore$  m ( $\angle$  B) = 90°

$$(BD)^2 = (DC)^2 - (BC)^2 = 169 - 144 = 25$$

∴ BD = 
$$\sqrt{25}$$
 = 5 cm.

$$\therefore$$
 AB = 5 + 11 = 16 cm.

In 
$$\triangle$$
 ABC:  $\cdots$  m ( $\angle$  B) = 90°

$$(AC)^2 = (AB)^2 + (BC)^2 = 256 + 144 = 400$$

$$\therefore$$
 AC =  $\sqrt{400}$  = 20 cm.

(The req.)

## Answers of school examinations in Geometry and measurement

# Cairo

#### 1

- (1) (b)
- (2) (a)
- (3) (a)
- (4)(c)
- (5) (a)

### 2

- (1)(-5,0)
- (2) XZ, YL
- (3) acute

- (4) bisects
- (5) 90°

#### 3

- [a] In  $\triangle$  ADB :  $\cdots$  m ( $\angle$  ADB) = 90°
  - $(BD)^2 = (AB)^2 (AD)^2 = (26)^2 (24)^2 = 100$
  - ∴ BD =  $\sqrt{100}$  = 10 cm.

In  $\triangle$  ADC:  $\therefore$  m ( $\angle$  ADC) = 90°

- $(CD)^2 = (AC)^2 (AD)^2 = (30)^2 (24)^2 = 324$
- $\therefore$  CD =  $\sqrt{324}$  = 18 cm.
- BC = 10 + 18 = 28 cm.
- $\therefore$  The area of  $\triangle$  ABC =  $\frac{1}{2} \times 28 \times 24 = 336$  cm<sup>2</sup>.

(The req.)

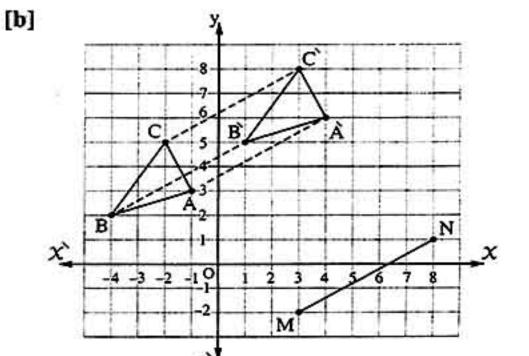
- [b] : AB // DE , BD is a transversal
  - $\therefore$  m ( $\angle$  B) = m ( $\angle$  D) = 60° (alternate angles)
  - → ∴ ∠ AOD is an exterior angle of Δ ABO
  - $\therefore m (\angle AOD) = m (\angle A) + m (\angle B)$
  - $m (\angle A) = 100^{\circ} 60^{\circ} = 40^{\circ}$

(The req.)

#### 4

- [a] In △ ABC: ... X is the mid-point of AB
  - , Y is the midpoint of BC
  - $\therefore XY = \frac{1}{2}AC$
- $\therefore$  AC = 28 cm.
- , : X is the mid-point of AB, Z is the mid-point of AC
- $\therefore XZ = \frac{1}{2}BC$
- $\therefore$  BC = 20 cm.
- , .. Y is the mid-point of BC, Z is the mid-point of AC
- $\therefore$  YZ =  $\frac{1}{2}$  AB
- $\therefore$  AB = 24 cm.
- $\therefore$  The perimeter of  $\triangle$  ABC = 28 + 20 + 24 = 72 cm.

(The req.)



### 5

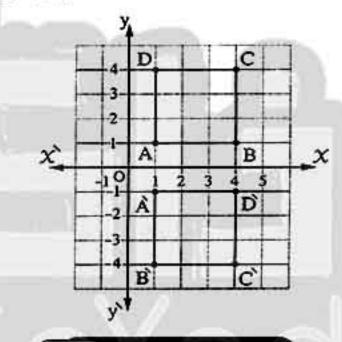
- [a]  $: \overline{AD} / | \overline{XY} / | \overline{BC} \to AX = XB$ 
  - $\therefore$  DY = YC
- .: Y is the midpoint of CD

In △ CDE: ... ZY // DE, Y is the midpoint of CD

- .. Z is the midpoint of CE
- ∴ CZ = ZE

(Q.E.D.)

[b]



## Cairo

- (2)(d) (3)(c)
- (4) (b)
- (5) (a)

2

- (2) (8 , 2) (3) half the length of the third side (1) 12
  - (5) rhombus

3

(4) y

- [a] : OH // BC , OB is a transversal
  - $\therefore$  m ( $\angle$  B) + m ( $\angle$  O) = 180°

(Two interior angles in the same side of the transversal)

- $m (\angle B) = 180^{\circ} 135^{\circ} = 45^{\circ}$
- · DE // BC , CD is a transversal

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#### $\therefore$ m ( $\angle$ C) + m ( $\angle$ D) = 180°

(Two interior angles in the same side of the transversal)

$$m (\angle C) = 180^{\circ} - 120^{\circ} = 60^{\circ}$$

In 
$$\triangle$$
 ABC :  $\therefore$  m ( $\angle$  BAC) = 180° - (45° + 60°) = 75°

(The req.)

#### [b] : ABCD is a parallelogram , M is the intersection point of its diagonals.

.. M is the midpoint of AC

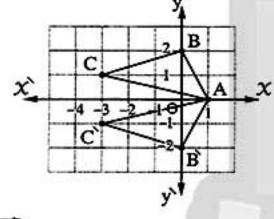
In △ ABC: :: M is the midpoint of AC, MO // AB

.. O is the midpoint of BC

(Q.E.D.)

#### [4]

[a]



#### [b] ∵ C ∈ BF

$$\therefore$$
 m ( $\angle$  BCD) = 180° - 30° = 150°

From the pentagon ABCDE:

$$\therefore m (\angle D) = 540^{\circ} - (120^{\circ} + 70^{\circ} + 110^{\circ} + 150^{\circ})$$
= 90° (The req.)

### [5]

#### [a] In $\triangle$ ADB : $\cdots$ m ( $\angle$ ADB) = 90°

$$\therefore (BD)^2 = (AB)^2 - (AD)^2 = (26)^2 - (24)^2 = 100$$

∴ BD = 
$$\sqrt{100}$$
 = 10 cm.

In  $\triangle$  ADC:  $\therefore$  m ( $\angle$  ADC) = 90°

$$\therefore$$
 (CD)<sup>2</sup> = (AC)<sup>2</sup> - (AD)<sup>2</sup> = (30)<sup>2</sup> - (24)<sup>2</sup> = 324

 $\therefore$  CD =  $\sqrt{324}$  = 18 cm.

$$\therefore$$
 BC = 10 + 18 = 28 cm.

(First req.)

$$\therefore$$
 The area of  $\triangle$  ABC =  $\frac{1}{2} \times 28 \times 24 = 336$  cm<sup>2</sup>.

(Second req.)

**[b]** From 
$$\triangle$$
 ABC : m ( $\angle$  ACB) = 180° - (90° + 30°) = 60°

$$\therefore \overline{BD} \cap \overline{AO} = \{C\}$$

$$\therefore$$
 m ( $\angle$  ACB) = m ( $\angle$  DCO) = 60°

(V.O.A)

.. From the quadrilateral CDEO

$$m (\angle E) = 360^{\circ} - (120^{\circ} + 60^{\circ} + 90^{\circ}) = 90^{\circ}$$

(The req.)

## Cairo

#### 1

### [2]

- (1) 130°
- (2)(2,4)
- (3) 180°
- (4) bisects the third side
- (5)90

### 3

### [a] From $\triangle$ BEF: m ( $\angle$ EBF) = 180° - (90° + 50°) = 40°

$$\because \overline{AE} \cap \overline{CF} = \{B\}$$

$$\therefore$$
 m ( $\angle$  ABC) = m ( $\angle$  EBF) = 40° (V.O.A)

$$\therefore$$
 m ( $\angle$  A) = m ( $\angle$  E) = 90° (alternate angles)

.. From the quadrilateral ABCD :

$$m (\angle C) = 360^{\circ} - (110^{\circ} + 90^{\circ} + 40^{\circ}) = 120^{\circ}$$

(The req.)

**[b]** The number of sides = 
$$\frac{360^{\circ}}{180^{\circ} - 135}$$
 = 8 sides.

### 4

### [a] In AABC: : D is the mid-point of AB, E is the mid-point of BC

:. DE = 
$$\frac{1}{2}$$
 AC =  $\frac{1}{2}$  × 10 = 5 cm.

, .. D is the midpoint of AB, F is the midpoint of AC

$$\therefore DF = \frac{1}{2} BC = \frac{1}{2} \times 8 = 4 cm.$$

. E is the midpoint of BC, F is the midpoint

∴ EF = 
$$\frac{1}{2}$$
 AB =  $\frac{1}{2}$  × 6 = 3 cm.

 $\therefore$  The perimeter of  $\triangle$  DEF = 5 + 4 + 3 = 12 cm.

(The req.)

#### [b] In $\triangle$ CBD: $\cdots$ m ( $\angle$ B) = 90°

$$\therefore (BD)^2 = (CD)^2 - (BC)^2 = (13)^2 - (12)^2 = 25$$

∴ BD = 
$$\sqrt{25}$$
 = 5 cm.

$$\therefore$$
 AB = 11 + 5 = 16 cm.

In 
$$\triangle$$
 ABC:  $\cdots$  m ( $\angle$  B) = 90°

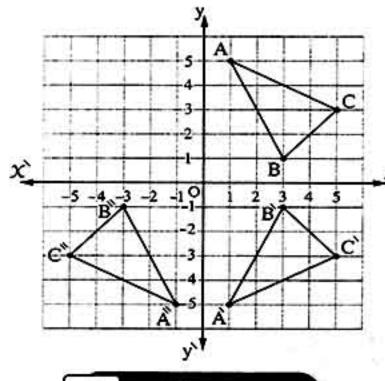
$$\therefore (AC)^2 = (AB)^2 + (BC)^2 = (16)^2 + (12)^2 = 400$$

∴ AC = 
$$\sqrt{400}$$
 = 20 cm.

(The req.)

المحاصد ریاضیات لغات (اِجابات) / ۱ اِعدادی / تیری ۲ (م : ۱)

5



Giza

11

- (1) (a)
- (a) (d)
- (3) (c)
- (4) (d)
- (5) (a)

2

- (1) parallel to the third side
- (2)(1,0)
- (3) rectangle
- (4) 108
- (5) 180

3

- [a] : DA  $\cap$  EB = {M}
  - $\therefore$  m ( $\angle$  BMD) = m ( $\angle$  AME) = 72° (V.O.A)
  - . MC bisects ∠ BMD
  - $\therefore$  m ( $\angle$  CMD) =  $\frac{72^{\circ}}{2}$  = 36°

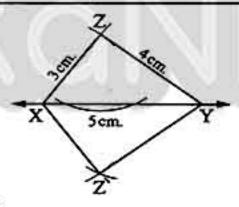
(The req.)

- [b] :  $m (\angle ABC) = m (\angle BAC)$ 
  - → ∠ ACD is an exterior angle of △ ABC
  - ∴ m ( $\angle$  ABC) =  $\frac{128^{\circ}}{2}$  = 64°

(The req.)

4

[a]



[b] In  $\triangle$  ABC:

- .. D is the midpoint of AB , E is the midpoint of AC
- : ED =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 10 = 5 cm.
- , .. D is the midpoint of AB, F is the midpoint of BC
- $\therefore DF = \frac{1}{2} AC = \frac{1}{2} \times 6 = 3 cm.$
- , .. E is the midpoint of AC, F is the midpoint of BC

- ∴ EF =  $\frac{1}{2}$  AB =  $\frac{1}{2}$  × 8 = 4 cm.
- $\therefore$  The perimeter of  $\triangle$  DEF = 5 + 3 + 4 = 12 cm.

(The req.)

[5]

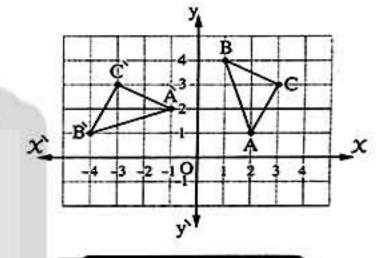
- [a] : BA // DF , BD is a transversal
  - $\therefore$  m ( $\angle$  D) = m ( $\angle$  B) = 60° (alternate angles)

In  $\triangle$  CDF:

 $m (\angle DCF) = 180^{\circ} - (40^{\circ} + 60^{\circ}) = 80^{\circ}$ 

(The req.)

[b]



Giza

[1]

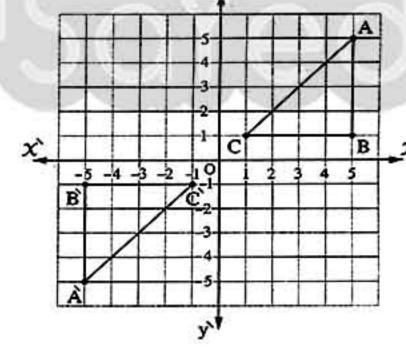
- (1) (b)
  - (2)(c)
- (3)(c)
- (4) (b)
- (5) (c)

2

- (1) bisects the third side
- (2)(2,5)
- (3) 8
- (4) equal in length, bisect each other, perpendicular
- (5) trapezium

3

[a]



[b] : EC = CF = FE

- ∴ ∆ CEF is an equilateral triangle
- $\therefore m (\angle ECF) = \frac{180^{\circ}}{3} = 60^{\circ}$
- $\therefore \overline{BF} \cap \overline{ED} = \{c\}$

$$\therefore$$
 m ( $\angle$  BCD) = m ( $\angle$  ECF) = 60° (V.O.A)

$$m (\angle B) = 360^{\circ} - (115^{\circ} + 98^{\circ} + 60^{\circ}) = 87^{\circ}$$

(The req.)

[a] m (
$$\angle$$
 HBD) = 360° - (135° + 110° + 45°) = 70°

(The req.)

$$\therefore$$
 m ( $\angle$  D) = m ( $\angle$  A) = 65° (alternate angles)

$$m (\angle ACE) = 65^{\circ} + 35^{\circ} = 100^{\circ}$$

(The req.)

[a] In 
$$\triangle$$
 ABC :  $\therefore$  m ( $\angle$  B) = 90°

$$\therefore (AC)^2 = (AB)^2 + (BC)^2 = (3)^2 + (4)^2 = 25$$

$$\therefore$$
 AC =  $\sqrt{25}$  = 5 cm.

In 
$$\triangle$$
 ACD: :: m ( $\angle$  ACD) = 90°

$$(AD)^2 = (AC)^2 + (CD)^2 = (5)^2 + (12)^2 = 169$$

∴ AD = 
$$\sqrt{169}$$
 = 13 cm.

$$= 3 + 4 + 12 + 13 = 32$$
 cm.

(The req.)

#### [b] In Δ ABC:

: X is the midpoint of AB, Y is the midpoint of BC

:. XY = 
$$\frac{1}{2}$$
 AC =  $\frac{1}{2}$  × 9 = 4.5 cm.

. . X is the midpoint of AB, Z is the midpoint of AC

∴ 
$$XZ = \frac{1}{2} BC = \frac{1}{2} \times 11 = 5.5 \text{ cm}.$$

Y is the midpoint of BC, Z is the midpoint of AC

: YZ = 
$$\frac{1}{2}$$
 AB =  $\frac{1}{2}$  × 10 = 5 cm.

 $\therefore$  The perimeter of  $\triangle XYZ = 4.5 + 5.5 + 5 = 15$  cm.

(The req.)

# Alexandria

#### 

- **①**(b)
- (2) (b)
- (3) (b)
- (4) (c)

(5) (b)

### 2

- (1) 360°
- (2) AC, BD
- (3)(9,-1)
- (4) (AC)<sup>2</sup>, (BC)<sup>2</sup> (5) bisects the third side

[a] In 
$$\triangle$$
 ABC:  $\cdots$  m ( $\angle$  B) = 90°

$$(AC)^2 = (AB)^2 + (BC)^2 = (7)^2 + (24)^2 = 625$$

### ∴ AC = $\sqrt{625}$ = 25 cm.

In 
$$\triangle$$
 ADC:  $\cdots$  m ( $\angle$  D) = 90°

$$\therefore (DC)^2 = (AC)^2 - (AD)^2 = (25)^2 - (15)^2 = 400$$

$$\therefore$$
 DC =  $\sqrt{400}$  = 20 cm.

(The req.)

**(b)** The number of sides = 
$$\frac{360^{\circ}}{180^{\circ} - 120^{\circ}} = 6$$
 sides

#### 4

#### [a] In $\triangle$ ABC:

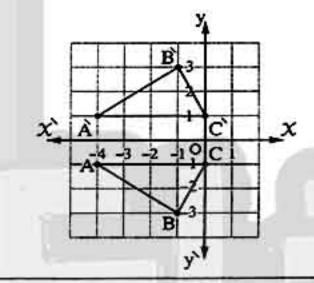
- .. D is the midpoint of AB , E is the midpoint of AC
- ∴ DE // BC
- :. DE // BF
- (1)

(2)

From (1) and (2): .: BEDF is a parallelogram

(Q.E.D.)

[b]



### [a] : DC // AB , AD is a transversal

$$\therefore m (\angle A) + m (\angle D) = 180^{\circ}$$

(Two interior angles in the same side of the transversal)

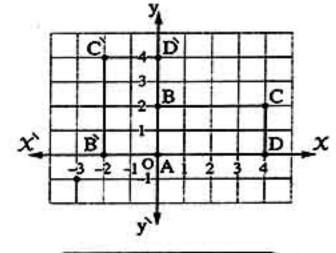
$$m (\angle A) = 180^{\circ} - 127^{\circ} = 53^{\circ}$$

 $\therefore$  m ( $\angle$  A) = m ( $\angle$  CBE) = 53° and they are corresponding angles

:. AD // BC

(QED.)

[b]



# Alexandria

#### 1

- (1) (d)
- (2) (b)
- (3)(c)
- (c)
- (5) (b)

83

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# Maths

### Answers of final examinations

2

- (1)75
- $(2) \pm 360$
- (3)(-4,-2)

- (4) 70
- (5) obtuse

- [a] In  $\triangle$  ABC:
  - .. X is the midpoint of AB, Y is the midpoint of AC
  - : XY // BC

In ∆ XYZ: : D is the midpoint of XZ

- , ED // XY
- .. E is the midpoint of YZ
- $\therefore YE = EZ$

(Q.E.D.)

[b] The measure of the interior angle =  $\frac{(10-2) \times 180^{\circ}}{}$ = 144°

- [a] In  $\triangle$  XYZ:  $\cdots$  m ( $\angle$  XYZ) = 90°
  - $\therefore (XZ)^2 = (XY)^2 + (YZ)^2 = (7)^2 + (24)^2 = 625$
  - $\therefore XZ = \sqrt{625} = 25 \text{ cm}.$

In  $\triangle$  XLZ:  $\cdots$  m ( $\angle$  XLZ) = 90°

- $\therefore (LZ)^2 = (XZ)^2 (LX)^2 = (25)^2 (15)^2 = 400$
- :. LZ =  $\sqrt{400}$  = 20 cm.

[b] The translation (LM) = M - L = (1, 5) - (2, 3)

$$=(-1,2)$$

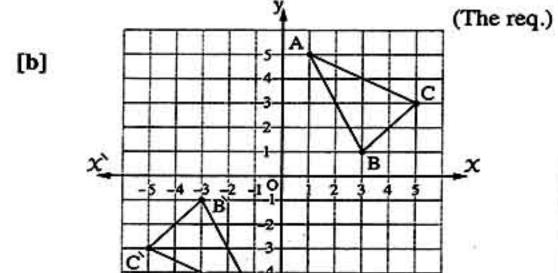
.. The point A = The image - The translation

$$=(-6,4)-(-1,2)=(-5,2)$$

5

- [a] : ABCD is a parallelogram
  - :. AD // BC , BD is a transversal
  - $\therefore$  m ( $\angle$  DBC) = m ( $\angle$  ADB) = 80° (alternate angles)

In  $\triangle$  BMC :  $\therefore$  m ( $\angle$  CMB) = 180° - (30° + 80°) = 70°



# El-Kalyoubia

[1]

- (1) (b)
- (2)(c)
- (3) (a)
- (4) (d)
- (5) (a)

[2]

- (1) right
- (2) parallel to the third side
- (3)(-3,-2)
- $(4)(AB)^2,(BC)^2$
- (5) 45

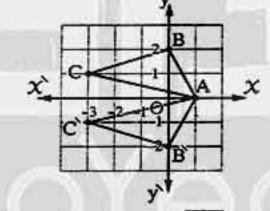
3

- [a] In  $\triangle$  ABC:
  - .. D is the midpoint of AB , E is the midpoint of AC
  - ∴ DE =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 10 = 5 cm.
  - : AD =  $\frac{1}{2}$  AB =  $\frac{1}{2}$  × 12 = 6 cm.
  - $AE = \frac{1}{2}AC = \frac{1}{2} \times 8 = 4 \text{ cm}.$
  - $\therefore$  The perimeter of  $\triangle$  ADE = 5 + 6 + 4 = 15 cm.

(The req.)

- [b] : B ∈ AC
  - $m (\angle ABE) = 180^{\circ} 106^{\circ} = 74^{\circ}$
  - ∵ BD bisects ∠ ABE
  - :. m ( $\angle$  ABD) = 74° ÷ 2 = 37°
- (The req.)

4 [a]



- [b] : ABCD is a rhombus and BD is a diagonal in it.
  - $\therefore$  m ( $\angle$  ABC) = 2 m ( $\angle$  ABD) = 2 × 62° = 124°
  - $m (\angle A) = 180^{\circ} 124^{\circ} = 56^{\circ}$
- (The req.)

5

- [a] :  $m (\angle X) = 90^{\circ}$ 
  - $(XY)^2 = (YZ)^2 (XZ)^2 = (20)^2 (16)^2 = 144$
- ∴ XY =  $\sqrt{144}$  = 12 cm.
- (The req.)

- [b] (1) Δ CON
- (2)  $\Delta$  LNB
- (3) A BON

El-Sharkia

1

- (1) 180
- $(2)(AB)^2, (BC)^2$
- (3) the third side

- (4) 540
- (5) (4,2)

هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى والمعلقة

#### 2

- (1) (a)
- (a) (p)
- (3) (a)
- (4)(c)
- (5) (c)

### 3

- [a] ∵ M∈AB
  - $m (\angle BME) = 180^{\circ} 110^{\circ} = 70^{\circ}$
  - .. MC bisects ∠ BME
  - ∴ m ( $\angle$  BMC) = 70° ÷ 2 = 35°
  - $\therefore \overrightarrow{AB} \cap \overrightarrow{CD} = \{M\}$
  - $\therefore$  m ( $\angle$  AMD) = m ( $\angle$  BMC) = 35° (V.O.A)

(The req.)

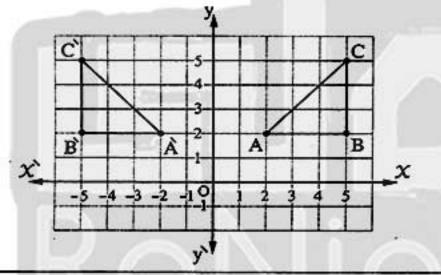
- [b] : DE // BC , DC is a transversal
  - $\therefore$  m ( $\angle$  C) = m ( $\angle$  D) = 30° (alternate angles)
  - ∴ ∠ DAB is an exterior angle of ∆ ABC
  - $\therefore$  m ( $\angle$  ABC) = 80° 30° = 50°

(The req.)

#### 4

[a] The measure of each interior angle =  $\frac{(6-2) \times 180^{\circ}}{}$  $= 120^{\circ}$ 

[b]



#### 5

#### In A ABC:

- $\because$  X is the midpoint of AB  $\rightarrow$  Y is the midpoint of  $\overline{AC}$
- :  $XY = \frac{1}{2}BC = \frac{1}{2} \times 8 = 4$  cm.
- : X is the midpoint of AB, Z is the midpoint of BC
- :  $XZ = \frac{1}{2} AC = \frac{1}{2} \times 10 = 5 \text{ cm}.$
- .. Y is the midpoint of AC , Z is the midpoint of BC
- $\therefore YZ = \frac{1}{2} AB = \frac{1}{2} \times 6 = 3 cm.$
- $\therefore$  The perimeter of  $\triangle XYZ = 4 + 5 + 3 = 12$  cm.

(The req.)

## Suez

- ① (b) (2)(c)
- (3) (a)
- (4) (c)
- (5) (c)

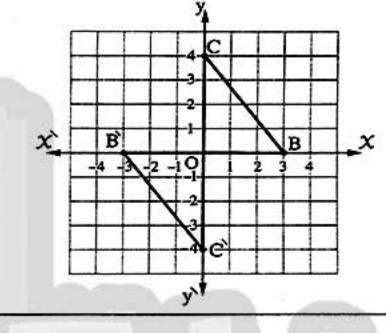
#### 2

- (1) half the length of the third side (2)(5,-1)
- (3) 180°
- (4) square
- (5)(-3,-2)

#### 3

- [a] : ABCD is a parallelogram
  - $m (\angle C) = 180^{\circ} 135^{\circ} = 45^{\circ}$
- (First req.)
- The perimeter of parallelogram ABCD
- $= (8 + 5) \times 2 = 26$  cm.
- (Second req.)

[b]



#### [4]

#### [a] In $\triangle$ ABC:

- .. D is the midpoint of AB , O is the midpoint of AC
- :. DO =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 8 = 4 cm.
- .. D is the midpoint of AB , E is the midpoint of BC
- ∴ DE =  $\frac{1}{2}$  AC =  $\frac{1}{2}$  × 10 = 5 cm.
- .. O is the midpoint of AC , E is the midpoint of BC
- ∴ OE =  $\frac{1}{2}$  AB =  $\frac{1}{2}$  × 6 = 3 cm.
- $\therefore$  The perimeter of  $\triangle$  DEO = 4 + 5 + 3 = 12 cm.

(The req.)

- [b] : AB // DE , BD is a transversal
  - $\therefore$  m ( $\angle$  B) = m ( $\angle$  D) = 60° (alternate angles)
  - ∴ ∠ ACD is an exterior angle of ∆ ABC
  - $\therefore$  m ( $\angle$  A) = 110° 60° = 50°
- (The req.)

#### [5]

- [a] In  $\triangle$  ABC:  $\cdots$  m ( $\angle$  B) = 90°
  - $(AC)^2 = (AB)^2 + (BC)^2 = (12)^2 + (9)^2 = 225$
  - $\therefore$  AC =  $\sqrt{225}$  = 15 cm.
  - In  $\triangle$  ACD:  $\therefore$  m ( $\angle$  ACD) = 90°
  - $(AD)^2 = (AC)^2 + (CD)^2 = (15)^2 + (20)^2 = 625$
  - :. AD =  $\sqrt{625}$  = 25 cm.

(The req.)

- [b] (1) \$\D LNB
- (2)  $\Delta$  DOM

# El-Beheira

(3) (b)

- (1) (b)
- (2) (a)
- (4)(c)
- (5) (a)

### 2

- (1) parallel to
- (2) C
- (3)(3,2)

- (4) (-7, -3)
- (5) (-2,-4)

### 3

- [a]  $:: B \in \overrightarrow{AC}$   $:: m (\angle ABE) = 180^{\circ} 116^{\circ} = 64^{\circ}$ 
  - : BD bisects ∠ ABE
  - $m (\angle ABD) = 64^{\circ} \div 2 = 32^{\circ}$
- (The req.)
- [b] :  $2 \times = 720^{\circ} (110^{\circ} + 90^{\circ} + 165^{\circ} + 115^{\circ}) = 240^{\circ}$ 
  - $\therefore X = 240^{\circ} \div 2 = 120^{\circ}$
- (The req.)

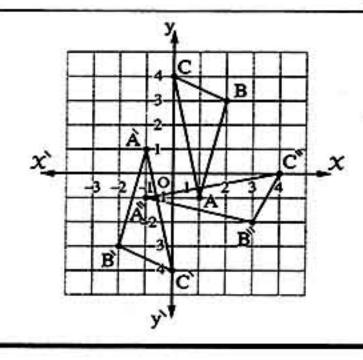
- [a] In  $\triangle$  ADB :  $\cdots$  m ( $\angle$  ADB) = 90°
  - $\therefore (BD)^2 = (AB)^2 (AD)^2 = (26)^2 (24)^2 = 100$
  - ∴ BD =  $\sqrt{100}$  = 10 cm.
  - In  $\triangle$  ADC:  $\therefore$  m ( $\angle$  ADC) = 90°
  - $\therefore (CD)^2 = (AC)^2 (AD)^2 = (30)^2 (24)^2 = 324$
  - :. CD =  $\sqrt{324}$  = 18 cm.
  - $\therefore$  BC = 10 + 18 = 28 cm.
- (The req.)

#### [b] In $\triangle$ ABC:

- .. D is the midpoint of AB , E is the midpoint of BC
- :. DE =  $\frac{1}{2}$  AC =  $\frac{1}{2}$  × 7 = 3.5 cm.
- .. D is the midpoint of AB , F is the midpoint of AC
- :. DF =  $\frac{1}{2}$  BC =  $\frac{1}{2} \times 8 = 4$  cm.
- .. E is the midpoint of BC . F is the midpoint of AC
- ∴ EF =  $\frac{1}{2}$  AB =  $\frac{1}{2}$  × 5 = 2.5 cm.
- $\therefore$  The perimeter of  $\triangle$  DEF = 3.5 + 4 + 2.5 = 10 cm.

(The req.)

### 5



# Beni Suef

#### 1

- (1) (c)
- (2) (b)
- (3) (b)
- (4) (b)
- (5) (c)

### [2]

- (1) rhombus
- (2) parallel to the third side
- (3) bisects the third side (4) (-4,-1)
- (5) 120°

### 3

- [a] The sum =  $(6-2) \times 180^{\circ} = 720^{\circ}$
- [b] : ABCD is a rhombus , AC is a diagonal in it
  - $\therefore$  m ( $\angle$  BCD) = 2 m ( $\angle$  ACB) = 2 × 62° = 124°
  - $m (\angle B) = 180^{\circ} 124^{\circ} = 56^{\circ}$
- (The req.)

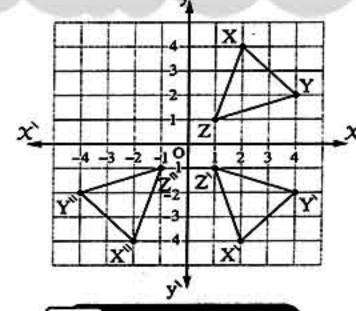
#### 4

- [a] In  $\triangle$  ABC:
  - .. D is the midpoint of AB , E is the midpoint of BC
  - :. DE =  $\frac{1}{2}$  AC =  $\frac{1}{2}$  × 10 = 5 cm.
  - : D is the midpoint of AB, F is the midpoint of AC
  - ∴ DF =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 12 = 6 cm.
  - , .. F is the midpoint of AC
  - :. FC =  $\frac{1}{2}$  AC =  $\frac{1}{2}$  × 10 = 5 cm.
  - , .: E is the midpoint of BC
  - :. EC =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 12 = 6 cm.
  - $\therefore$  The perimeter of DECF = 5 + 6 + 5 + 6 = 22 cm.

(The req.)

- [b]  $: m (\angle X) = 90^{\circ}$ 
  - $\therefore (XY)^2 = (YZ)^2 (XZ)^2 = (20)^2 (16)^2 = 144$
  - $\therefore XY = \sqrt{144} = 12 \text{ cm}.$
- (The req.)

# 5



## El-Menia

#### [1]

- ① (b)
- (2) (a)
- (3) (b)
- (4) (b)
- (5) (a)

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هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

2

- (2)(8,2)(1) rhombus
- (3) 120°
- (4) 180°

(5) bisects the third side

- [a] : DE // BC , BD is a transversal
  - $\therefore$  m ( $\angle$  B) = m ( $\angle$  D) = 60° (alternate angles)
  - ∴ ∠ CAD is an exterior angle of Δ ABC
  - $m (\angle C) = 100^{\circ} 60^{\circ} = 40^{\circ}$

(The req.)

- [b] In ∆ ABC:
  - .. D is the midpoint of AB , E is the midpoint of BC
  - ∴ DE =  $\frac{1}{2}$  AC =  $\frac{1}{2}$  × 10 = 5 cm.
  - .. D is the midpoint of AB, F is the midpoint of AC
  - : DF =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 12 = 6 cm.
  - , .. F is the midpoint of AC
  - :. FC =  $\frac{1}{2}$  AC =  $\frac{1}{5}$  × 10 = 5 cm.
  - , .. E is the midpoint of BC
  - : EC =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 12 = 6 cm.
  - $\therefore$  The perimeter of DECF = 5 + 6 + 5 + 6 = 22 cm.

(The req.)

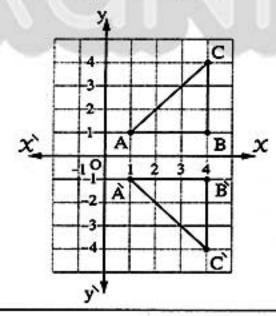
- [a]  $\cdot \cdot \cdot m (\angle BAE) + m (\angle EAC) + m (\angle CAB) = 360^{\circ}$ (accumulative at A)
  - $\therefore$  m ( $\angle$  CAB) = 360° (150° + 90°) = 120°
  - : AB // CD , AC is a transversal
  - $\therefore$  m ( $\angle$  CAB) + m ( $\angle$  C) = 180°

(interior angles in the same side of the transversal)

 $m (\angle C) = 180^{\circ} - 120^{\circ} = 60^{\circ}$ 

(The req.)

[b]

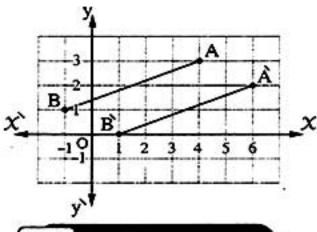


5

- [a]  $\ln \Delta ADC : : m (\angle ADC) = 90^{\circ}$ 
  - $(CD)^2 = (AC)^2 (AD)^2 = (30)^2 (24)^2 = 324$
  - $\therefore$  CD =  $\sqrt{324}$  = 18 cm.  $\therefore$  BC = 10 + 18 = 28 cm.
  - $\therefore$  The area of  $\triangle$  ABC =  $\frac{1}{2} \times 28 \times 24 = 336$  cm<sup>2</sup>.

(The req.)

[b]



# Aswan

[1]

- (1)(c) (2) (a)
- (3) (a)
- (4) (d)
- (5) (b)

2

- (1)(0,5)(2)45°
- (3) (5,4) (4) 360 (5) 120

3

- [a] (1) D (2) ∆ BYM
- [b] In  $\triangle$  XYZ:  $\cdots$  m ( $\angle$  Y) = 90°
  - $\therefore (XZ)^2 = (XY)^2 + (YZ)^2 = (3)^2 + (4)^2 = 25$
  - $\therefore XZ = \sqrt{25} = 5 \text{ cm}.$

In  $\triangle$  LXZ:  $\therefore$  m ( $\angle$  LXZ) = 90°

- $\therefore (XL)^2 = (LZ)^2 (XZ)^2 = (13)^2 (5)^2 = 144$
- $\therefore XL = \sqrt{144} = 12 \text{ cm}.$

(The req.)

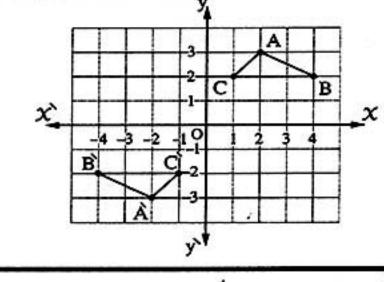
[4]

- [a] Let the measures of the angles of the quadrilateral
  - $\therefore 2x + 3x + 3x + 4x = 360^{\circ}$
  - $\therefore 12 x = 360^{\circ}$
- $\therefore x = 30^{\circ}$
- .. The measure of the smallest angle is: 60°
- [b] : AB // CD , AD is a transversal
  - $\therefore$  m ( $\angle$  D) = m ( $\angle$  A) = 50°
    - (alternate angles)
  - ∴ ∠ AEC is an exterior angle of Δ CDE
  - $m (\angle C) = 110^{\circ} 50^{\circ} = 60^{\circ}$
  - In  $\triangle$  CDE:  $\therefore$  m ( $\angle$  CED) = 180° (60° + 50°) = 70°

(The req.)

[5]

[a]



[b] : DA // CB , DC is a transversal

 $\therefore m (\angle D) + m (\angle C) = 180^{\circ}$ 

(interior angles in the same side of the transversal)

 $m (\angle D) = 180^{\circ} - 60^{\circ} = 120^{\circ}$ 

 $\therefore$  m ( $\angle$  D) = m ( $\angle$  BAE) = 120°

but they are corresponding angles

:. AB // CD

, ∵ <del>DA</del> // <del>CB</del>

.. ABCD a parallelogram

(Q.E.D.)

# 15 Southern Sinai

[1]

(1) (a) (

(2) (b)

(3) (c)

(4) (d)

(5) (d)

[2]

(1) parallelogram

(2) parallel to

(3)(-3,-2)

(4) The hypotenuse (5) 90

3

[a] The number of sides =  $\frac{360^{\circ}}{180^{\circ} - 135^{\circ}}$  = 8 sides

 $[b] : M \in \overline{AC}$ 

 $\therefore$  m ( $\angle$  BMC) = 180° - 75° = 105°

In  $\triangle$  BMC:

 $m (\angle BCM) = 180^{\circ} - (50^{\circ} + 105^{\circ}) = 25^{\circ}$ 

 $\therefore$  m ( $\angle$  BCA) = m ( $\angle$  CAD) = 25°

but they are alternate angles

: AD // BC

 $\cdots \overline{AB} / \overline{DC}$ 

.. ABCD is a parallelogram

(Q.E.D.)

4

 $[a] : m (\angle X) = 90^{\circ}$ 

 $\therefore (XZ)^2 = (YZ)^2 - (XY)^2 = (15)^2 - (12)^2 = 81$ 

∴ XZ =  $\sqrt{81}$  = 9 cm.

(The req.)

[b] In Δ ABC:

:: D is the midpoint of  $\overline{AB}$ , E is the midpoint of AC

∴ DE =  $\frac{1}{2}$  BC =  $\frac{1}{2}$  × 10 = 5 cm.

, ∵ D is the midpoint of AB

:. AD =  $\frac{1}{2}$  AB =  $\frac{1}{2}$  × 12 = 6 cm.

, ∵ E is the midpoint of AC

∴ AE =  $\frac{1}{2}$  AC =  $\frac{1}{2}$  × 8 = 4 cm.

 $\therefore$  The perimeter of  $\triangle$  ADE = 6 + 4 + 5 = 15 cm.

(The req.)

[5]

(1) AALO

(2)  $\Delta$  OYC

(3) ∆ CZO